

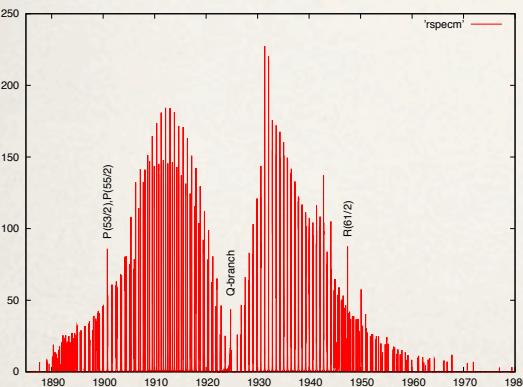
Composite Approaches for ab Initio Spectroscopy: **CCX (X=N, P, As, Sb) and HN₂O radicals**

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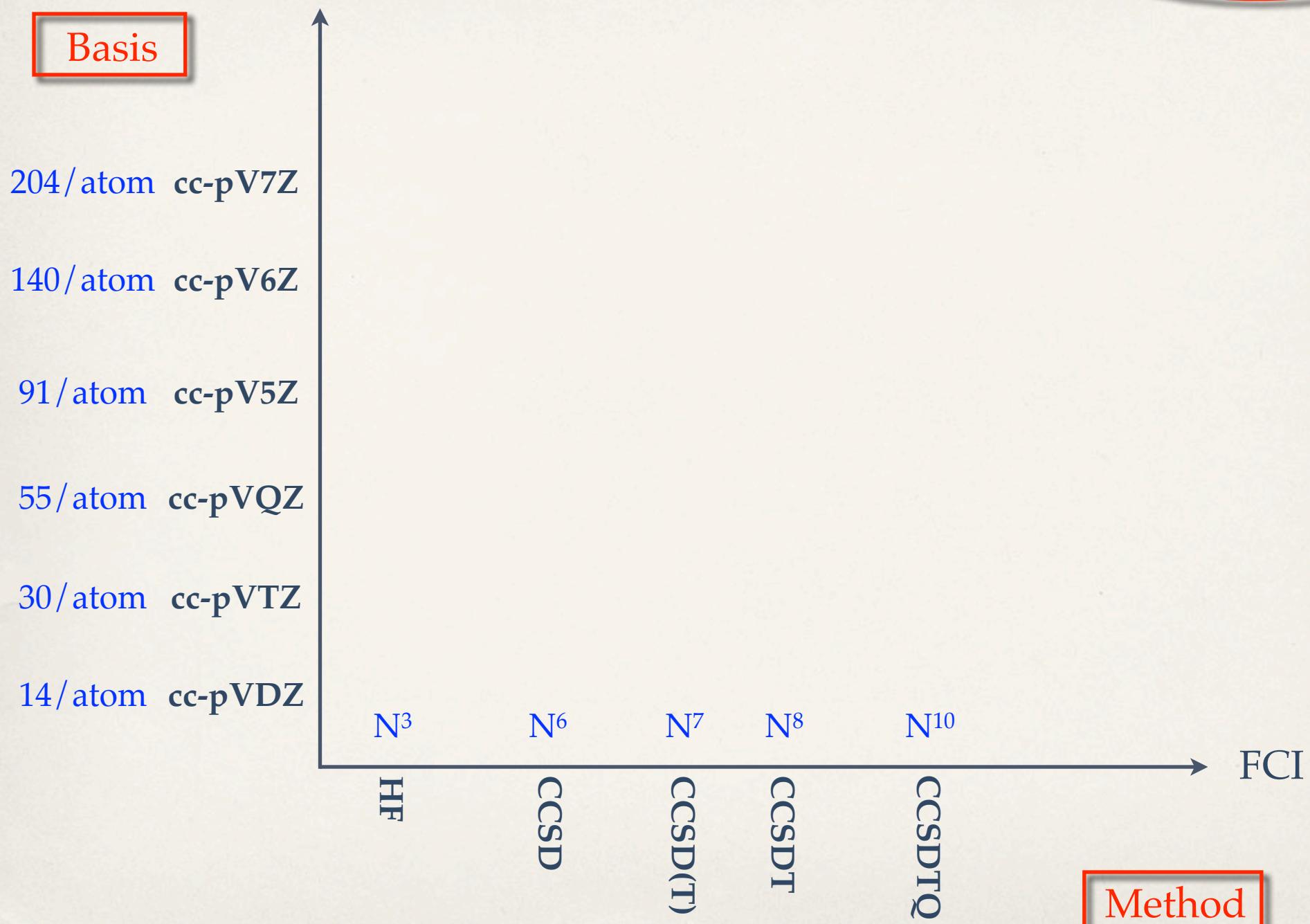
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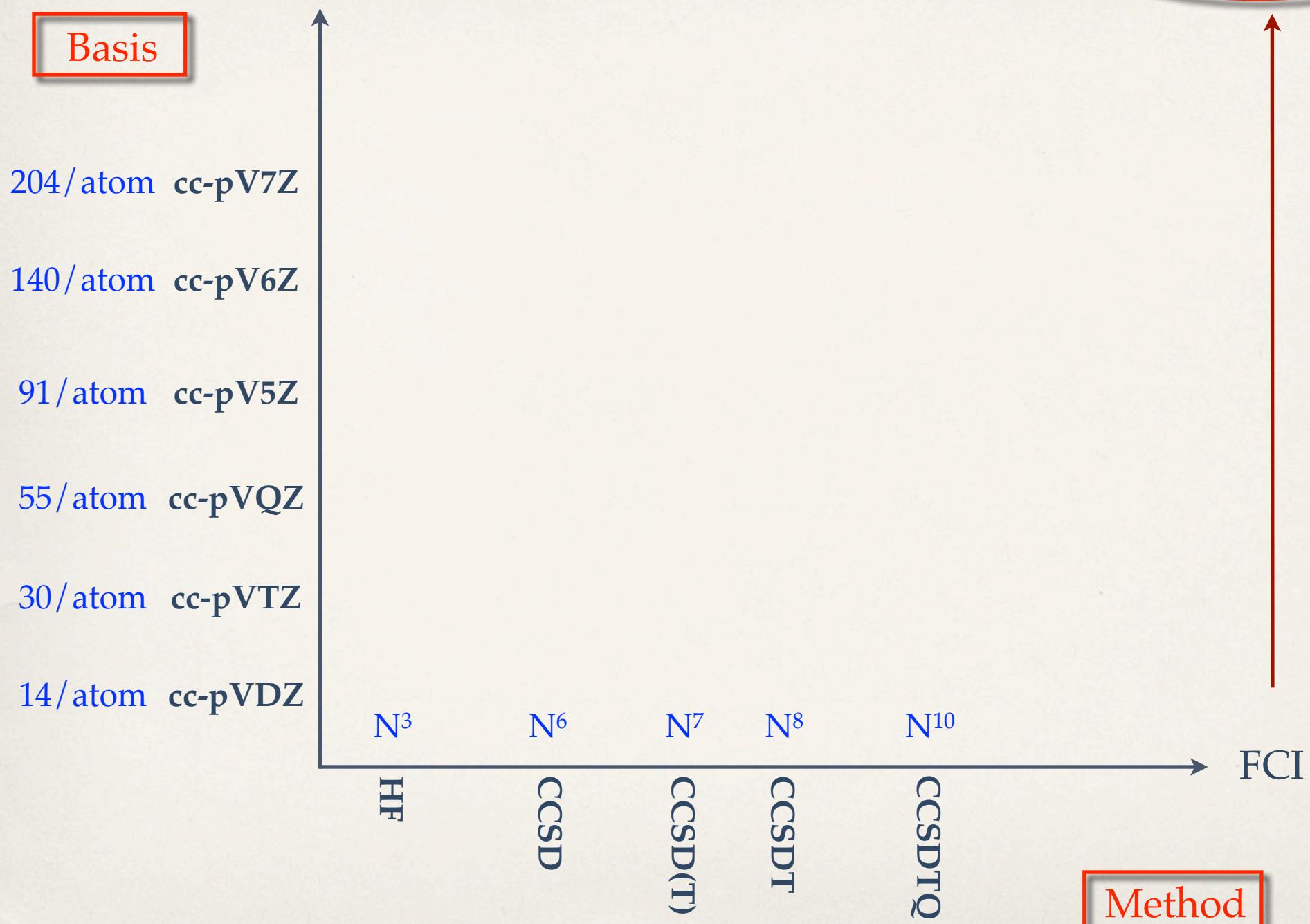
Complete basis set (CBS)

Exact, BO, non-rel
 $H\Psi = E\Psi$



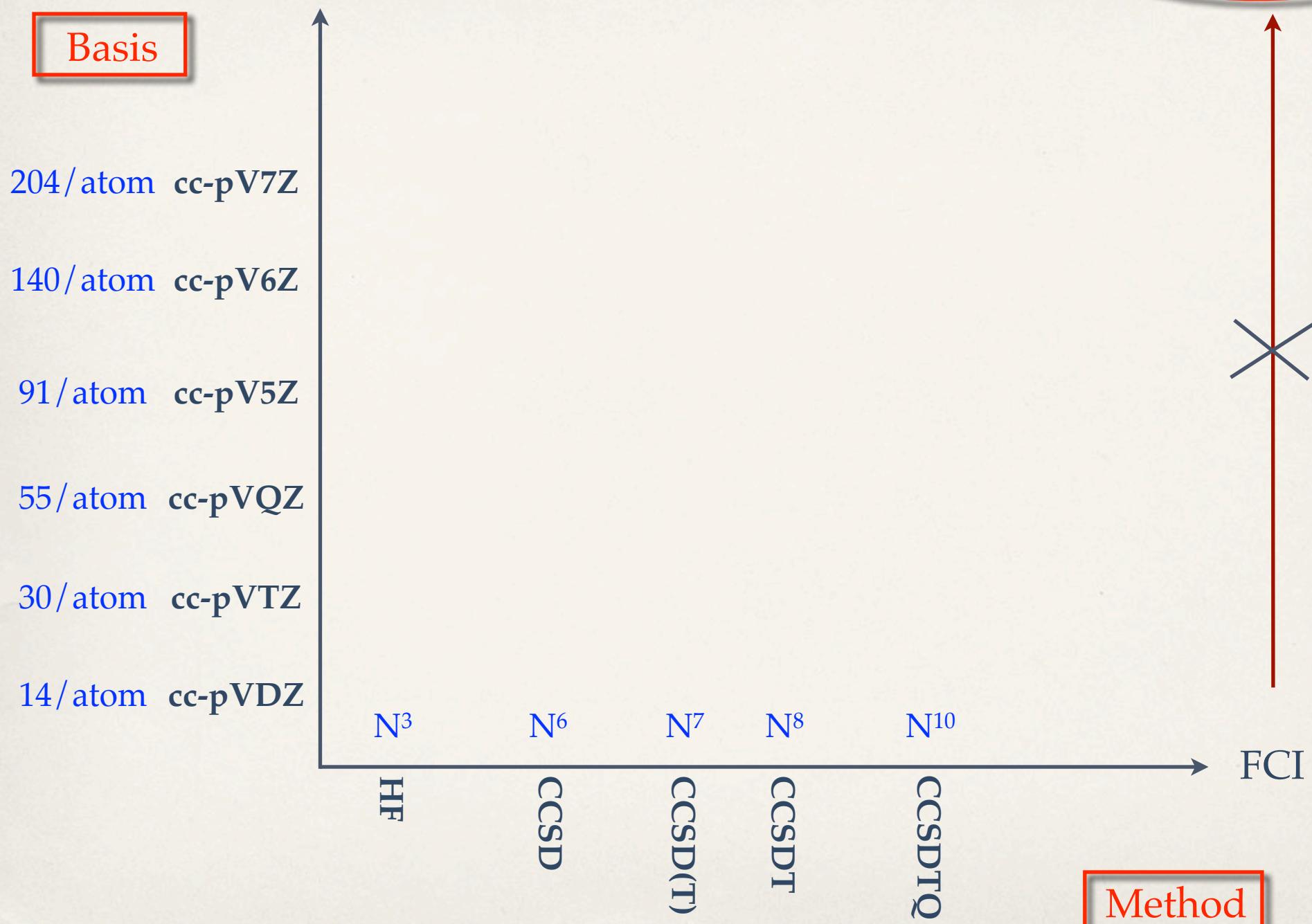
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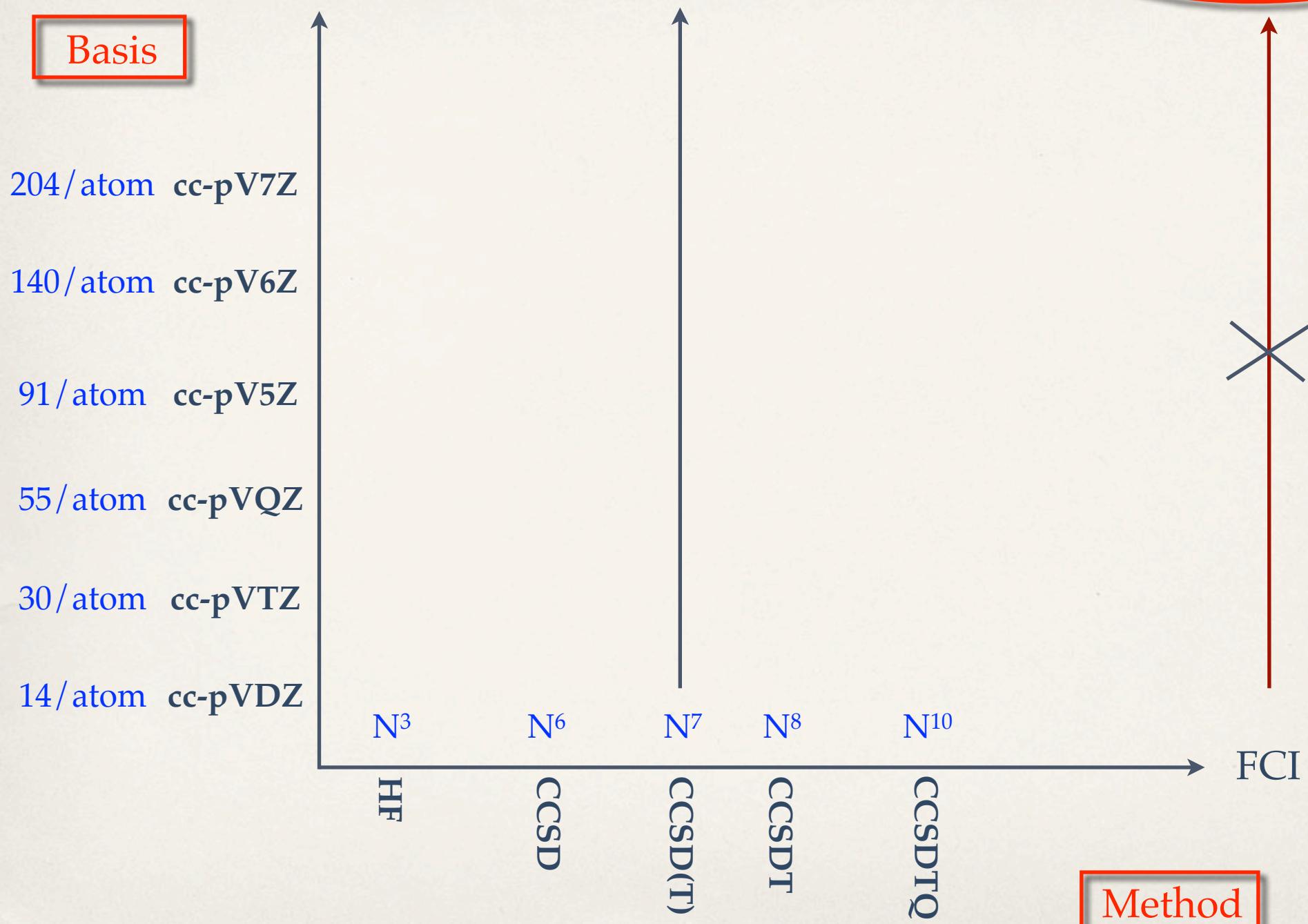
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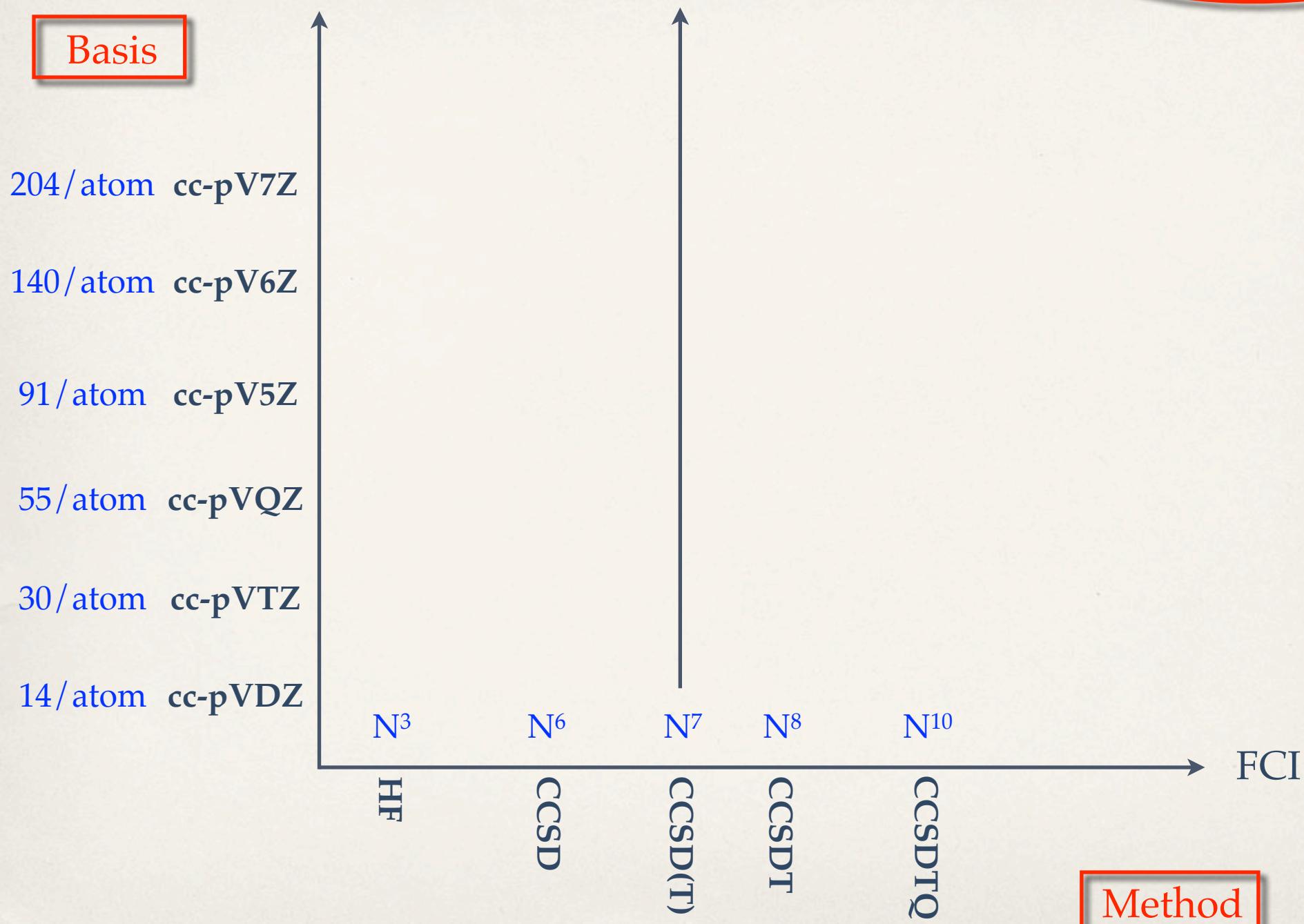
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Complete basis set (CBS)

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Methods for high accuracy work



Multireference configuration interaction, MRCI

$$\Psi_{CI} = \sum_{ref} \Phi_{ref} + \sum_i C_i^a \Phi_i^a + \sum_{ij} C_{ij}^{ab} \Phi_{ij}^{ab} + \dots$$

- Allows for correct dissociation of molecules, capable of very high accuracy, but can become intractable for large systems



Coupled cluster methods

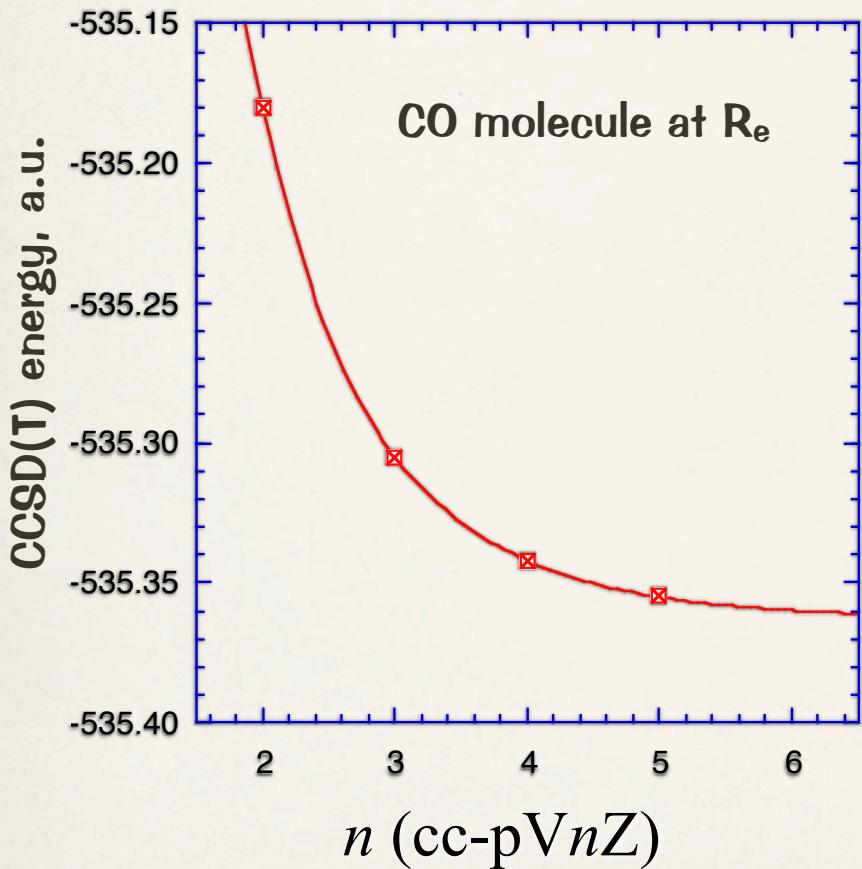
$$\Psi_{CC} = e^{\hat{T}} |0\rangle \text{ where } \hat{T} = \hat{T}_1 + \hat{T}_2 + \dots$$

where CCSD corresponds to a coupled cluster method with \hat{T} truncated at \hat{T}_2

- Provides a hierarchy of methods that converges to the exact solution within a given 1-particle basis set
 - Inherently based on a single determinant wave function (HF), so can not in general describe dissociation

Estimating the complete basis set limit

Systematic basis set convergence using correlation consistent basis sets allows for extrapolation of energies to the complete basis set (CBS) limit



Hartree-Fock:

$$E(n) = E_{\text{HF-limit}} + Ae^{-bn}$$

or

$$E(n) = E_{\text{HF-limit}} + A(n+1)e^{-9\sqrt{n}}$$

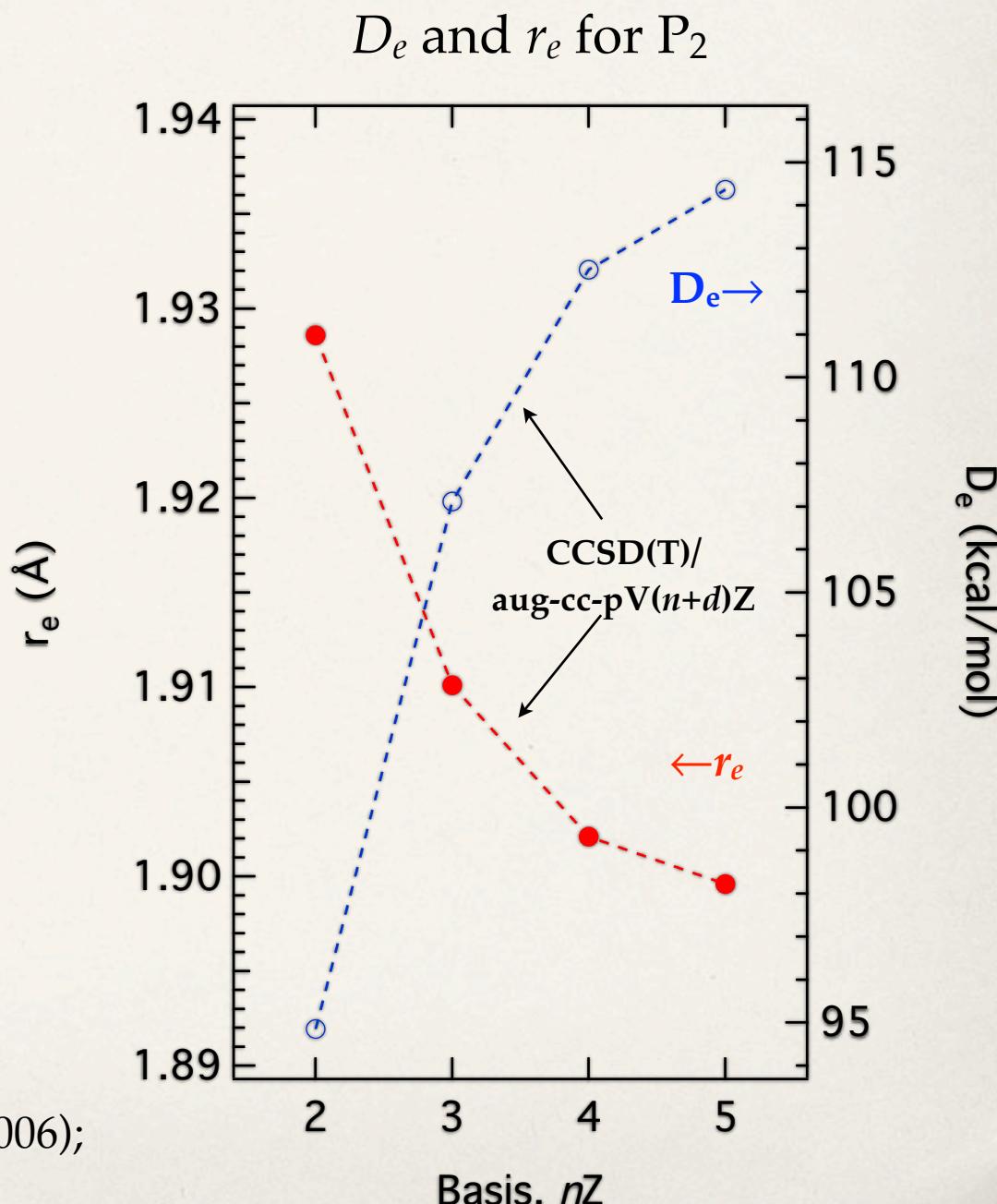
Correlation:

$$E(n) = E_{\text{CBS}} + \frac{a}{n^3}$$

The CBS limit represents the exact solution for the particular choice of method

Improving the basis set convergence rate

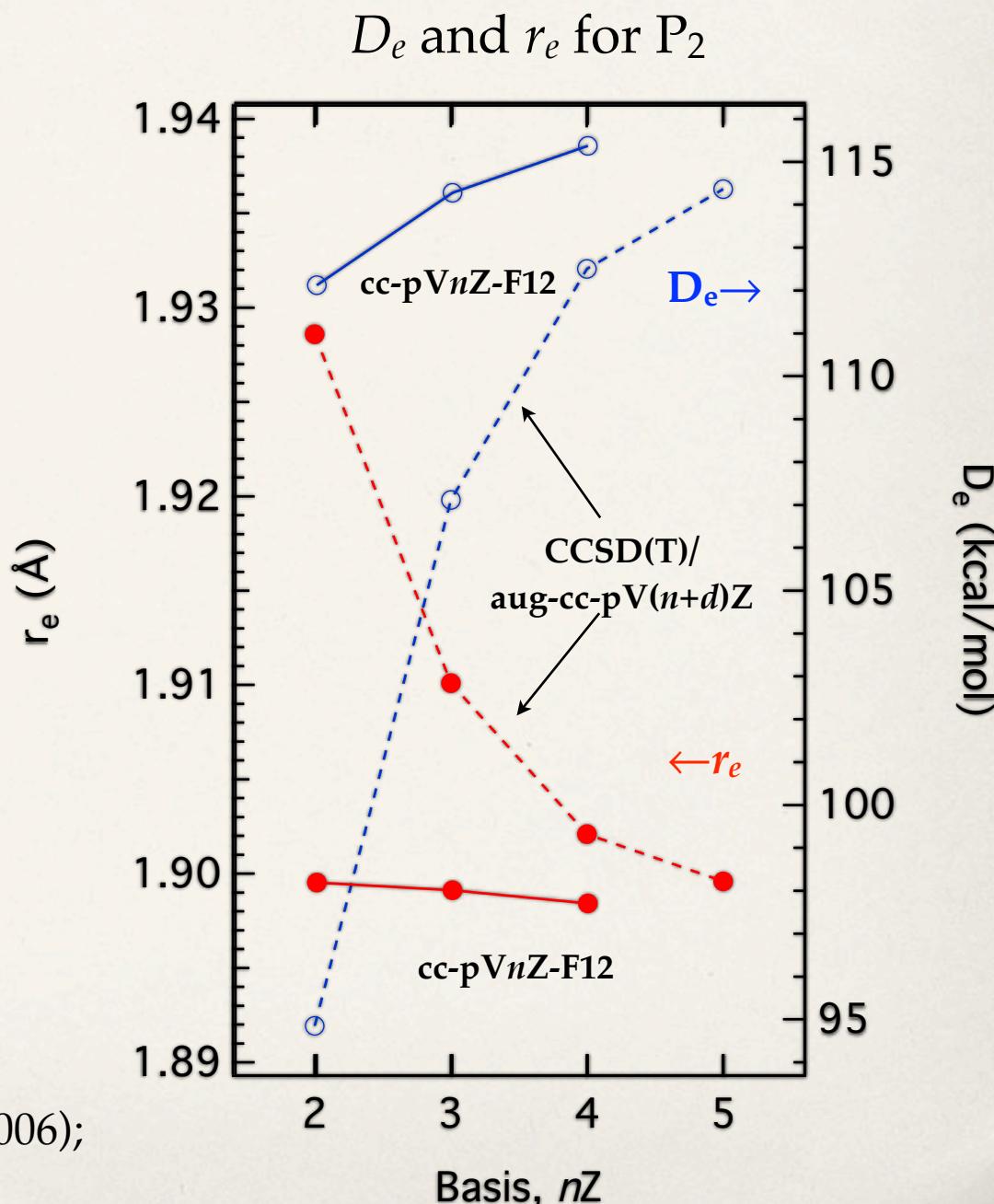
- Standard 1-particle basis sets yield very slow convergence due to a poor description of the 2-electron coalescence cusp
- Addition of a single function non-linear in r_{12} ($e^{-\gamma r_{12}}$), results in substantially better convergence. Referred to as F12 methods.
- Over the last few years our group has been developing basis sets optimal for use in F12 calculations, cc-pV n Z-F12



Klopper et al., Int. Rev. Phys. Chem. **25**, 427 (2006);
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Composite Methods

- ➊ Assume additivity:

$$E = E(\text{base})$$

- ➋ Base calculation: highly correlated method with large correlation consistent basis set, e.g., CCSD(T)/aug-cc-pV5Z

Composite Methods

- ➊ Assume additivity:

$$E = E(\text{base}) + \Delta \text{CBS}$$

- ➋ Base calculation: highly correlated method with large correlation consistent basis set, e.g., CCSD(T)/aug-cc-pV5Z
- ➌ Extrapolate to the CBS limit using energies from 2 consecutive basis sets

Composite Methods

- ➊ Assume additivity:

$$E = E(\text{base}) + \Delta\text{CBS} + \Delta\text{CV}$$

- ➋ Base calculation: highly correlated method with large correlation consistent basis set, e.g., CCSD(T)/aug-cc-pV5Z
- ➌ Extrapolate to the CBS limit using energies from 2 consecutive basis sets
- ➍ Add contributions due to electron correlation of outer core electrons

Goal: try to converge each contribution wrt to method and basis set

Composite Methods



Assume additivity:

$$E = E(\text{base}) + \Delta\text{CBS} + \Delta\text{CV} + \Delta\text{Rel}$$

- 📌 Base calculation: highly correlated method with large correlation consistent basis set, e.g., CCSD(T)/aug-cc-pV5Z
- 📌 Extrapolate to the CBS limit using energies from 2 consecutive basis sets
- 📌 Add contributions due to electron correlation of outer core electrons
- 📌 Add effects of scalar relativity on light atoms while including corrections for the pseudopotential approx. (if used)

Goal: try to converge each contribution wrt to method and basis set

Composite Methods

- ➊ Assume additivity:

$$E = E(\text{base}) + \Delta\text{CBS} + \Delta\text{CV} + \Delta\text{Rel} + \Delta\text{FCI}$$

- ➋ Base calculation: highly correlated method with large correlation consistent basis set, e.g., CCSD(T)/aug-cc-pV5Z
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- ➏ If possible, include correction for high-level electron correlation

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Composite Methods



Assume additivity:

$$E = E(\text{base}) + \Delta\text{CBS} + \Delta\text{CV} + \Delta\text{Rel} + \Delta\text{FCI} + \Delta\text{SO}$$

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Composite Methods



Assume additivity:

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- Base calculation: highly correlated method with large correlation consistent basis set, e.g., CCSD(T)/aug-cc-pV5Z
- Extrapolate to the CBS limit using energies from 2 consecutive basis sets
- Add contributions due to electron correlation of outer core electrons
- Add effects of scalar relativity on light atoms while including corrections for the pseudopotential approx. (if used)
- If possible, include correction for high-level electron correlation
- Add contributions due to spin-orbit coupling
- Add anything else that comes to mind!

Goal: try to converge each contribution wrt to method and basis set

Consider H₂O

- ➊ PES defined by 50 symmetry-unique points accurately fit to polynomials in displacement coordinates
- ➋ The following contributions were investigated:
 - ➌ extrapolations to the CCSD(T)/CBS limit (frozen-core and CV)
 - ➌ relativistic effects via Douglas-Kroll-Hess CCSD(T) calculations
 - ➌ higher-order correlation via CCSDT/CBS(TQ) and CCSDT(Q)/aVTZ
 - ◆ both FC and CV (the latter with cc-pwCVTZ and cc-pwCVDZ)
 - ➌ Born-Oppenheimer diagonal corrections (MRCI)
 - ➌ choice of masses (nuclear vs. atomic), Breit interaction, QED, etc.
- ❼ Fully anharmonic vibrational energies (for total J=0) were obtained via a variational approach using the full triatomic hamiltonian

Errors from experiment in cm^{-1}

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	$\nu_1 (a_1)$	$\nu_2 (a_1)$	$\nu_3 (b_1)$	(020)	(101)
CCSD(T)/aVQZ	-1.7	+1.8	-3.5	+4.2	-4.1
CCSD(T)/CBS	+2.4	+0.8	+1.8	+1.9	+5.4
Expt'l	3657.1	1594.8	3755.9	3151.6	7249.8

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$+\Delta\text{Rel}$	+6.6	+1.3	+6.4	+2.6	+13.9
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$+\Delta\text{FCI (FC)}$	-0.7	+0.7	-0.5	+1.5	-1.1
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+ $\Delta\text{FCI (FC)}$	-0.7	+0.7	-0.5	+1.5	-1.1
+ $\Delta\text{FCI (CV)}$	-1.0	+0.5	-0.9	+0.6	-2.0
Nuc. masses	-0.1	+0.9	+0.0	+1.4	-0.2
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+ΔFCI (CV)	-1.0	+0.5	-0.9	+0.6	-2.0
Nuc. masses	-0.1	+0.9	+0.0	+1.4	-0.2
+BODC	+0.3	+0.5	+0.6	+0.5	+0.9
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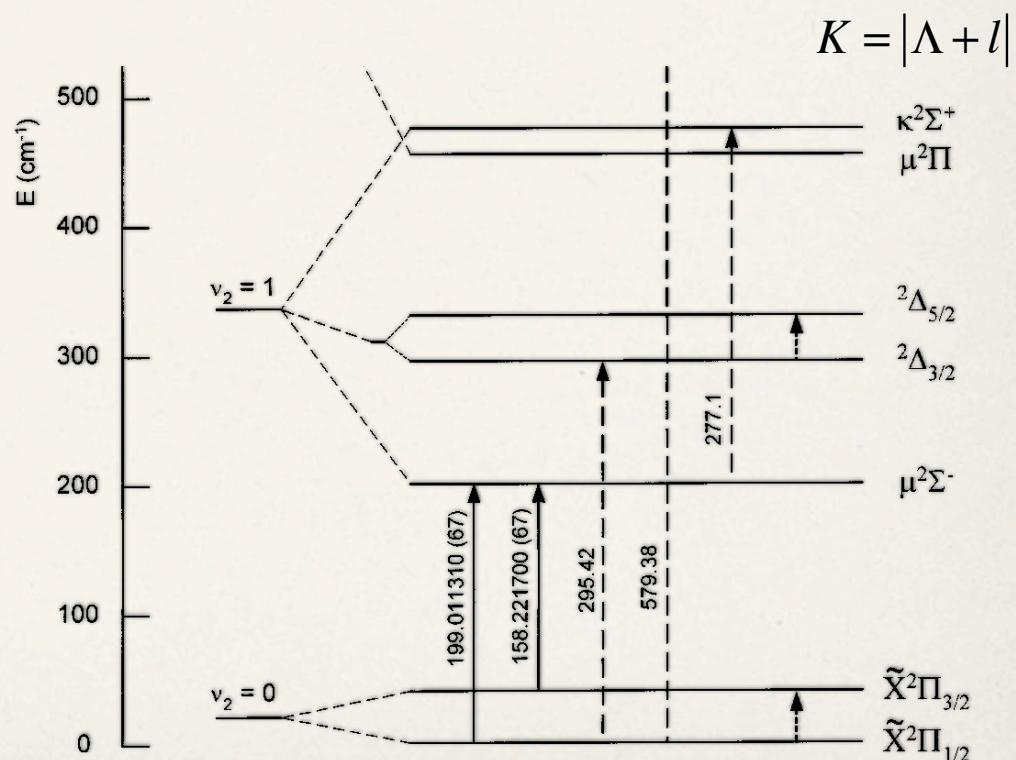
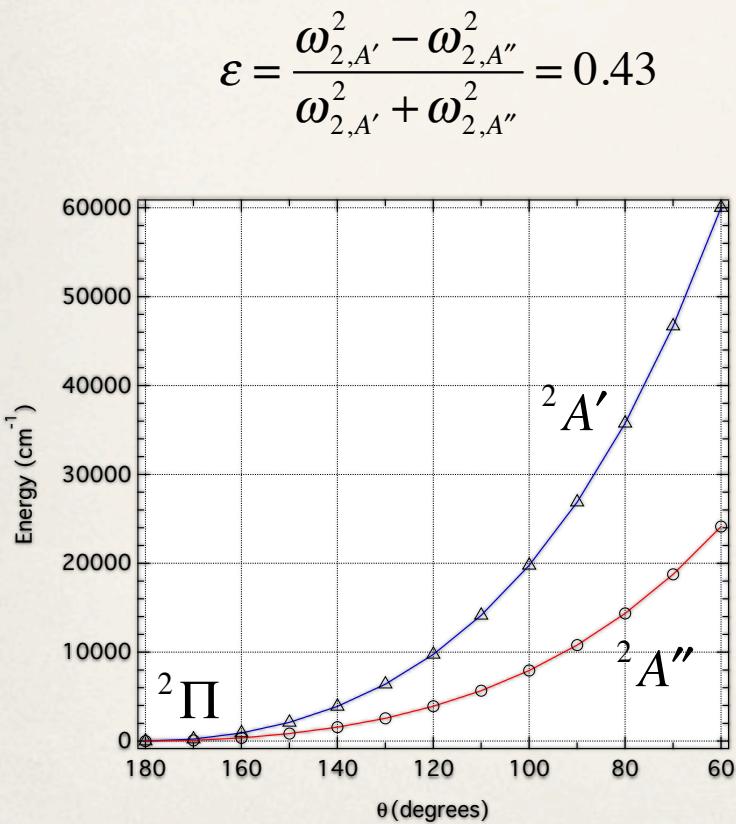
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+BODC	+0.3	+0.5	+0.6	+0.5	+0.9
+Breit,QED,etc.	-0.2	+0.4	+0.1	+0.3	-0.1
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Total	3656.9	1595.0	3756.1	3151.9	7249.7
Expt'l	3657.1	1594.8	3755.9	3151.6	7249.8

The X² Π CCN radical

- Should be important species in interstellar medium but not observed due to small permanent dipole moment
- Strong vibronic Renner-Teller effect on bending mode has motivated numerous spectroscopic investigations



Details of the PES Calculations for CCN

- PES defined by 50 symmetry-unique points for both RT components accurately fit to polynomials in displacement coordinates
- The following contributions were included:
 - CCSD(T)-F12b for both valence and CV with CBS extrapolations
 - relativistic effects via Douglas-Kroll-Hess CCSD(T) calculations
 - higher-order correlation via CAS-MRCI+Q/cc-pVTZ
- All of these calculations were also carried out for the excited $^4\Sigma^-$ state
- In addition the following were also calculated at each point on the PES:
 - Spin-orbit matrix elements at the CASSCF level
 - Permanent and transition dipole moments at CCSD(T) and CASSCF levels of theory, respectively (aug-cc-pVTZ)

Contributions to the Composite Surface: CCN

\AA and cm^{-1} ; average surface, $(A' + A'')/2$

2nd-order VPT

^a Expt: Gillett and Brown, Can. J. Phys. **72**, 1001 (1994); Oliphant et al., J. Chem. Phys. **92**, 2244 (1990)

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	$r_e(\text{CC})$	$r_e(\text{CN})$	$\nu_1 (\text{CN})$	$\nu_2 (\text{bend})$	$\nu_3 (\text{CC})$
VDZ-F12	1.382 5	1.185 7	1922.9	318.3	1033.6
+ΔVTZ-F12	-0.001 7	-0.000 8	+7.4	+1.6	+5.3

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+ΔCBS	-0.000 1	+0.000 0	+0.2	+0.4	+0.2

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+ΔRel	-0.000 2	-0.000 2	-0.8	-0.1	-0.5
+ΔFCI	-0.001 5	+0.002 9	-18.1	-3.4	+5.2
Total	1.374 9	1.184 7	1923.3	322.3	1050.4

^a Expt: Gillett and Brown, Can. J. Phys. **72**, 1001 (1994); Oliphant et al., J. Chem. Phys. **92**, 2244 (1990)

Contributions to the Composite Surface: CCN

Å and cm⁻¹; average surface, $(A' + A'')/2$

2nd-order VPT

	r_e (CC)	r_e (CN)	ν_1 (CN)	ν_2 (bend)	ν_3 (CC)
VDZ-F12	1.382 5	1.185 7	1922.9	318.3	1033.6
+ΔVTZ-F12	-0.001 7	-0.000 8	+7.4	+1.6	+5.3
+ΔVQZ-F12	-0.000 4	-0.000 3	+2.0	+0.8	+0.4
+ΔCBS	-0.000 1	+0.000 0	+0.2	+0.4	+0.2
+ΔCV	-0.003 8	-0.002 6	+9.7	+2.7	+6.4
+ΔRel	-0.000 2	-0.000 2	-0.8	-0.1	-0.5
+ΔFCI	-0.001 5	+0.002 9	-18.1	-3.4	+5.2
Total	1.374 9	1.184 7	1923.3	322.3	1050.4
Expt ^{1a}			1923.25		1050.76

^a Expt: Gillett and Brown, Can. J. Phys. **72**, 1001 (1994); Oliphant et al., J. Chem. Phys. **92**, 2244 (1990)

Full variational treatment of the ro-vibronic problem

- Fully anharmonic ro-vibronic energies and transition intensities were calculated variationally using the YART code of Mitrushchenkov in a 2-step procedure:
 - rotationless vibronic equation solved by 3-dim. diagonalization of $\hat{T}_K + V$ for $K \leq 20$. For $K > 0$ the coupled equations for the RT pairs were solved by diagonalizing:

$$\begin{pmatrix} \hat{T}_{|K-\Lambda|} + V_+ & V_- \\ V_- & \hat{T}_{|K+\Lambda|} + V_+ \end{pmatrix}$$

where $V_{\pm} = \frac{1}{2}(V_{A'} \pm V_{A''})$
 $K = |\Lambda + l| \quad ; \quad \Lambda = \pm 1$
 $l = \pm v_2, \pm(v_2 - 2), \dots, \pm 1 \text{ or } 0$

- the exact \hat{T}_K was employed, no contraction of the basis was used, and states 7000 cm^{-1} above the (000) of the $X^2\Pi$ and 4000 cm^{-1} above the $a^4\Sigma^-$ were included.
- resulting vibronic states were then used as a basis for the full ro-vibrational diagonalization including spin-orbit and rotation up to $J=155/2$.

Energy level structure of the ro-vibronic levels ($J=P, K=0-3$)

where

$$P = |K + \Sigma|$$

with

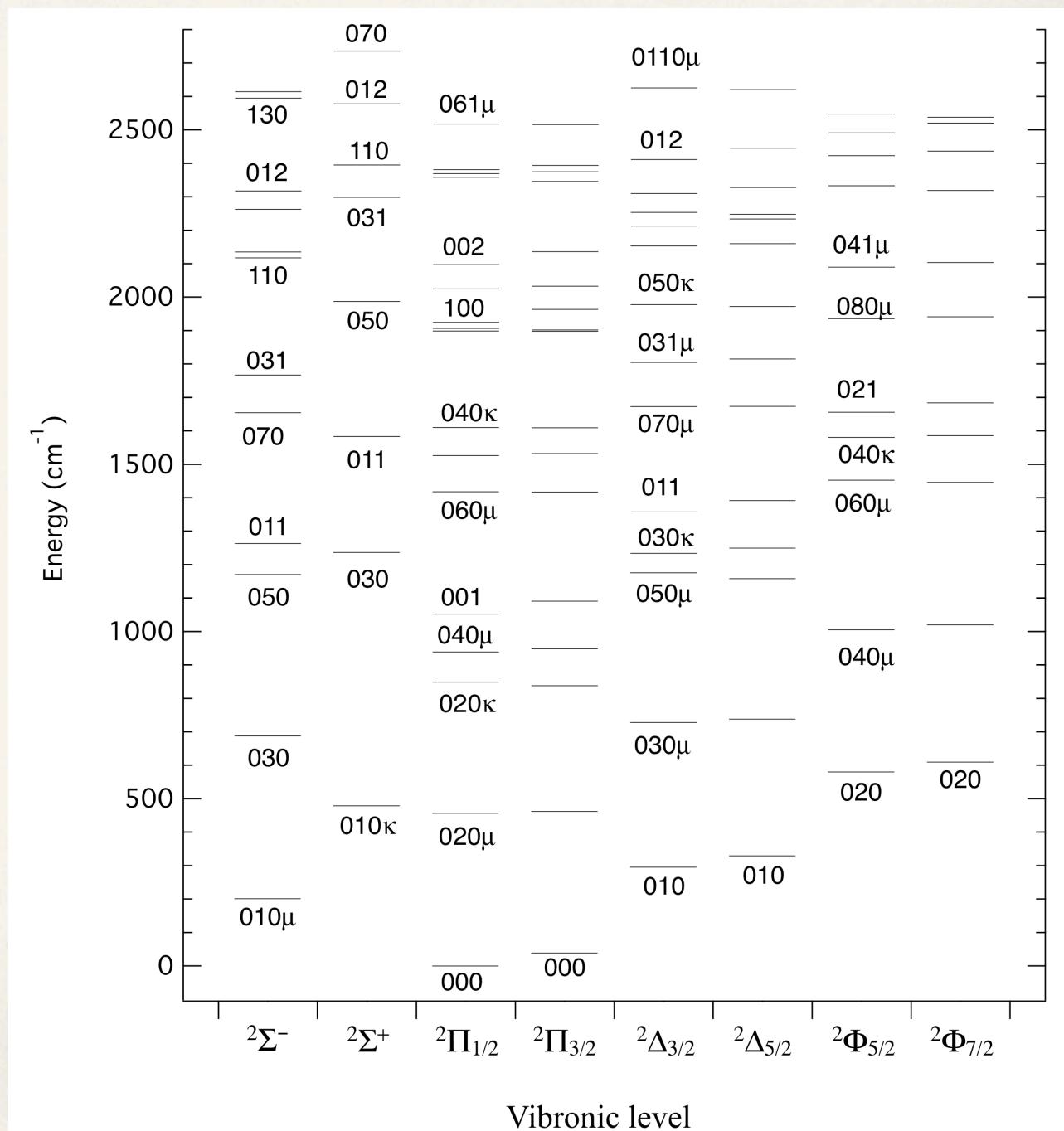
$$K = |\Lambda + l|$$

for a ${}^2\Pi$ state:

$$\Lambda = \pm 1$$

$$\Sigma = \pm \frac{1}{2}$$

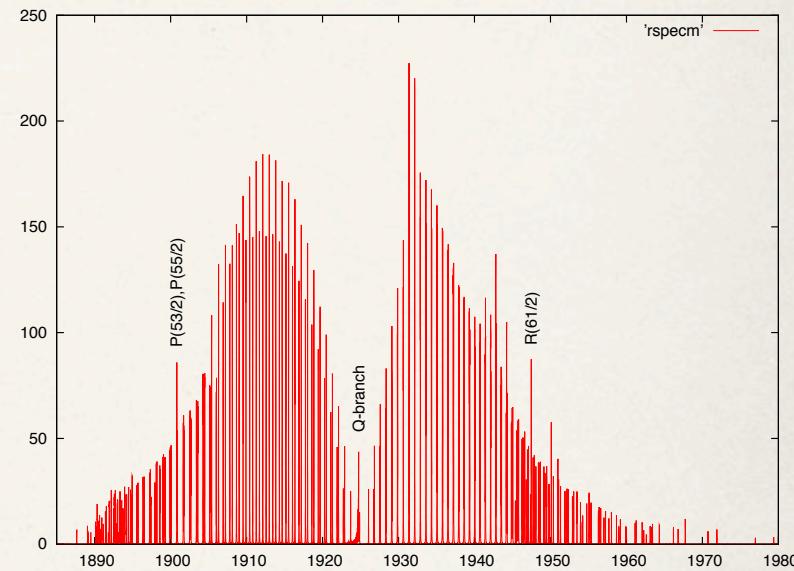
$$l = \pm v_2, \pm (v_2 - 2), \dots, \pm 1 \text{ or } 0$$



Selected Ro-vibronic Transition Energies for CCN

	Theory	Expt.
The (100) band		
(100) $^2\Pi_{1/2} \leftarrow (000) ^2\Pi_{1/2}; P(9/2)$	1921.29	1919.69
(100) $^2\Pi_{1/2} \leftarrow (000) ^2\Pi_{1/2}; R(5/2)$	1927.60	1925.99
(100) $^2\Pi_{3/2} \leftarrow (000) ^2\Pi_{3/2}; P(29/2)$	1912.56	1911.04
(100) $^2\Pi_{3/2} \leftarrow (000) ^2\Pi_{3/2}; R(9/2)$	1929.08	1927.55
The (010) band		
(010) $\mu ^2\Sigma^- \leftarrow (000) ^2\Pi_{1/2}; Q(1/2)$	200.99	199.06
(010) $\mu ^2\Sigma^- \leftarrow (000) ^2\Pi_{3/2}; P(3/2)$	162.09	158.28
(010) $\kappa ^2\Sigma^+ \leftarrow (010) \mu ^2\Sigma^-; Q(1/2)$	277.77	277.10
(010) $^2\Delta_{3/2} \leftarrow (000) ^2\Pi_{1/2}; R(1/2)$	295.26	295.42
(020) $^2\Phi_{5/2} \leftarrow (000) ^2\Pi_{1/2}; S(1/2)$	580.31	579.38
Spin-orbit transitions		
(000) $^2\Pi_{3/2} \leftarrow (000) ^2\Pi_{1/2}; P(7/2)$	35.00	36.89
(000) $^2\Pi_{3/2} \leftarrow (000) ^2\Pi_{1/2}; Q(3/2)$	37.72	39.60
(000) $^2\Pi_{3/2} \leftarrow (000) ^2\Pi_{1/2}; R(19/2)$	46.97	48.82
The $1_0^1 2_1^1$ hot band		
(110) $\mu ^2\Sigma^- \leftarrow (010) \mu ^2\Sigma^-; P(7), F_1$	1913.4571	1911.3882
(110) $^2\Delta \leftarrow (010) ^2\Delta; R(17/2), F_1$	1924.8741	1922.9424

Theoretical (100) band at 300 K



Experiment

(100): Gillett and Brown, Can. J. Phys. **72**, 1001 (1994)

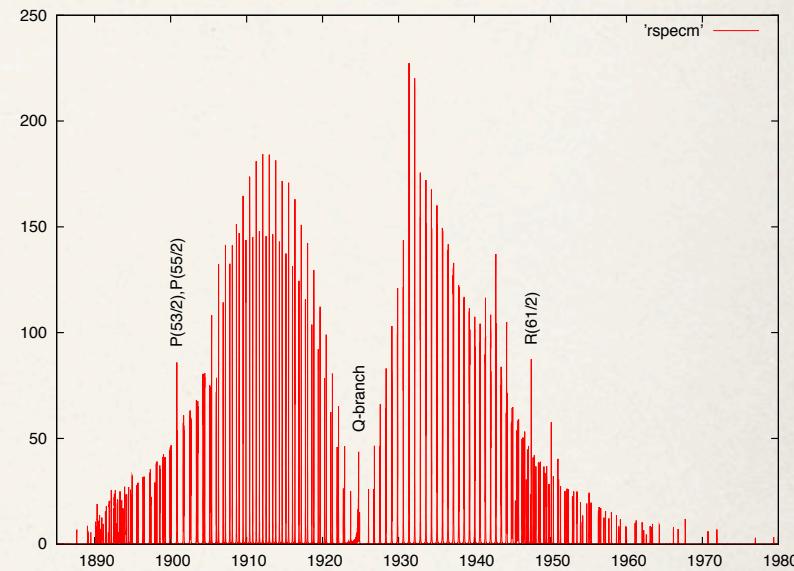
(010) & SO: Allen et al., J. Mol. Spectrosc. **201**, 17 (2000).

Hot band: Beaton et al., J. Mol. Spectrosc. **209**, 60 (2001)

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Theoretical (100) band at 300 K



Experiment

(100): Gillett and Brown, Can. J. Phys. **72**, 1001 (1994)

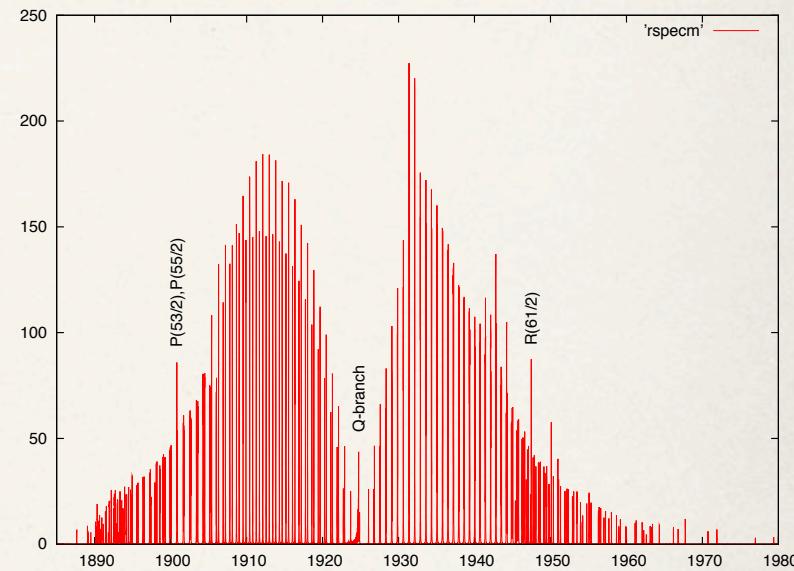
(010) & SO: Allen et al., J. Mol. Spectrosc. **201**, 17 (2000).

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Theoretical (100) band at 300 K



Experiment

(100): Gillett and Brown, Can. J. Phys. **72**, 1001 (1994)

(010) & SO: Allen et al., J. Mol. Spectrosc. **201**, 17 (2000).

Hot band: Beaton et al., J. Mol. Spectrosc. **209**, 60 (2001)

The X² Π CCP radical: Preliminary Results

- Jet-cooled LIF spectrum of C₂P reported by Clouthier and co-workers
 - Assigned ground state vibrational frequencies and Renner-Teller effect
- High resolution microwave spectrum reported by Ziurys, Clouthier, and co-workers
 - Yielded r_0 , r_s , and $r_m^{(1)}$ structures
- Detected in the circumstellar envelope of IRC+10216
- All calculations of this work mostly analogous to those of CCN
 - •C-C-P resonance structure causes problems for ROHF (same for CCAs)
 - Use full-valence CASSCF orbitals in the CCSD(T) calculations
 - Full variational calculations are currently just underway

F.X. Sunahori, J. Wei, & D.J. Clouthier, *J. Chem. Phys.* 128, 4311 (2008)

D.T. Halfen, M. Sun, D.J. Clouthier, & L.M. Ziurys, *J. Chem. Phys.* 130, 014305 (2009);

D.T. Halfen, D.J. Clouthier, & L.M. Ziurys, *Astrophys. J. Lett.* 677 L101 (2008).

Contributions to the Composite Surface: CCP

\AA and cm^{-1} ; average surface, $(A' + A'')/2$

2nd-order VPT

	$r_e(\text{CC})$	$r_e(\text{CP})$	$\nu_1 (\text{CC})$	$\nu_2 (\text{bend})$	$\nu_3 (\text{CP})$
VTZ-F12	1.310 5	1.613 2	1671.5	205.2	833.1
+ΔVQZ-F12	-0.000 3	-0.000 5	+1.3	+2.8	+0.6
+ΔCBS	+0.000 0	-0.000 1	+0.3	+0.6	+0.0
+ΔCV	-0.003 7	-0.005 1	+9.1	+0.6	+5.7
+ΔRel	-0.000 2	-0.000 2	-1.0	-0.5	-0.9
+ΔFCI	+0.001 6	+0.001 9	-10.8	-0.3	-7.0
Total	1.307 9	1.609 2	1670.4	208.4	831.5
Expt'l^a	1.289	1.621	1644.3		834.8

$B_0 = 6361 \text{ MHz}$ vs. expt'l value of 6392.41 MHz

$B_e = 6354 \text{ MHz}$ vs. approx. expt'l value of 6366 MHz

^a $r_m^{(1)}$ structure

Contributions to the Composite Surface: CCP

\AA and cm^{-1} ; average surface, $(A' + A'')/2$

2nd-order VPT

	$r_e(\text{CC})$	$r_e(\text{CP})$	$\nu_1 (\text{CC})$	$\nu_2 (\text{bend})$	$\nu_3 (\text{CP})$	(002)
VTZ-F12	1.310 5	1.613 2	1671.5	205.2	833.1	1654.7
+ΔVQZ-F12	-0.000 3	-0.000 5	+1.3	+2.8	+0.6	+1.3
+ΔCBS	+0.000 0	-0.000 1	+0.3	+0.6	+0.0	+0.1
+ΔCV	-0.003 7	-0.005 1	+9.1	+0.6	+5.7	+10.8
+ΔRel	-0.000 2	-0.000 2	-1.0	-0.5	-0.9	-1.7
+ΔFCI	+0.001 6	+0.001 9	-10.8	-0.3	-7.0	-13.7
Total	1.307 9	1.609 2	1670.4	208.4	831.5	1651.5
Expt'l^a	1.289	1.621	1644.3		834.8	1677.7

$B_0 = 6361 \text{ MHz}$ vs. expt'l value of 6392.41 MHz

$B_e = 6354 \text{ MHz}$ vs. approx. expt'l value of 6366 MHz

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\AA and cm^{-1} ; average surface, $(A' + A'')/2$

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$+\Delta\text{Rel}$	-0.000 2	-0.000 2	-1.0	-0.5	-0.9	-1.7
$+\Delta\text{FCI}$	+0.001 6	+0.001 9	-10.8	-0.3	-7.0	-13.7
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^a $r_m^{(1)}$ structure

The X² Π CCAs and CCSb radicals: Preliminary Results

- Jet-cooled LIF spectrum of C₂As reported by Clouthier and co-workers
- Assigned ground state vibrational frequencies and Renner-Teller effect
- Spin-orbit coupling now large enough to nearly overwhelm the RT interaction
- For these calculations, relativistic effects must now be included at the outset
 - Choose relativistic effective core potentials on As and Sb with new cc-pVnZ-F12-PP basis sets in F12 calculations
 - Use DKH calculations to account for the small pseudopotential errors and account for scalar relativistic effects from the carbon atoms
- For both C₂As and C₂Sb low-lying cyclic minima exist on the PES
 - after including spin-orbit, these lie above the linear configuration by 4.5 kcal/mol for C₂As and 1.0 kcal/mol for C₂Sb

Contributions to the Composite Surface: CCAs

Å and cm⁻¹; average surface, $(A' + A'')/2$

2nd-order VPT

	r_e (CC)	r_e (CAs)	ν_1 (CC)	ν_2 (bend)	ν_3 (CAs)
VTZ-F12	1.302 7	1.741 5	1690.1	153.4	659.5
+ΔVQZ-F12	-0.000 3	-0.000 6	+0.8	+2.9	+0.9
+ΔCBS	-0.000 0	-0.000 1	+0.0	+2.0	+0.3

Expt'l ^a			1691.7		661.0
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^a Wei et al., J. Chem. Phys. **129**, 4307 (2008). Data from the $\Omega=1/2$ state was used.

Contributions to the Composite Surface: CCAs

\AA and cm^{-1} ; average surface, $(A' + A'')/2$

2nd-order VPT

	$r_e(\text{CC})$	$r_e(\text{CAs})$	$\nu_1 (\text{CC})$	$\nu_2 (\text{bend})$	$\nu_3 (\text{CAs})$
VTZ-F12	1.302 7	1.741 5	1690.1	153.4	659.5
+ Δ VQZ-F12	-0.000 3	-0.000 6	+0.8	+2.9	+0.9
+ Δ CBS	-0.000 0	-0.000 1	+0.0	+2.0	+0.3
+ Δ CV	-0.004 5	-0.009 7	+9.6	-11.4	+2.3

Expt'l ^a			1691.7		661.0
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Contributions to the Composite Surface: CCAs

\AA and cm^{-1} ; average surface, $(A' + A'')/2$

2nd-order VPT

	$r_e(\text{CC})$	$r_e(\text{CAs})$	$\nu_1 (\text{CC})$	$\nu_2 (\text{bend})$	$\nu_3 (\text{CAs})$
VTZ-F12	1.302 7	1.741 5	1690.1	153.4	659.5
+ Δ VQZ-F12	-0.000 3	-0.000 6	+0.8	+2.9	+0.9
+ Δ CBS	-0.000 0	-0.000 1	+0.0	+2.0	+0.3
+ Δ CV	-0.004 5	-0.009 7	+9.6	-11.4	+2.3
+ Δ Rel	-0.000 1	+0.000 8	-0.5	+2.9	-1.7

Expt'l ^a			1691.7		661.0
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Contributions to the Composite Surface: CCAs

\AA and cm^{-1} ; average surface, $(A' + A'')/2$

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VTZ-F12	1.302 7	1.741 5	1690.1	153.4	659.5
+ Δ VQZ-F12	-0.000 3	-0.000 6	+0.8	+2.9	+0.9
+ Δ CBS	-0.000 0	-0.000 1	+0.0	+2.0	+0.3
+ Δ CV	-0.004 5	-0.009 7	+9.6	-11.4	+2.3
+ Δ Rel	-0.000 1	+0.000 8	-0.5	+2.9	-1.7
+ Δ FCI	+0.001 5	+0.001 6	-13.9	+0.5	-3.7

Expt'l ^a			1691.7		661.0
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^a Wei et al., J. Chem. Phys. **129**, 4307 (2008). Data from the $\Omega=1/2$ state was used.

Contributions to the Composite Surface: CCAs

\AA and cm^{-1} ; average surface, $(A' + A'')/2$

2nd-order VPT

	$r_e(\text{CC})$	$r_e(\text{CAs})$	$\nu_1 (\text{CC})$	$\nu_2 (\text{bend})$	$\nu_3 (\text{CAs})$
VTZ-F12	1.302 7	1.741 5	1690.1	153.4	659.5
+ Δ VQZ-F12	-0.000 3	-0.000 6	+0.8	+2.9	+0.9
+ Δ CBS	-0.000 0	-0.000 1	+0.0	+2.0	+0.3
+ Δ CV	-0.004 5	-0.009 7	+9.6	-11.4	+2.3
+ Δ Rel	-0.000 1	+0.000 8	-0.5	+2.9	-1.7
+ Δ FCI	+0.001 5	+0.001 6	-13.9	+0.5	-3.7
Total	1.2993	1.7335	1686.1	150.3	657.6
Expt'l ^a			1691.7		661.0

^a Wei et al., J. Chem. Phys. **129**, 4307 (2008). Data from the $\Omega=1/2$ state was used.

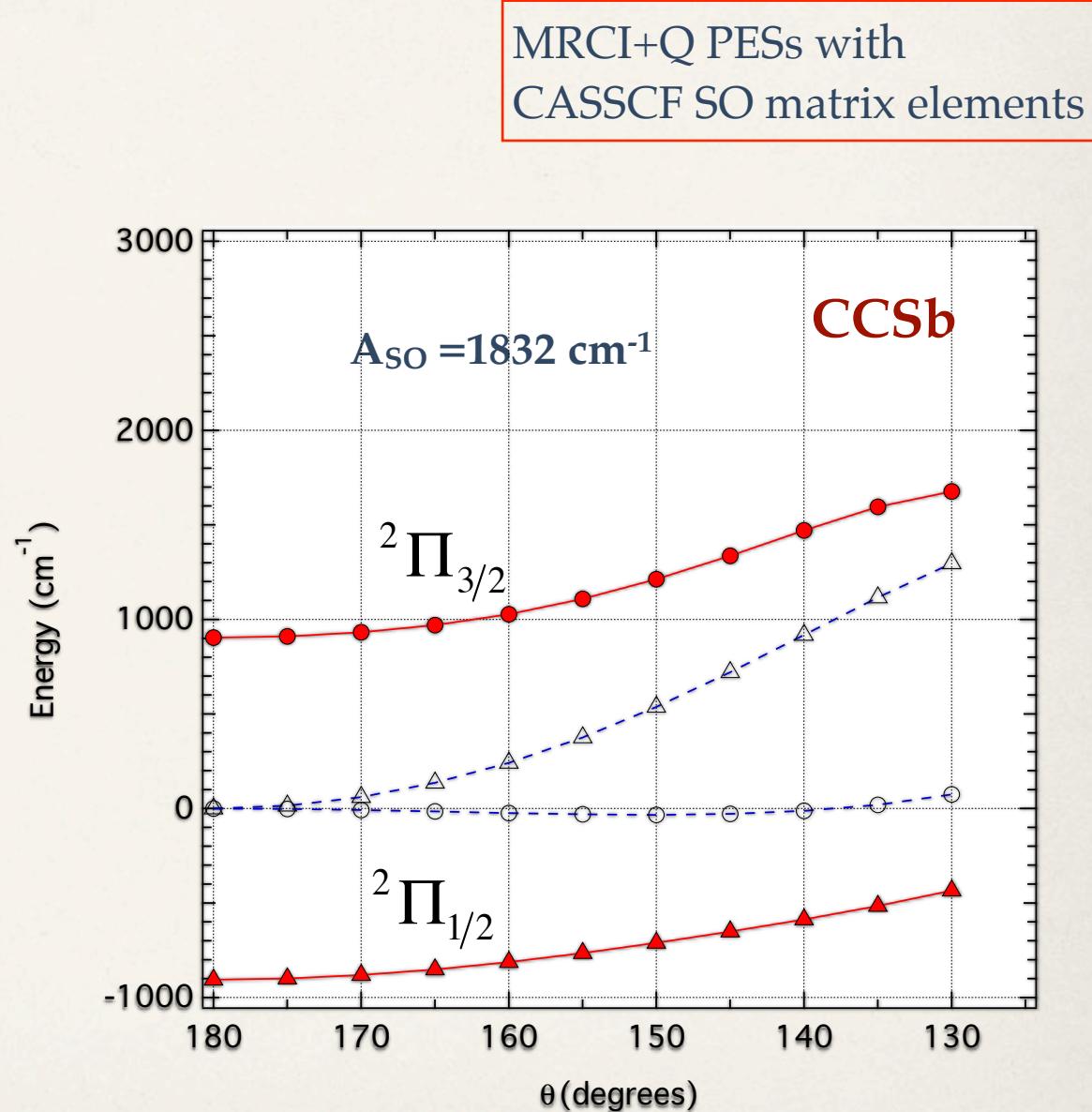
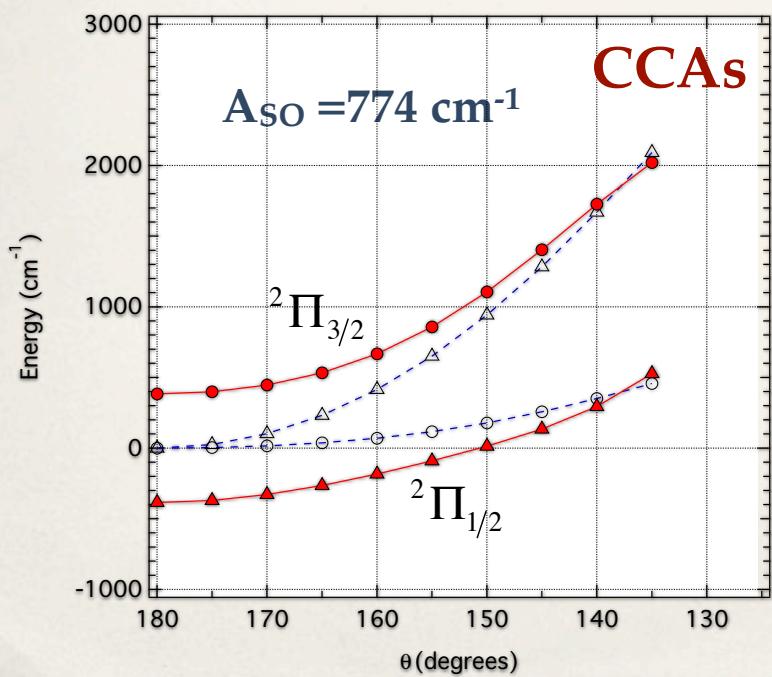
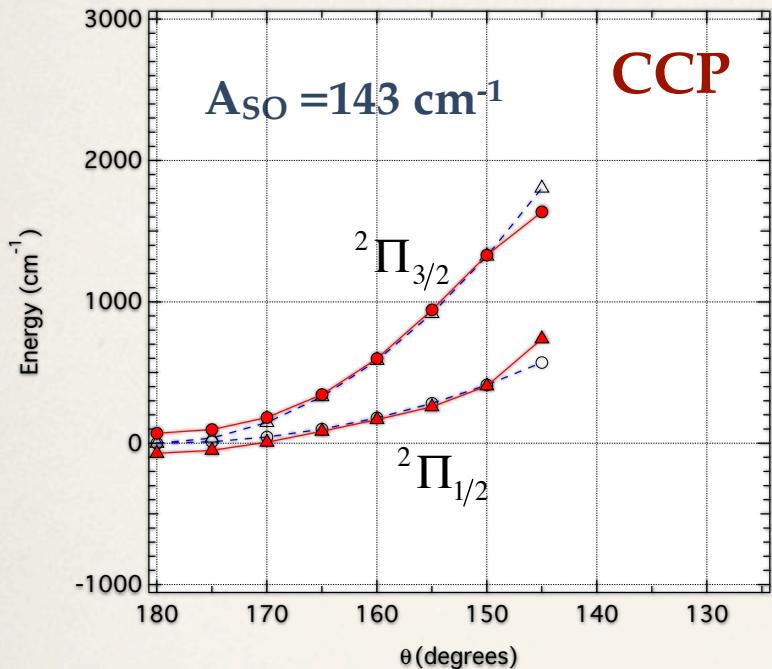
Contributions to the Composite Surface: CCSb

\AA and cm^{-1} ; average surface, $(A' + A'')/2$

2nd-order VPT

	$r_e(\text{CC})$	$r_e(\text{CSb})$	$\nu_1 (\text{CC})$	$\nu_2 (\text{bend})$	$\nu_3 (\text{CSb})$
VTZ-F12	1.293 3	1.953 3	1742.6	98.5	566.0
+ Δ VQZ-F12	-0.000 3	-0.000 8	+1.4	+2.8	+0.6
+ Δ CBS	+0.000 1	-0.000 1	+0.0	+1.6	-0.1
+ Δ CV	-0.002 3	-0.021 4	+2.5	+8.5	+7.8
+ Δ Rel	+0.000 4	+0.000 2	+1.7	+2.8	-0.7
+ Δ FCI	+0.002 4	+0.000 8	-13.2	+2.7	-8.8
Total	1.293 5	1.932 1	1735.0	116.9	564.8

Impact of Spin-Orbit on Bending Potentials



Moving from N to Sb

Å and cm⁻¹

	r_{CC}	r_{CX}	$\omega(CC)$	ω_2	$\omega(CX)$	$\mu(D)$
CCN	1.375	1.185	1058	322	1967	0.30
CCP	1.308	1.609	1700	217	830	3.11
CCAs	1.299	1.734	1720	108	652	3.87
CCSb	1.294	1.932	1766	117	556	5.01

Spectroscopic Properties of the X²A' HN₂O Radical

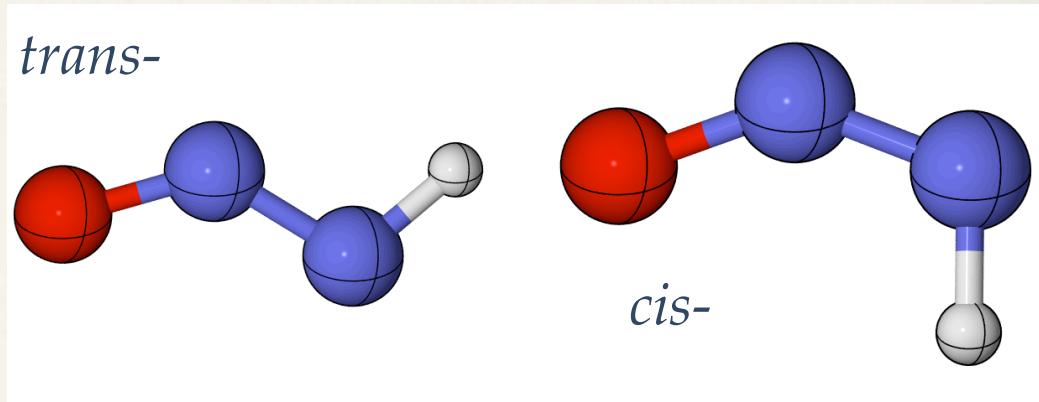
Proposed to be important in the planetary atmosphere of Saturn's rings; formed by reaction of NH with NO.

trans- isomer lower than *cis*- by 6.9 kcal/mol

Composite approach:

CCSD(T)/CBS +ΔCV + ΔDK
+ΔCCSDT + ΔCCSDT(Q)

Large contribution from (Q)



<i>trans</i> -	ΔT	Δ(Q)	Theory	Matrix IR
v₁	+30.2	-49.6	3286.9	3254.0
v₂	-20.4	-37.1	1629.6	1628.9
v₃	+8.1	-69.5	1279.0	1294.5
v₄	-5.1	-66.2	1172.1	1213.4
v₅	0.0	-34.4	638.7	---
v₆	-16.7	-13.5	740.4	746.5

Acknowledgments

- Dr. Kazim Yousaf (WSU)
- Dr. Gerald Knizia and Prof. Hans-Joachim Werner (Uni. Stuttgart)

- Most CCSD(T) and all F12 calculations were carried out with the MOLPRO suite of ab initio programs (v2010.1).
- The CFOUR program was used for the CCSD(T) frequencies of HNNO.
- The MRCC program was used for all higher order coupled cluster calculations

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