

Recap of McLerran-Venugopalan (MV) model

- study of small- x gluon field in large nucleus.

long range

- + longitudinal coherent length of such gluons can be much longer than the size of nucleus

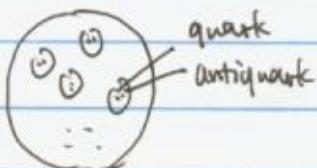
- momentum scale associated with small- x gluons

$$n^2 \sim 1/\alpha_{\text{exp}} A^{1/3} \gg \Lambda_{\text{QCD}}^2$$

↳ Classical field!

- large- x partons serve as classical source

How we calculated it:



i) source $\rho_{\text{cov}}(\vec{x}) = \sum_{a=1}^{N_c-1} \epsilon^a \rho_a^a(\vec{x})$

ii) Classical Yang-Mills equation $D_\mu F^{\mu\nu} = J^\nu$

solve for gluon field A_{cov}

iii) Gauge transformation $A^{\mu c} = S A^{\mu a} S^{-1} - \frac{i}{g} (\partial_\mu S) S^{-1}$

Result:

$$= \overline{E}_c = \overline{0} - \overline{0} = \overline{E}_c$$

minimum energy box

Alternative:

$$\rho_{lc} = S \rho_{uv} s^{-1}$$

→ continuous density approach

When calculating physical observables, one has to integrate over all charge densities with some weight function $W[\rho_{lc}]$. Valence quarks are independent, W has to be Gaussian.

$$W = \exp \left\{ - \int dx_2^z \int_{-\infty}^{\infty} dx^- \frac{\text{tr} [\rho_{lc}^2(x^-, x_2^z)]}{\mu^2(x^-, x_2^z)} \right\}.$$

$$\langle \hat{O}_p \rangle = \frac{\int D\rho_{lc} \hat{O}_p W[\rho_{lc}]}{\int D\rho_{lc} W[\rho_{lc}]}$$

Jalilian-Marian-Iancu - Melkman - Weigert - Leonidov - Kovner evolution equation.

- quantum corrections to the classical MV model.
- includes the small- x evolution in the wave function of the target.
- $W[\rho_{lc}] \rightarrow W_Y[\rho_{lc}]$
- Small- x evolution: $Y \rightarrow Y + dY$.
the gluons at Y become large- x gluons, and are incorporated into a source of classical fields.
- Color Glass Condensate (CGC)