

Last time: Solving Boundary-Value Problems in Magnetostatics

| Method                                | no Ferromagnetics<br>$\vec{B} = \mu \vec{H}$  | Ferromagnetics ( $\vec{M} \neq 0$ for $\vec{B}, \vec{H} = 0$ )  |
|---------------------------------------|---|---|
| $\vec{A}$                             | $\nabla^2 \vec{A} = -\mu \vec{J}$ $\Rightarrow \vec{A}(\vec{x}) = \frac{\mu}{4\pi} \int_V d^3x' \frac{\vec{J}(\vec{x}')}{ \vec{x} - \vec{x}' }$ | $\nabla^2 \vec{A} = -\mu_0 [\vec{J} + \nabla \times \vec{M}]$ $\vec{A}(\vec{x}) = \frac{\mu_0}{4\pi} \int_V d^3x' \frac{\vec{J}(\vec{x}') + \nabla' \times \vec{M}(\vec{x}')}{ \vec{x} - \vec{x}' }$ $+ \frac{\mu_0}{4\pi} \int_S da' \frac{\vec{K}(\vec{x}') + \vec{M}(\vec{x}') \times \hat{n}'}{ \vec{x} - \vec{x}' } \quad \text{Surface term}$ |
| $\Phi_M$<br>(only for $\vec{J} = 0$ ) | $\nabla^2 \Phi_M = 0$ <p>Solve Laplace eq'n with b.c.'s.</p>  | $\nabla^2 \Phi_M = \nabla \cdot \vec{M}$ $\Rightarrow \Phi_M(\vec{x}) = -\frac{1}{4\pi} \int_V d^3x' \frac{\nabla' \cdot \vec{M}(\vec{x}')}{ \vec{x} - \vec{x}' }$ $+ \frac{1}{4\pi} \int_S da' \frac{\hat{n}' \cdot \vec{M}(\vec{x}')}{ \vec{x} - \vec{x}' }$  |