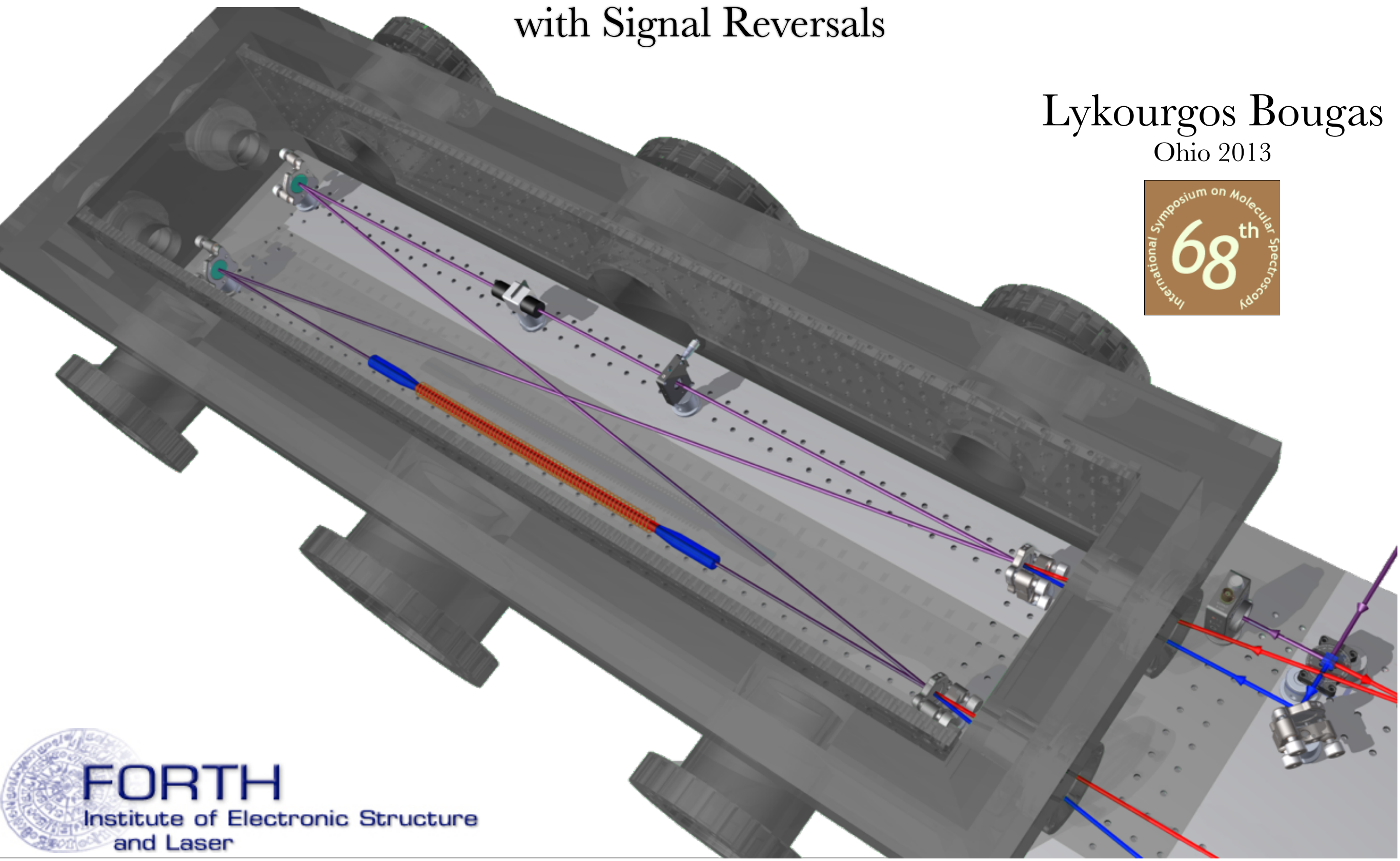


Chiral Cavity Ring-Down

Absolute Measurements of Optical Rotation in Gases and Liquids
with Signal Reversals

Lykourgos Bougas
Ohio 2013



How to enhance circular birefringence?

PNC optical rotation & natural optical activity

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PNC optical rotation & natural optical activity



10^{-9} - 10^{-5} rad/pass

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$$\phi \equiv (\text{specific rotation}) \times \rho \times l$$



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density or path length

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Optical Cavities

Enhancement factor $\propto N \approx 2\mathcal{F}/\pi$

($R=99.99\% \rightarrow N \sim 10^4$)

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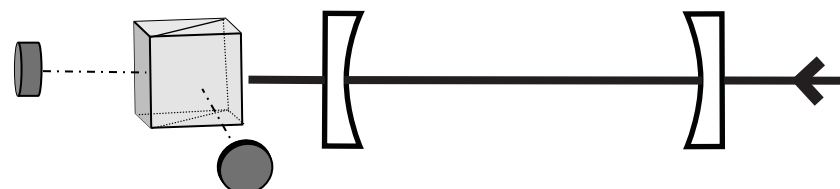


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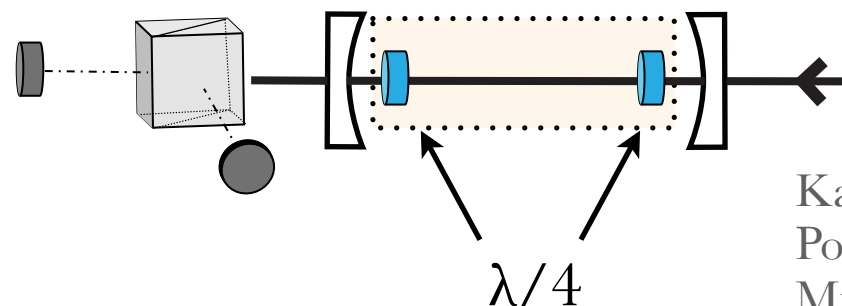


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YES

Kastler (1970)
Poirson et. al. (1998)
Muller et. al. (2002)

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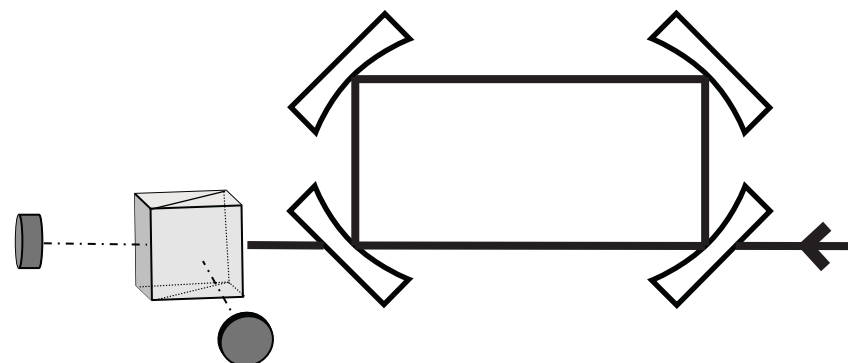


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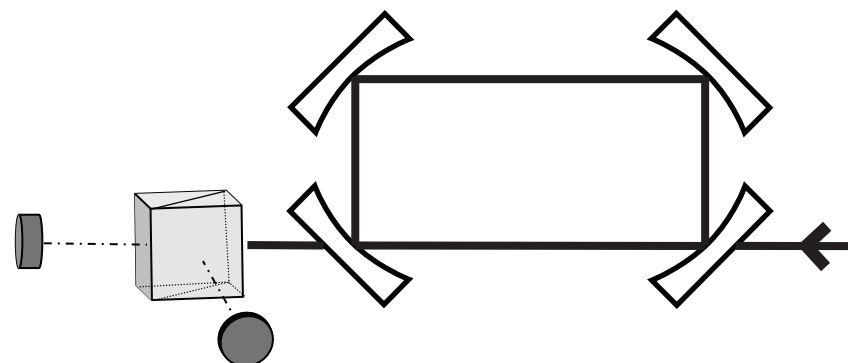


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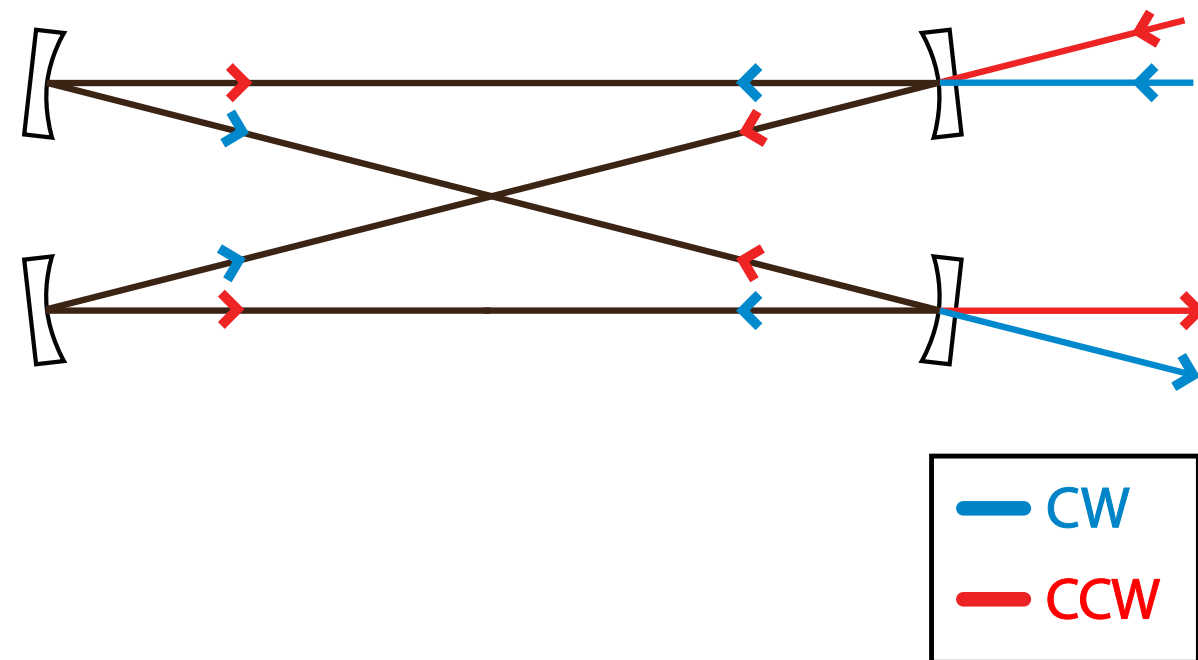


Disadvantages:

- mechanical adjustments
- measurements of CB only
- large linear birefringence
- intracavity optics

4-mirror bowtie cavity

- supports counter-propagating beams
- simultaneous measure effects of different symmetry under P & T
- $\delta/\text{reflection} < 1\text{mrad}$
- signal reversals



Linear birefringence δ :

linear birefringence presents an adversity to high precision optical rotation measurements using high-finesse cavities

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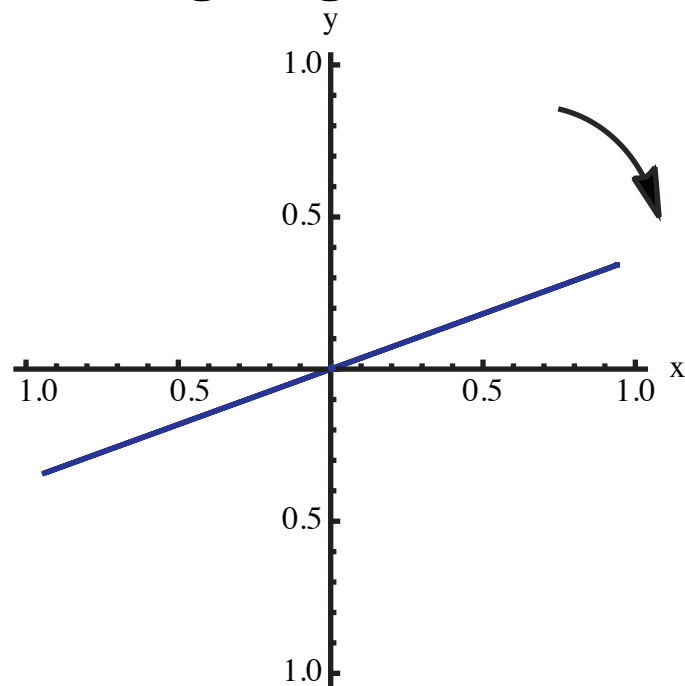
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$\delta = \pi / (2N) \Rightarrow$ after N passes
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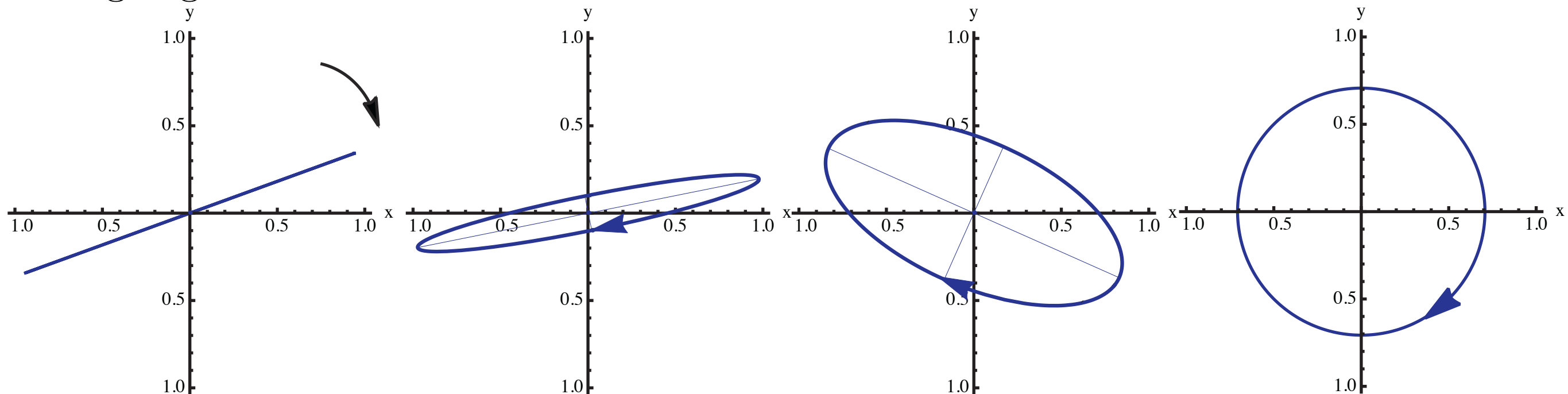
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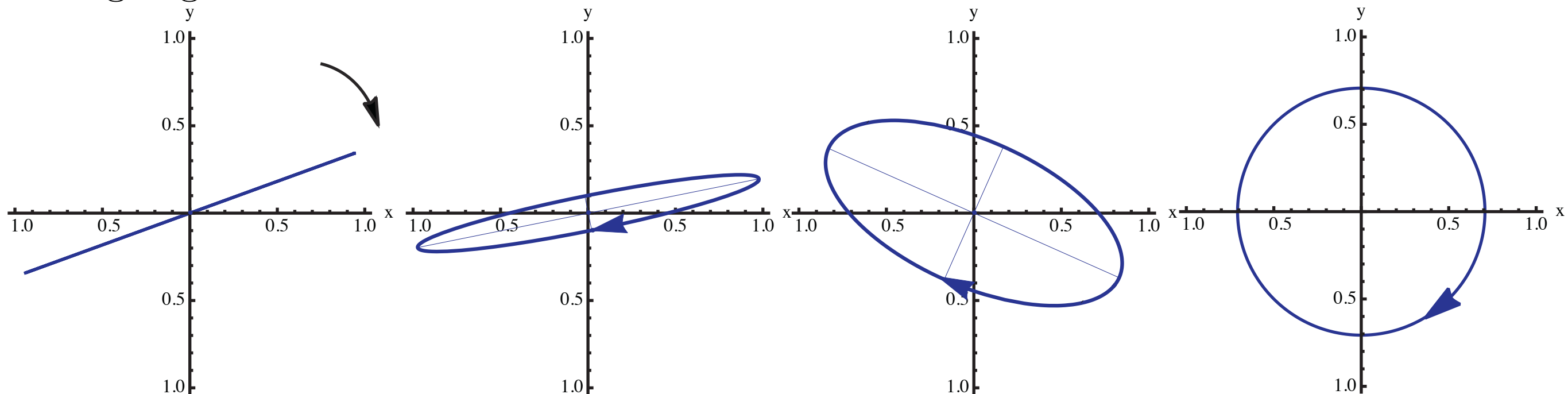
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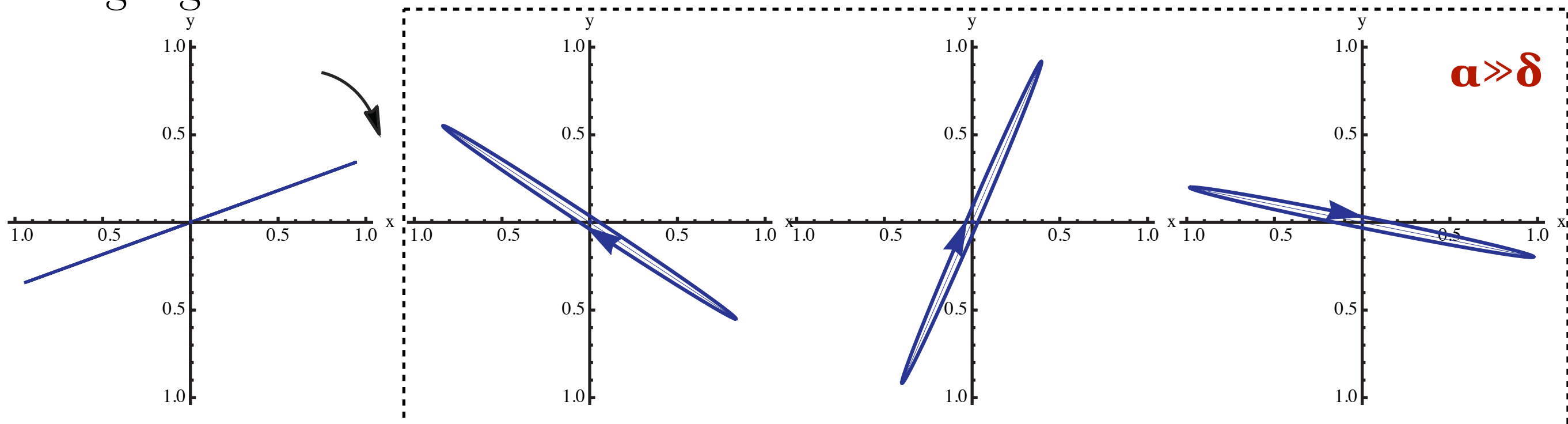
How?

inducing a larger circular birefringence $\alpha \gg \delta$
 keeps intracavity light linearly polarized

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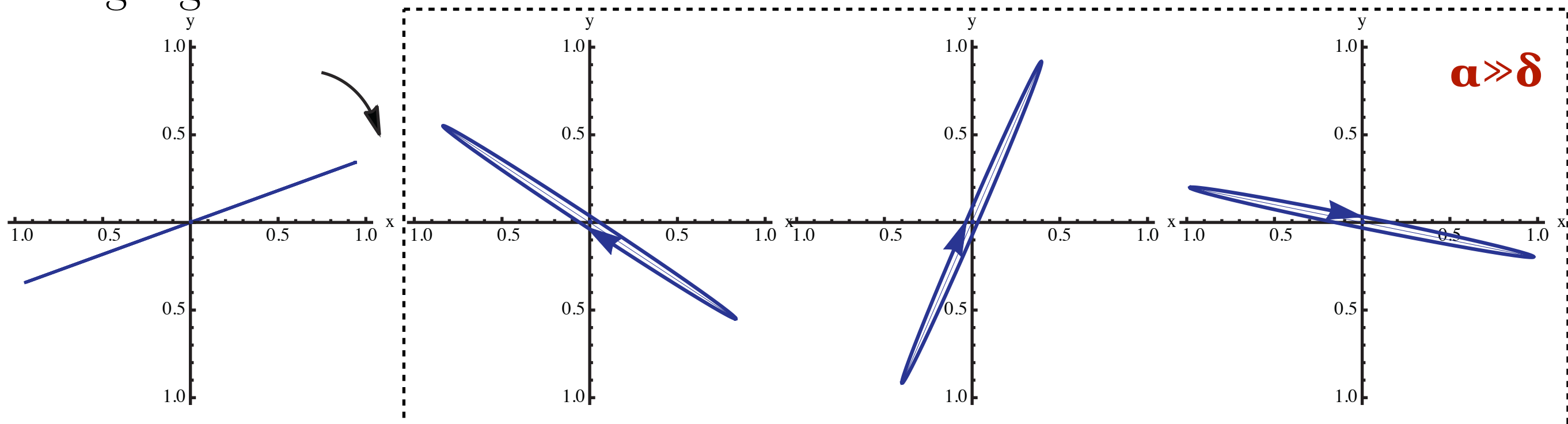
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$\alpha \gg \delta$ ensures the enhancement of the circular birefringence

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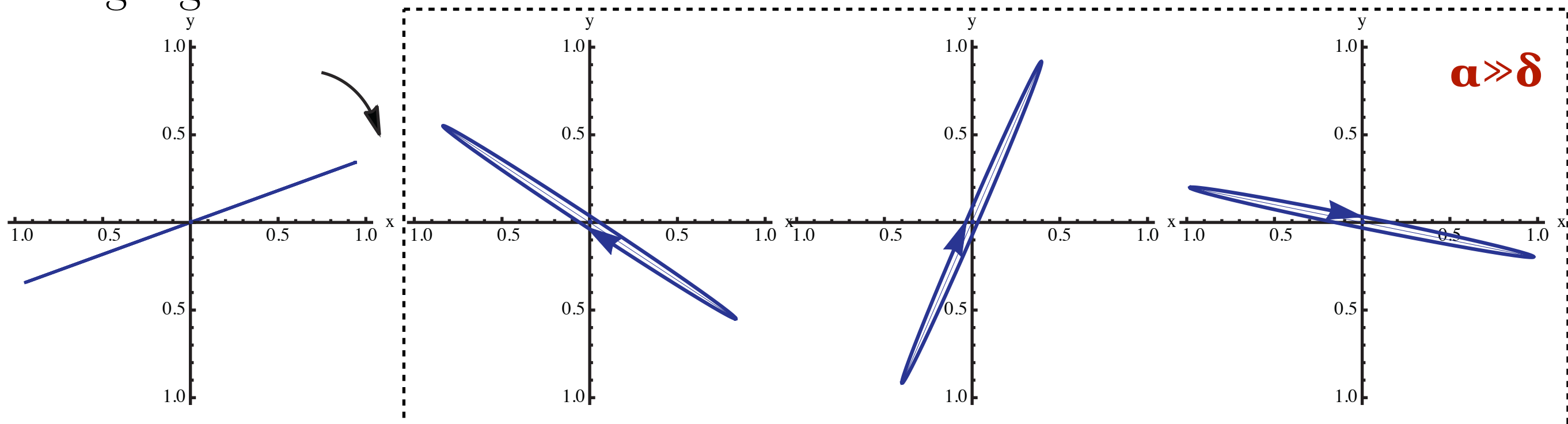
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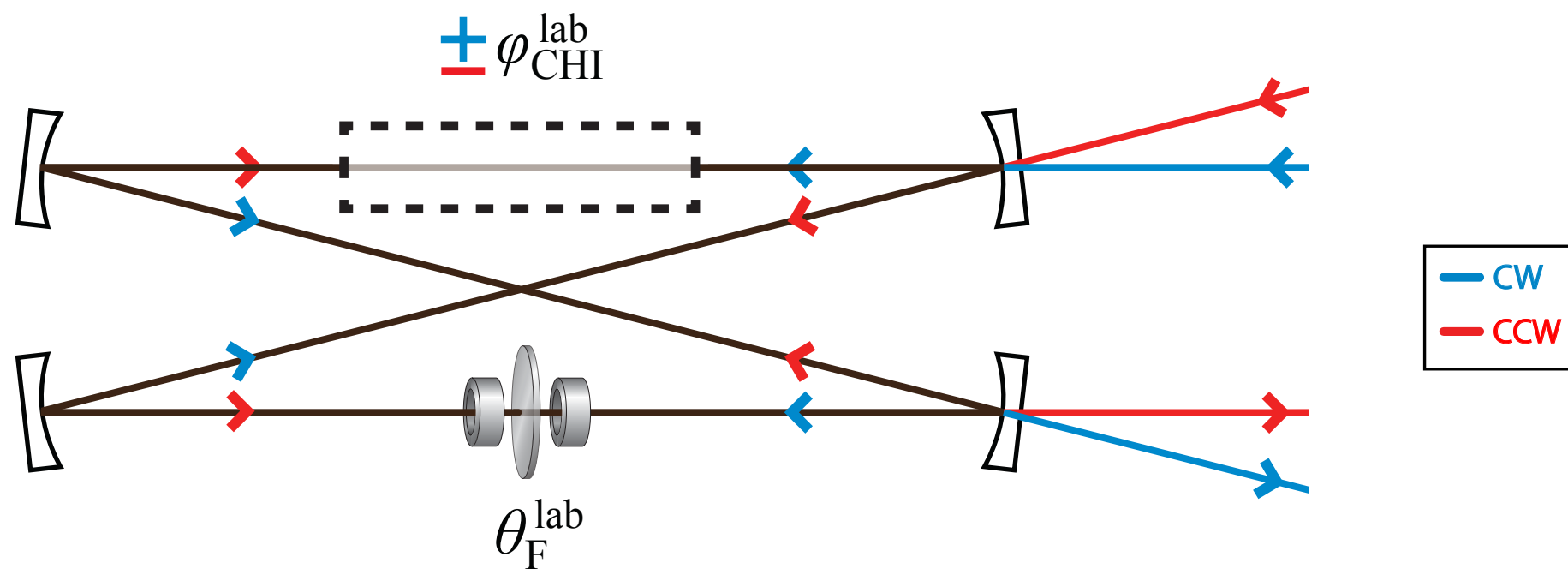


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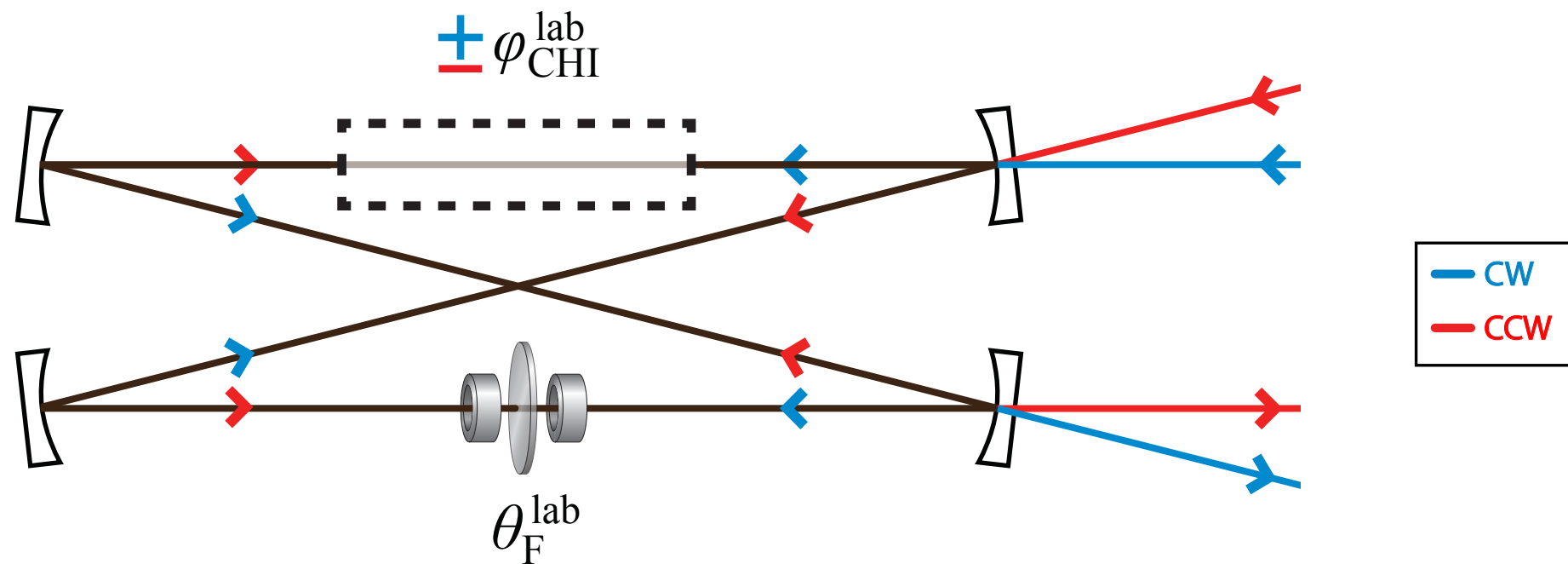
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P even & T odd

Principles of the technique



Principles of the technique



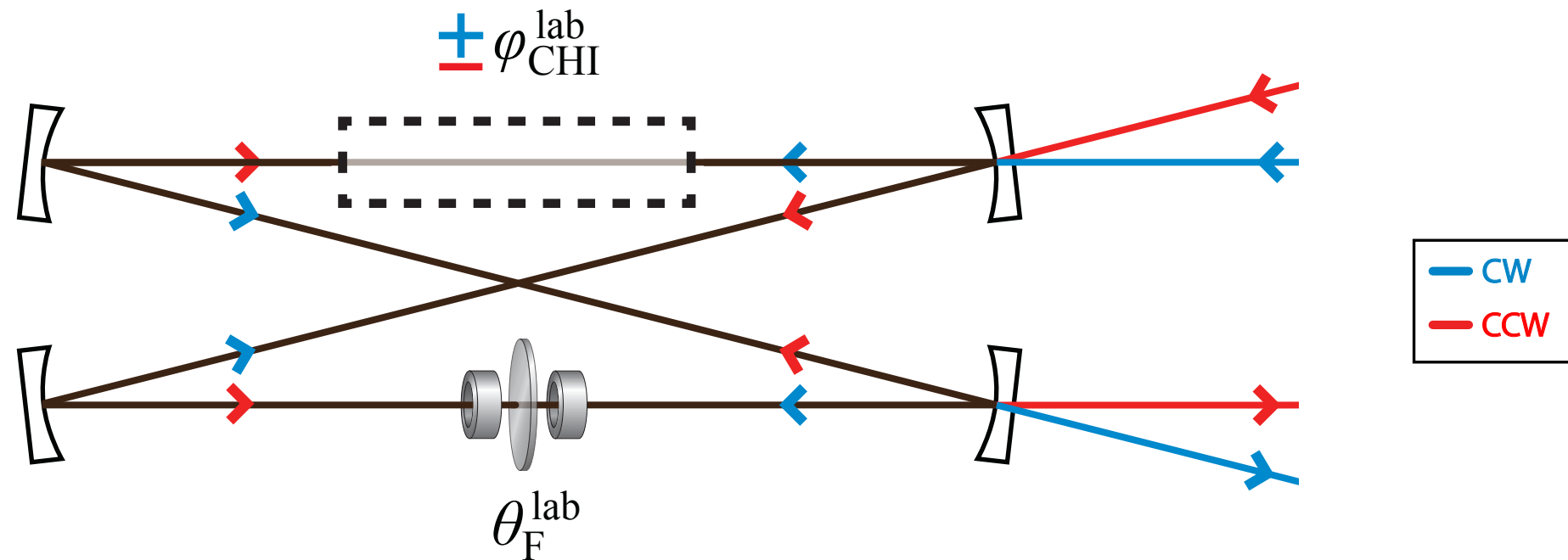
for a single pass:

$+\vec{B}$

$$\alpha_{\text{CW}} = \theta_{\text{F}} + \phi_{\text{CHI}}$$

$$\alpha_{\text{CCW}} = \theta_{\text{F}} - \phi_{\text{CHI}}$$

Principles of the technique



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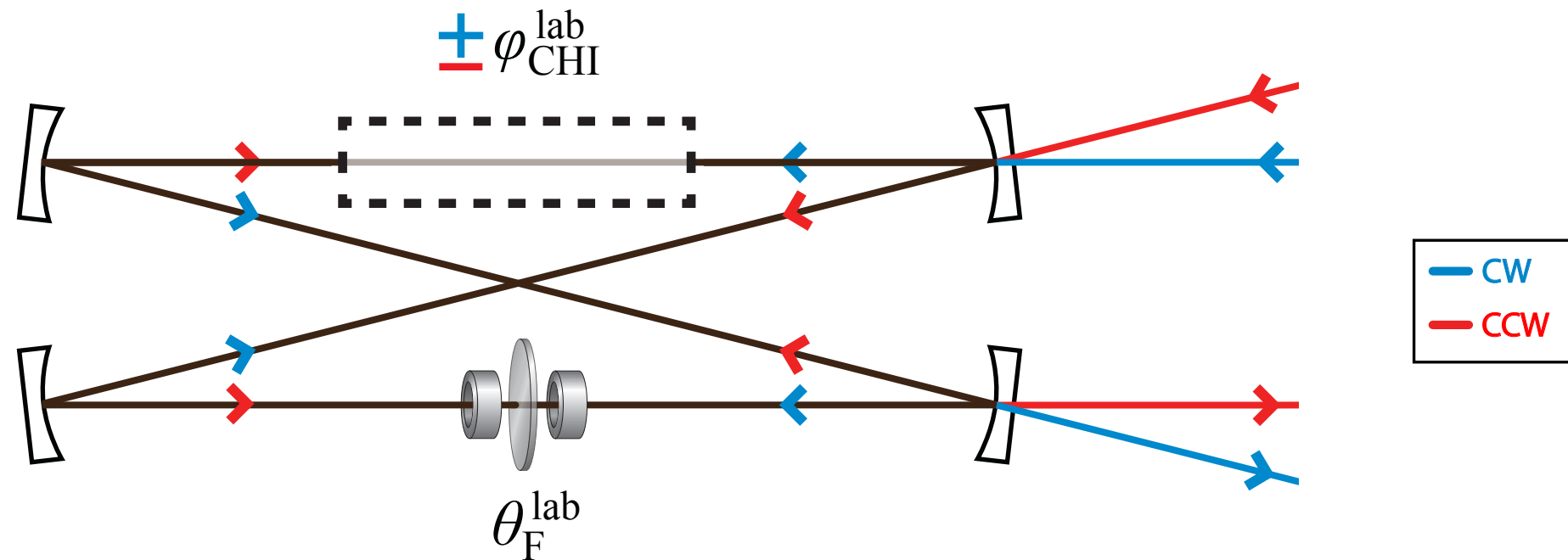
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$$\alpha_{\text{CW}} - \alpha_{\text{CCW}} = 2\phi_{\text{CHI}}$$

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REVERSAL $-\vec{B}$

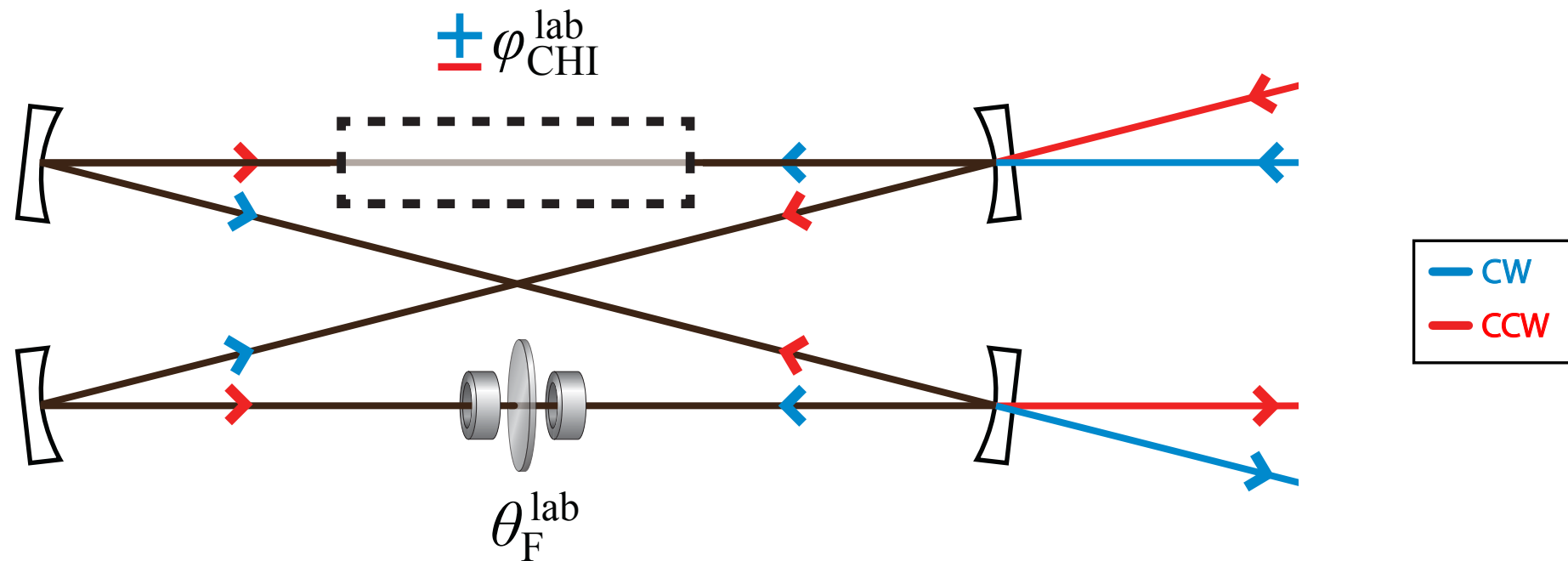
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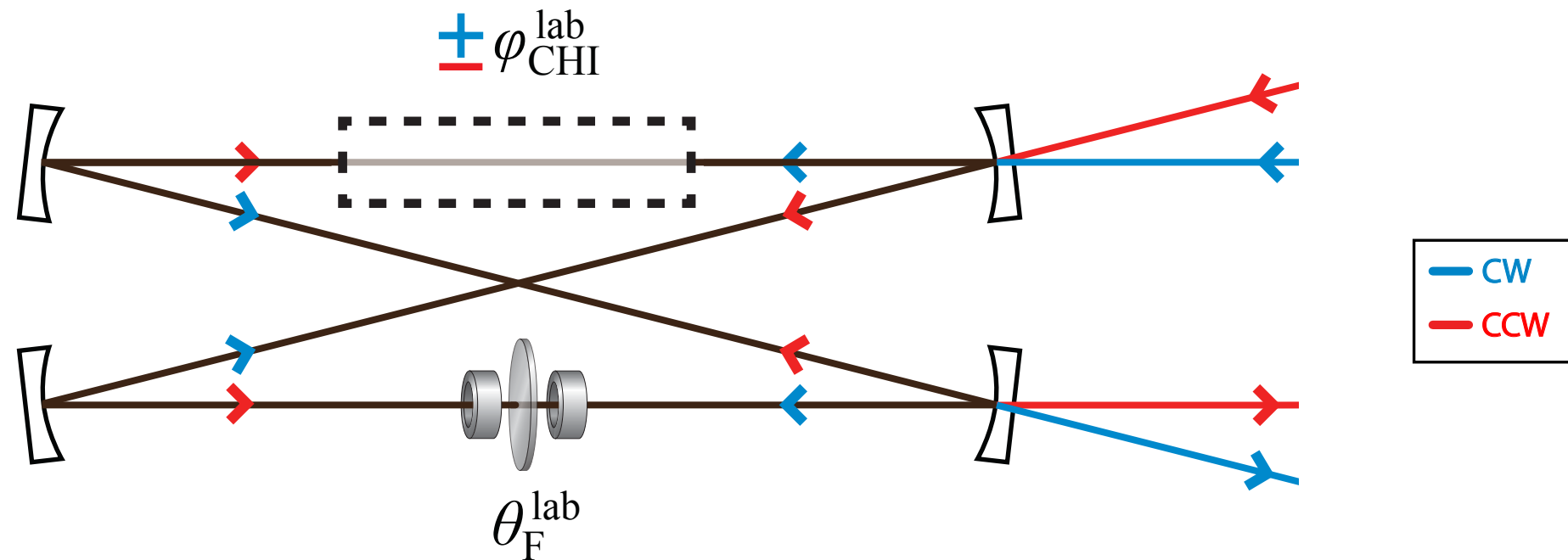
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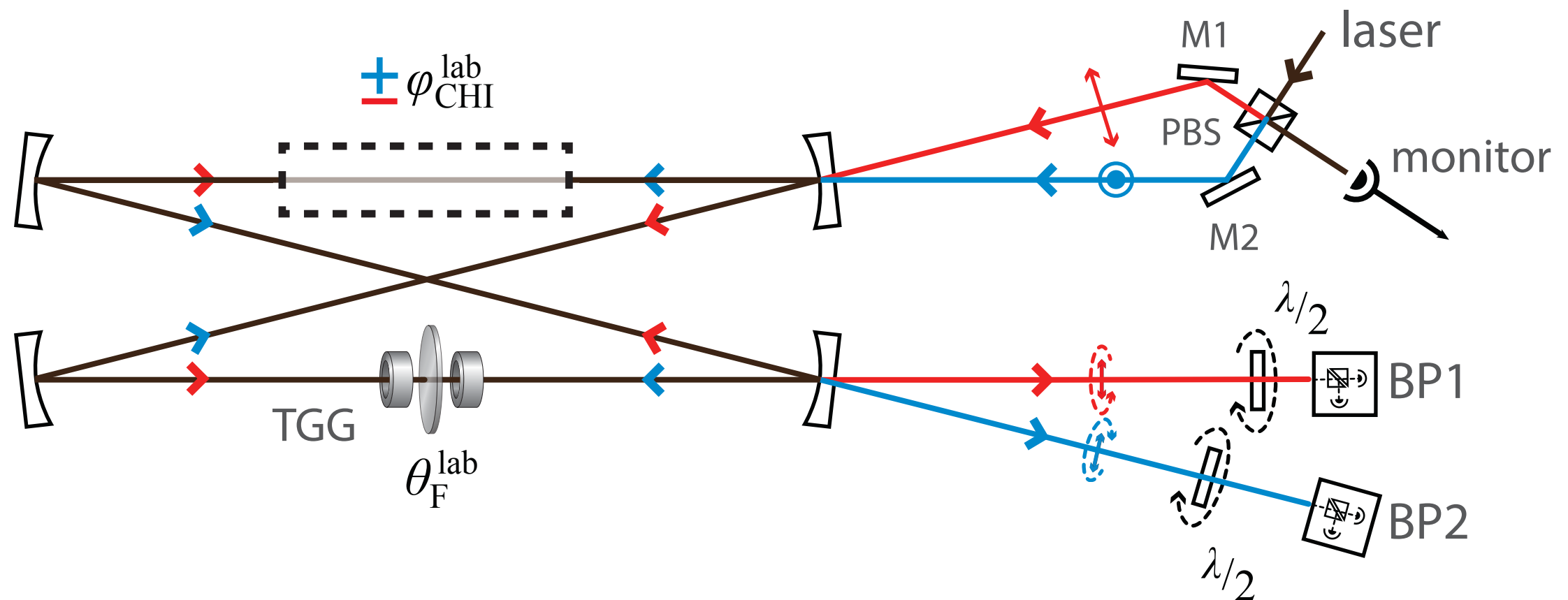
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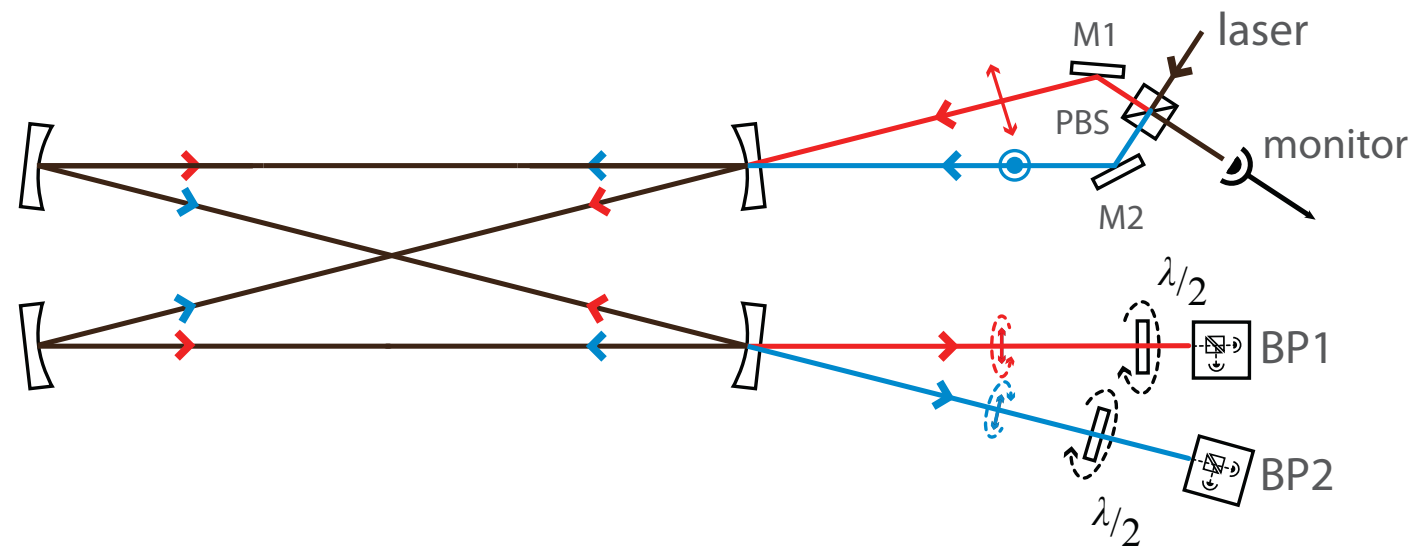
symmetry breaking allows one to perform
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$$\Delta\alpha(+B) - \Delta\alpha(-B) = 4\phi_{\text{CHI}}$$

Chiral Cavity Ring Down

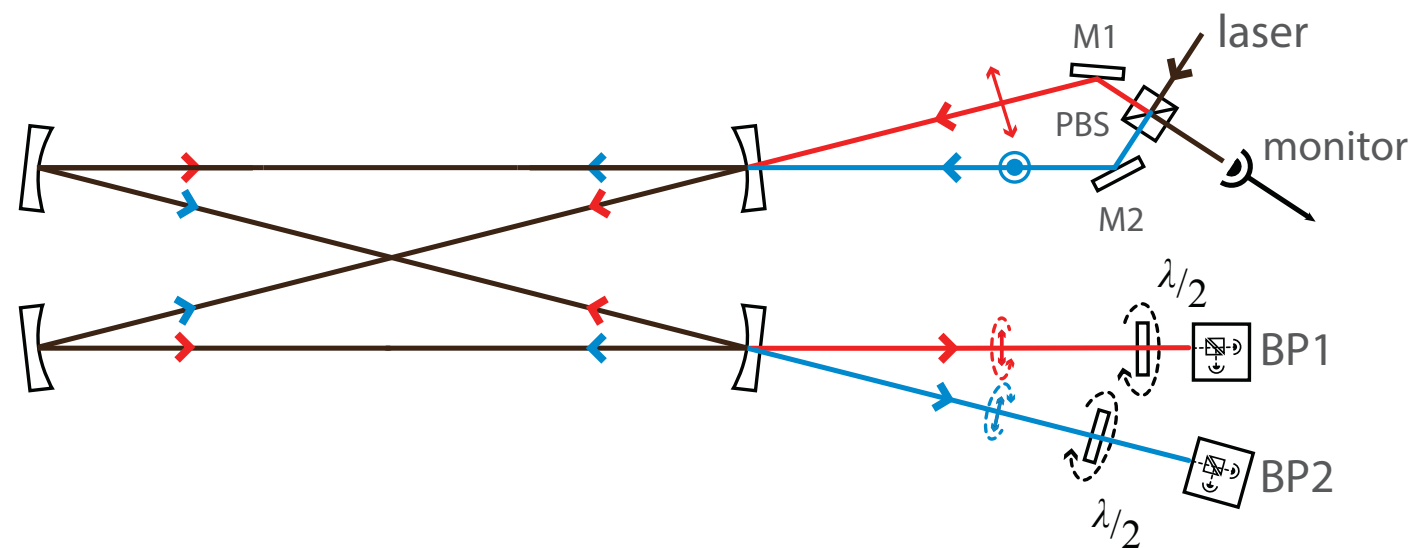


A pulsed proof-of-principle experiment



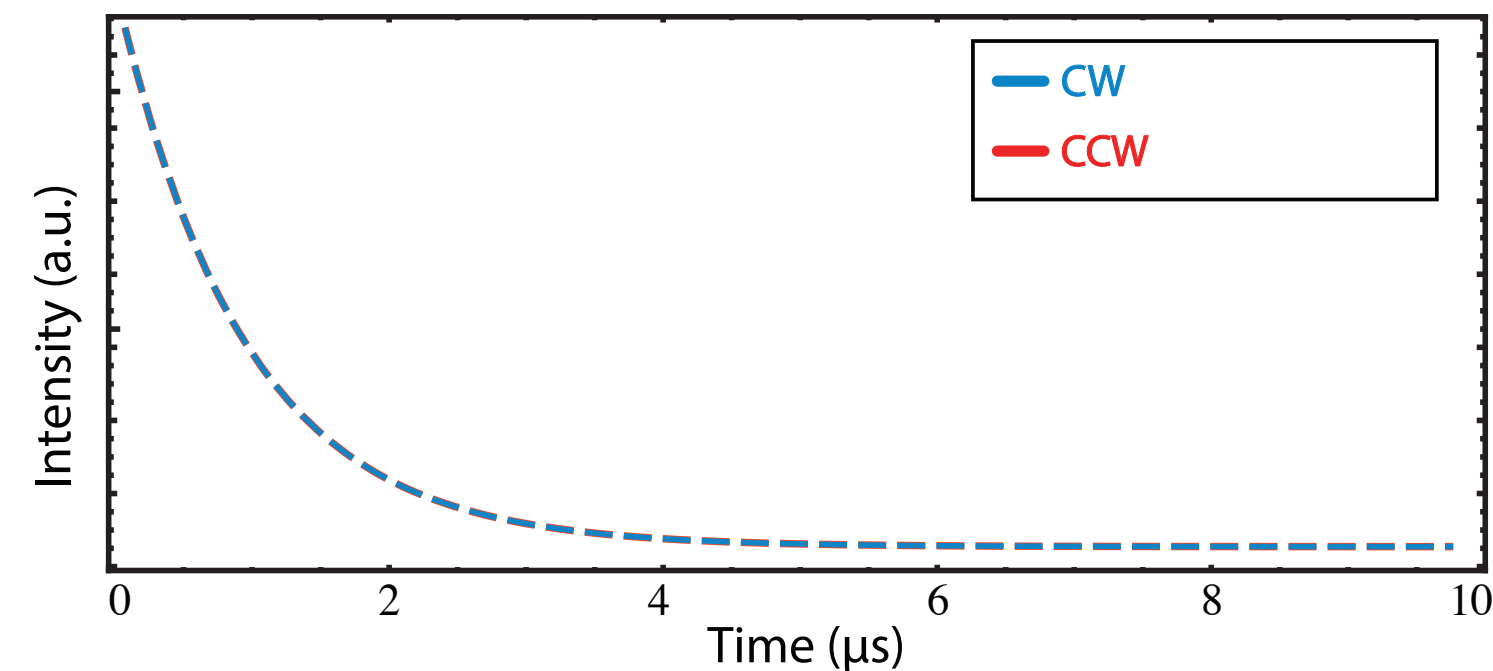
Cavity Ring Down:

one measures the temporal evolution of a light pulse injected in the cavity



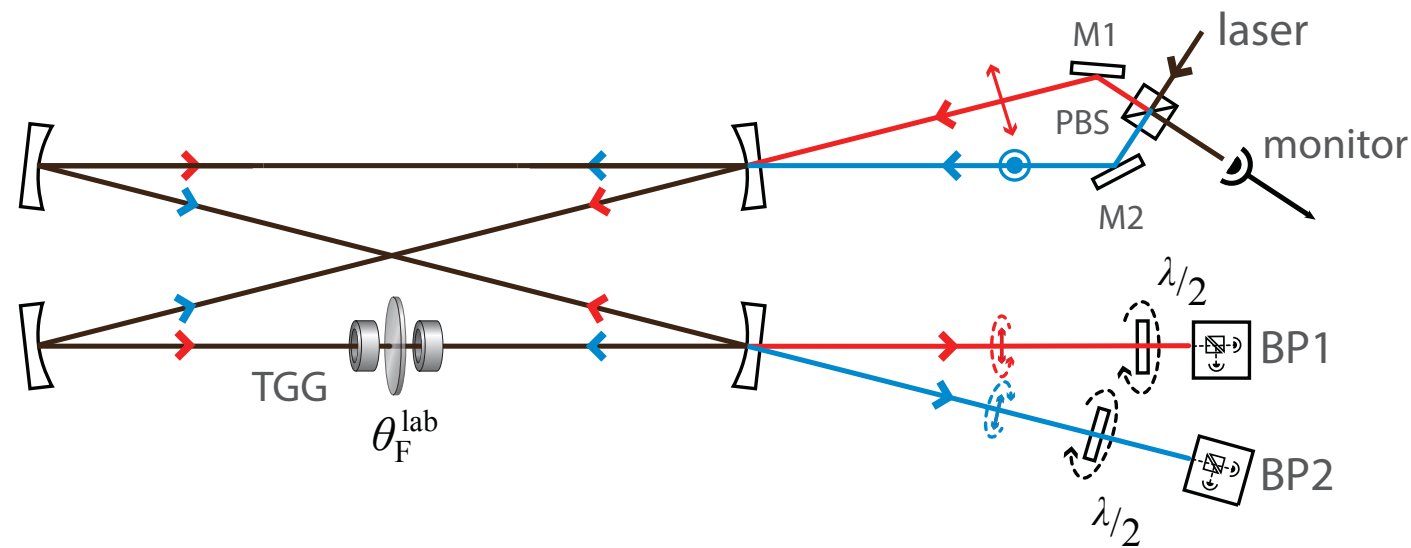
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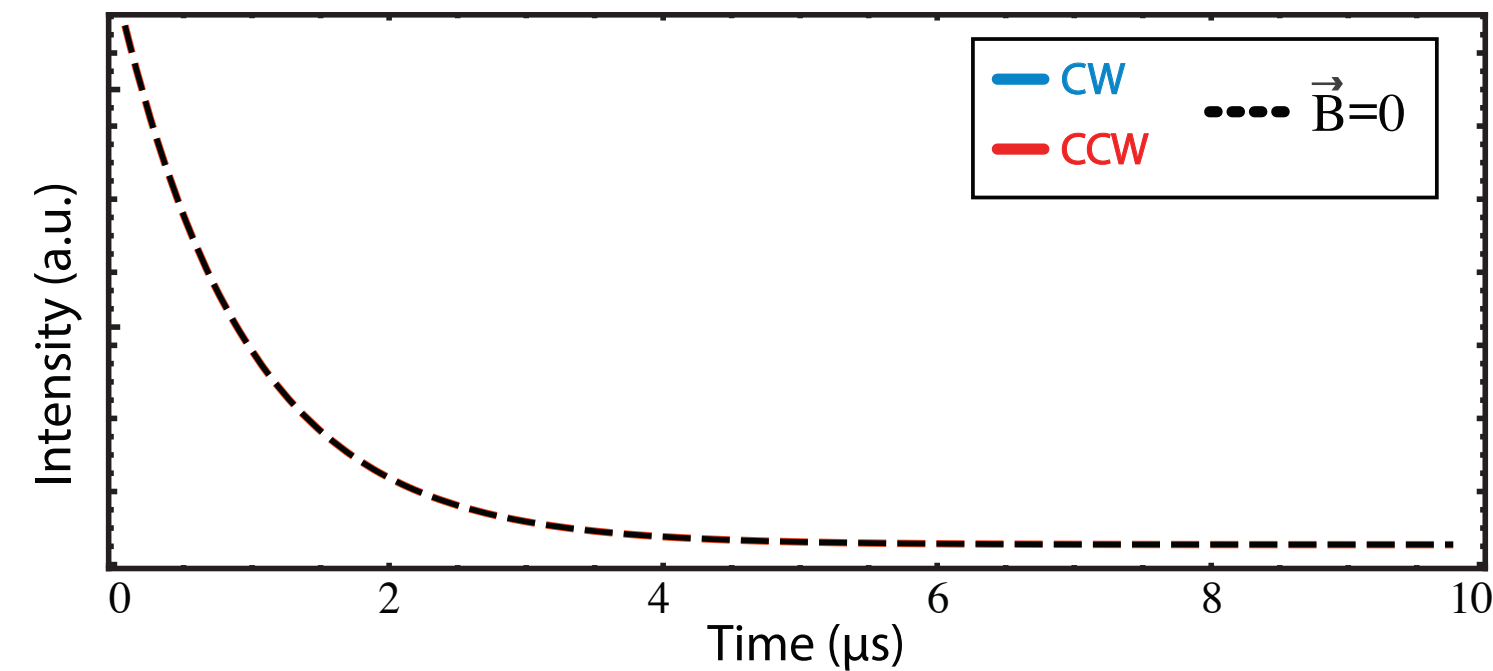


parameters

- ROC=-1m, $R > 0.998\%$, $l=3.6\text{m}$
- laser @ 800nm, $\tau \approx 32\text{fs}$, $\Delta\nu=40\text{nm}$, rep. rate 1kHz, $\sim 2\text{mJ/pulse}$



$\vec{B}=0$



Cavity Ring Down:

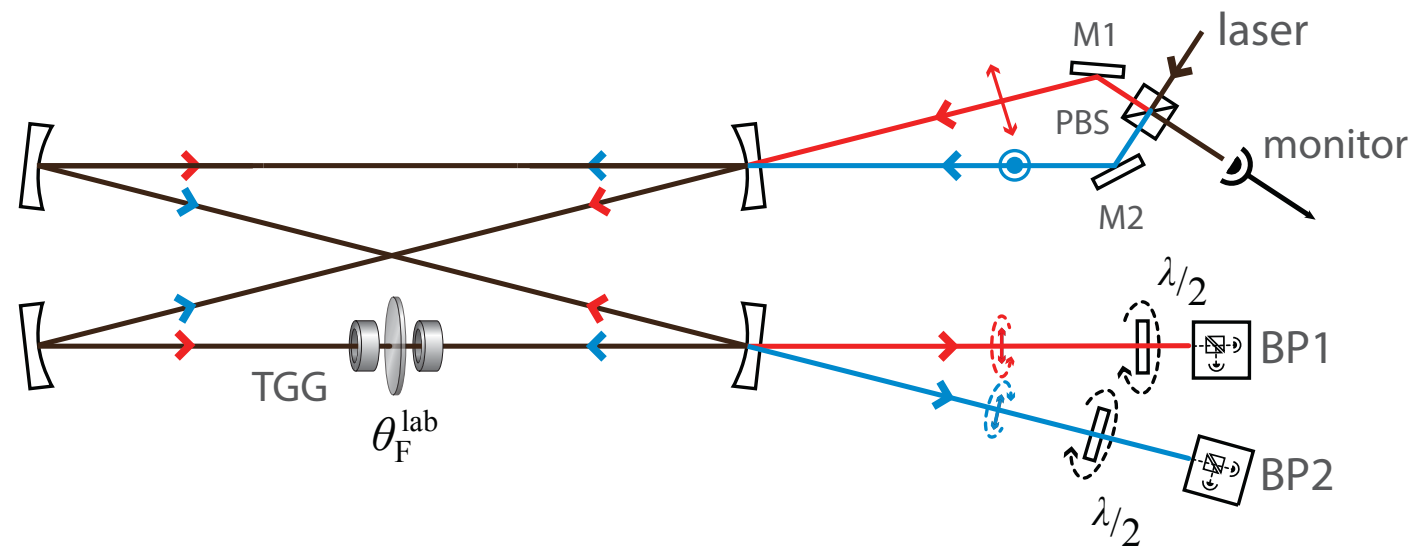
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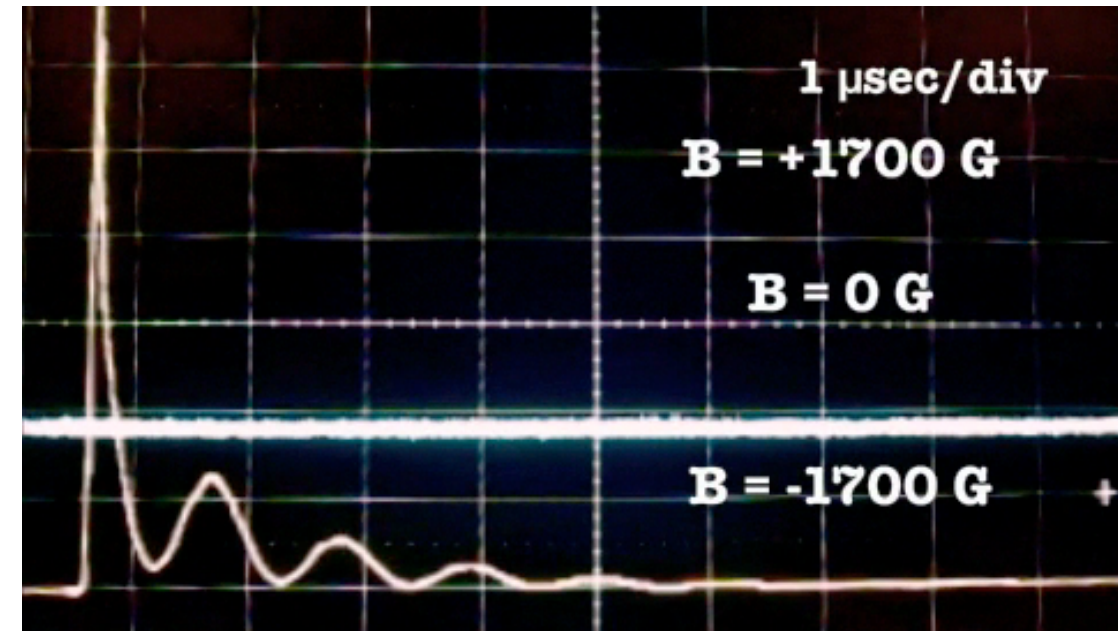
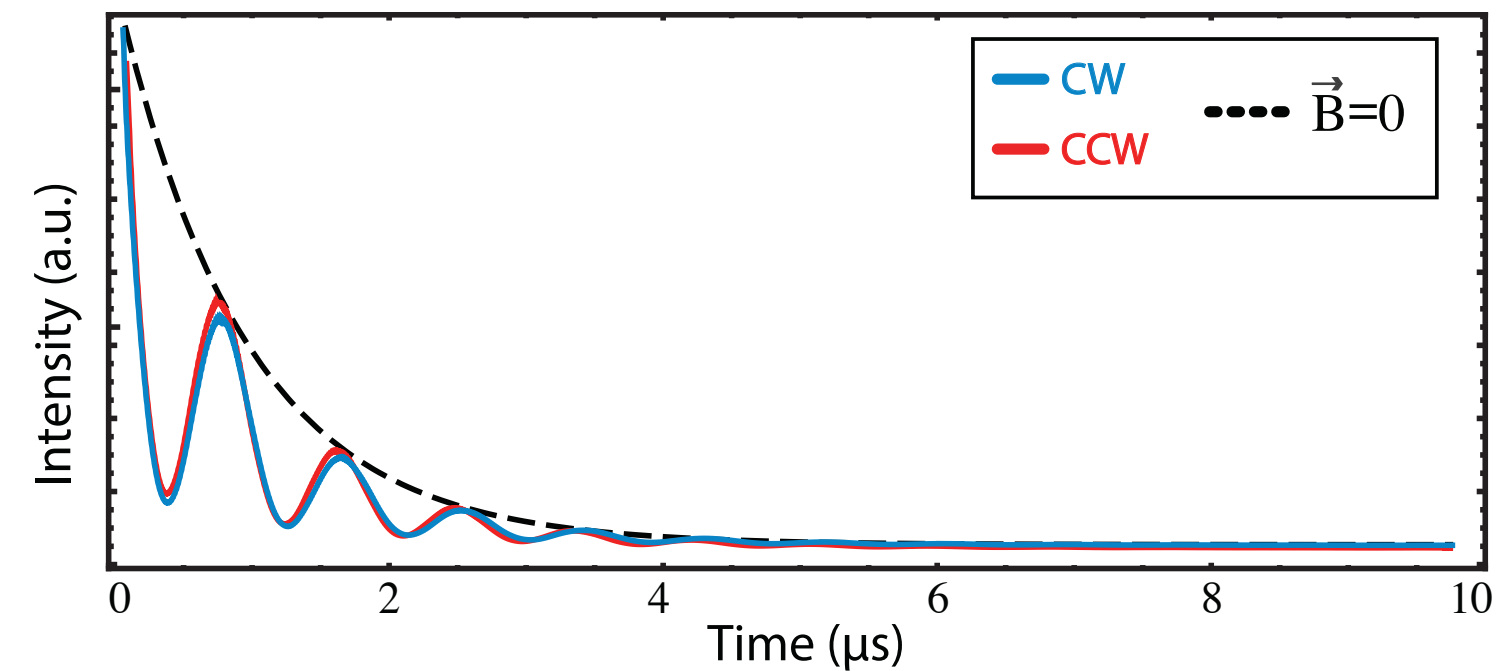
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- **TerbiumGalliumGarnet** $V\sim 80\text{ rad T}^{-1}\text{ cm}^{-1}$

Chiral Cavity Ring Down

Experiment



$\vec{B} \neq 0$

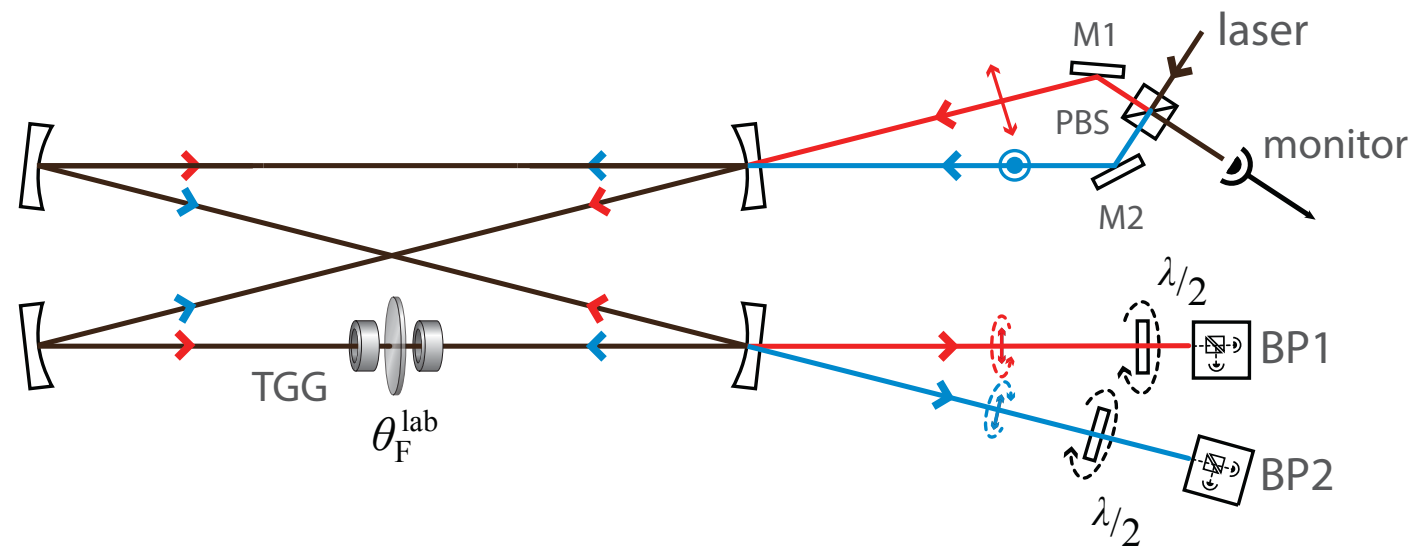


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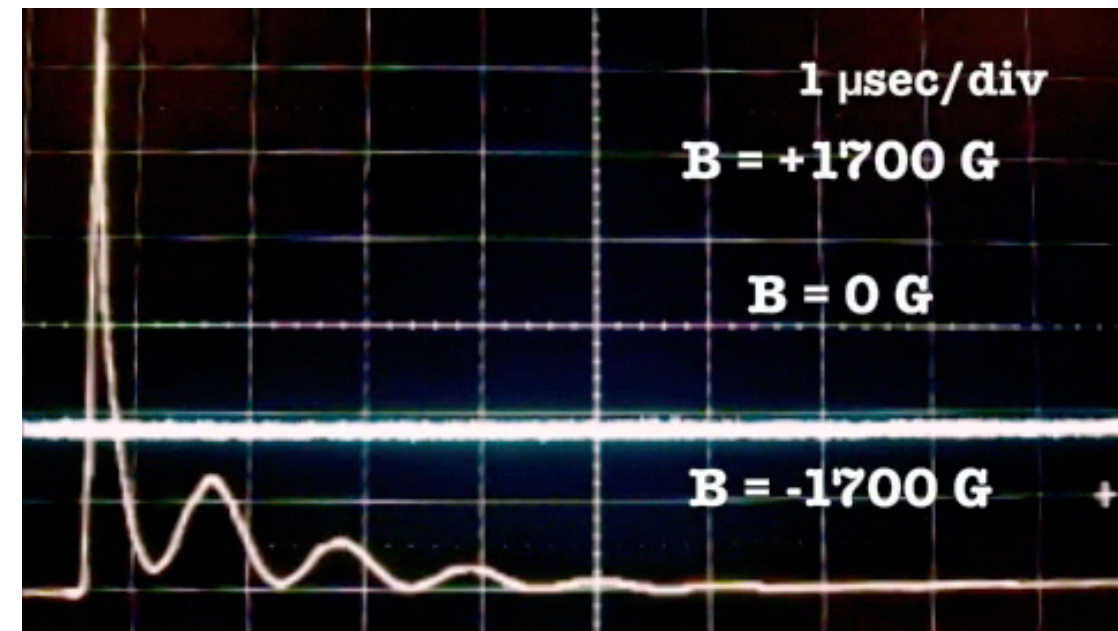
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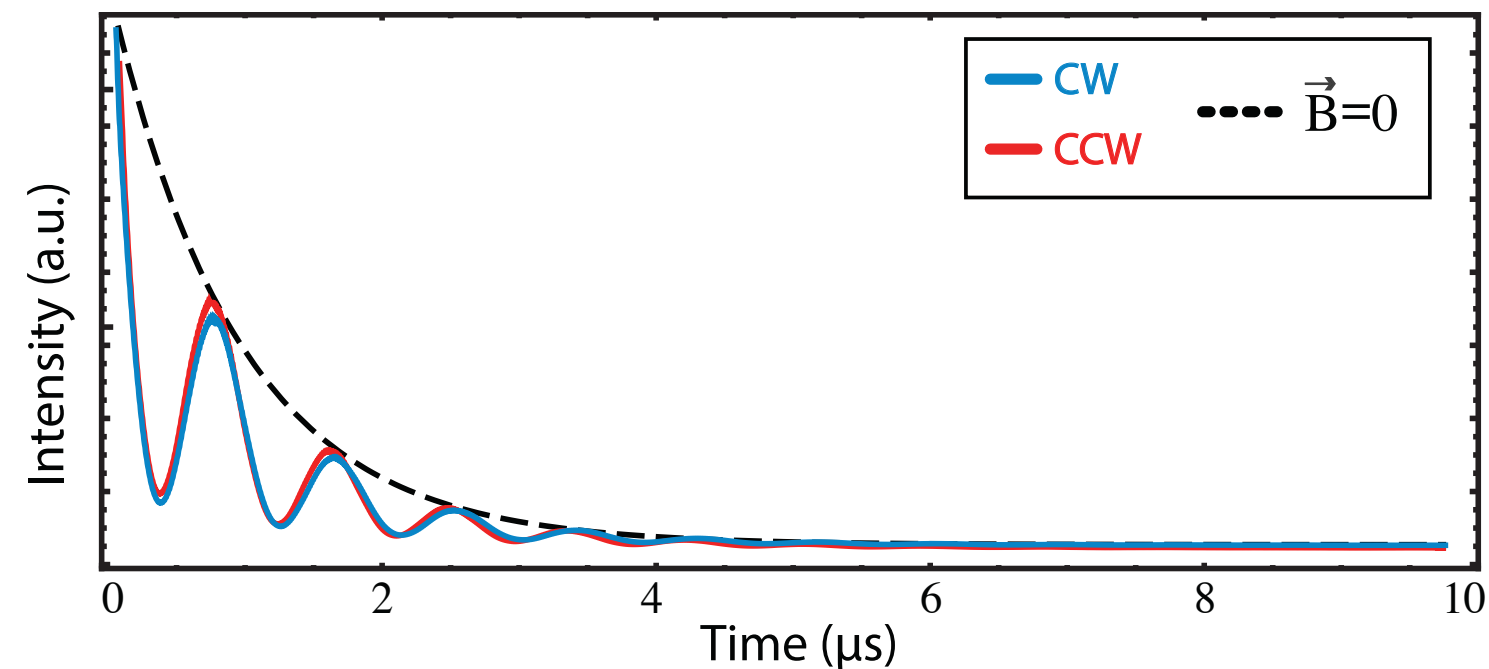


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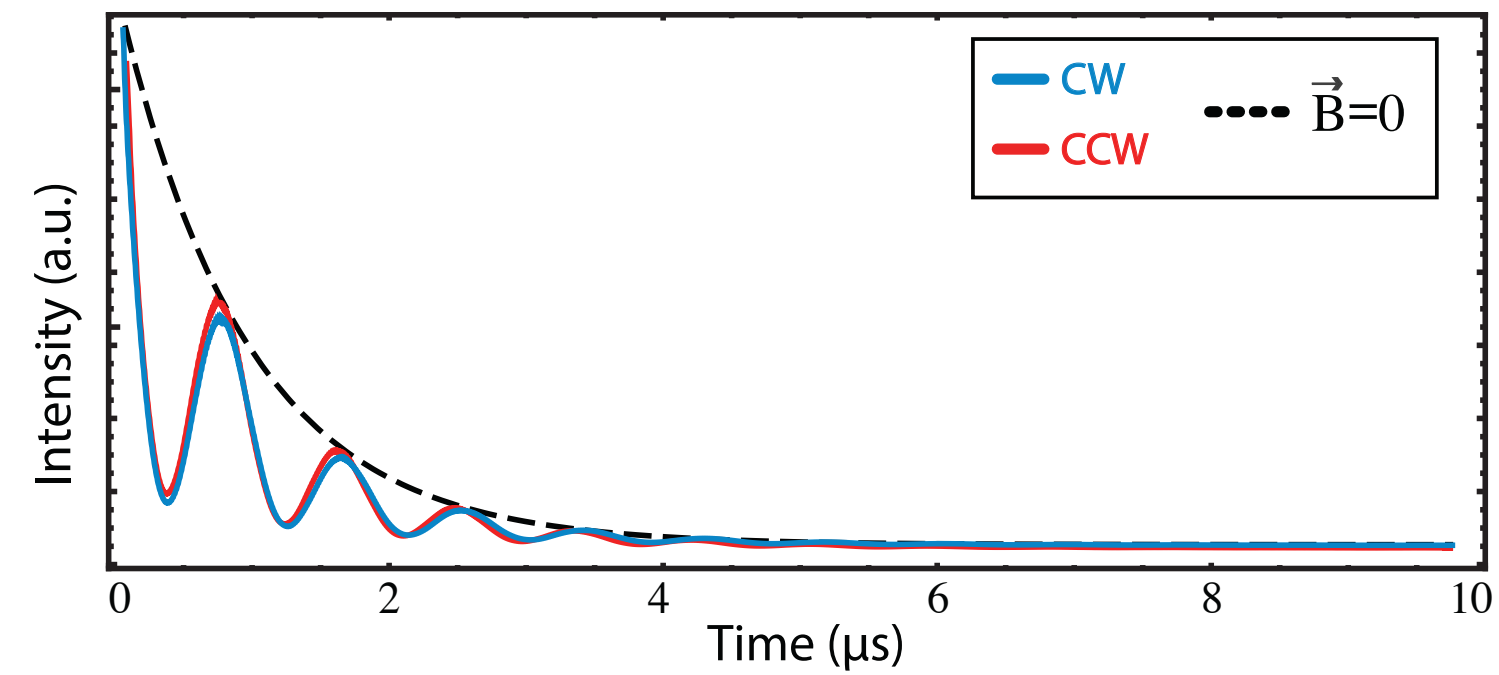
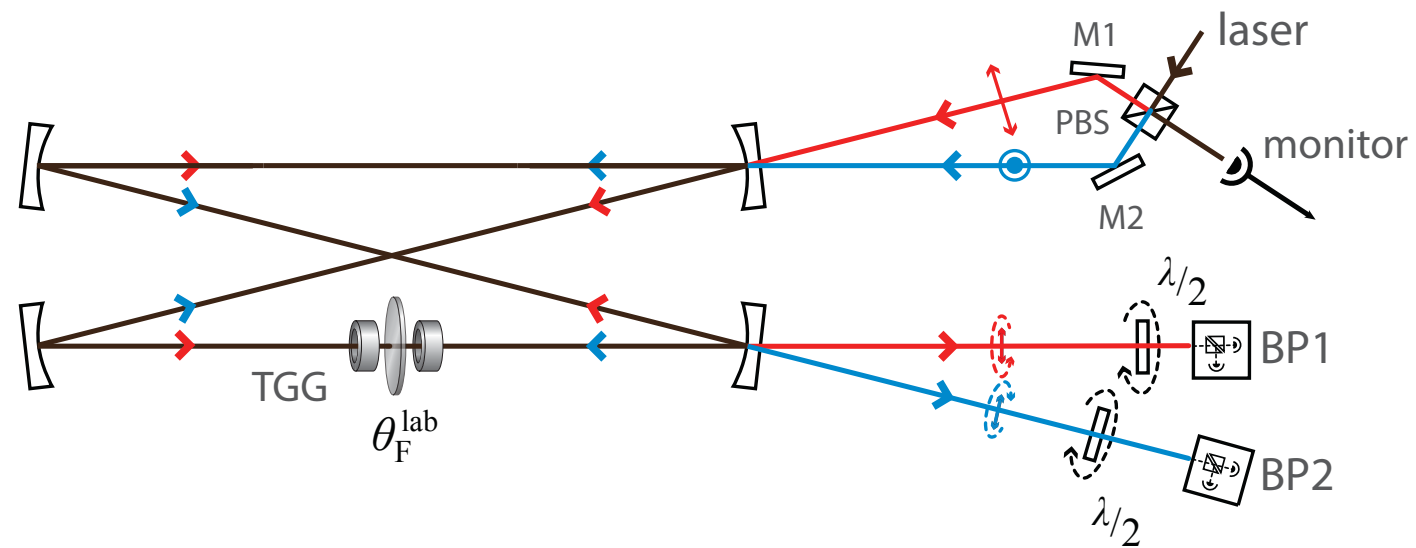
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CRD Polarimetry: one measures the rate of the **polarization rotation of light** injected in the cavity

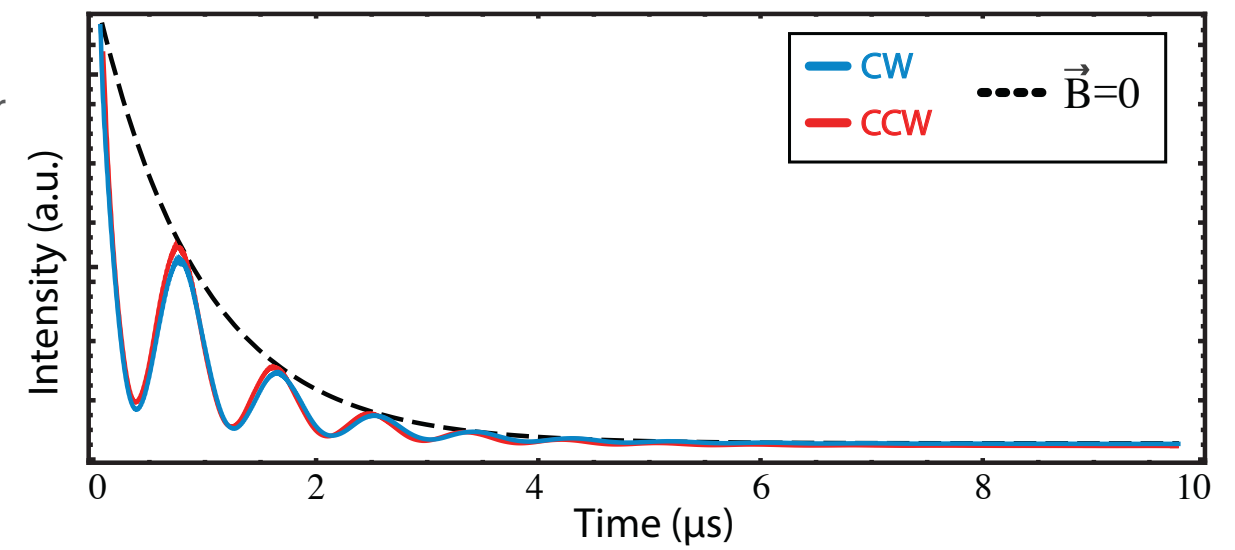
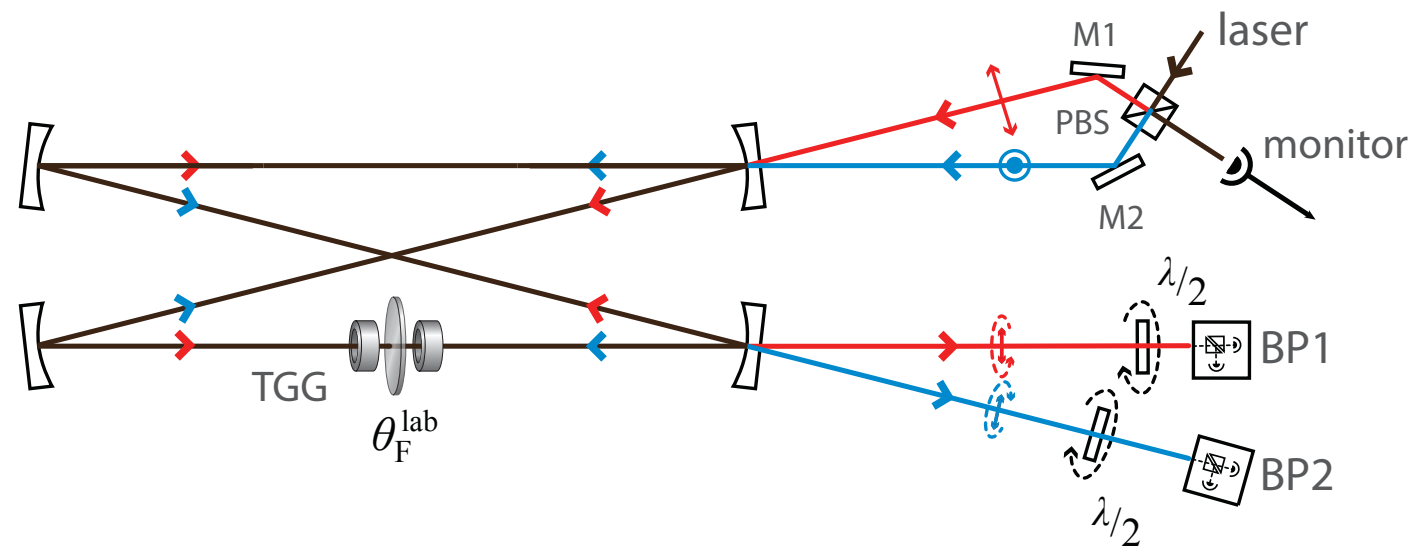
Chiral Cavity Ring Down

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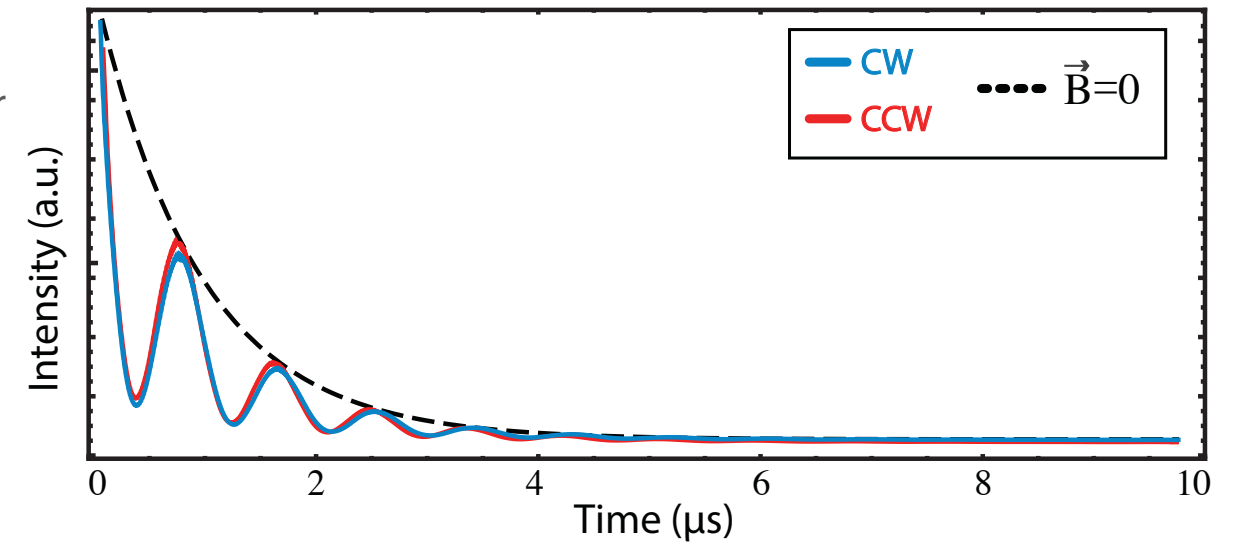
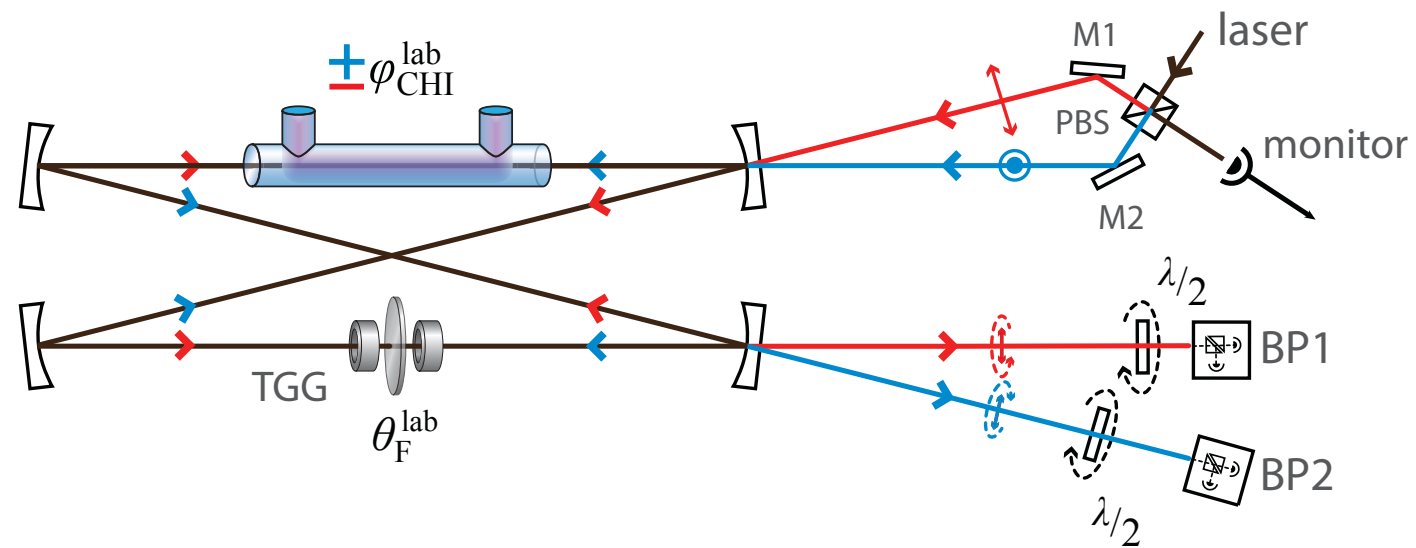
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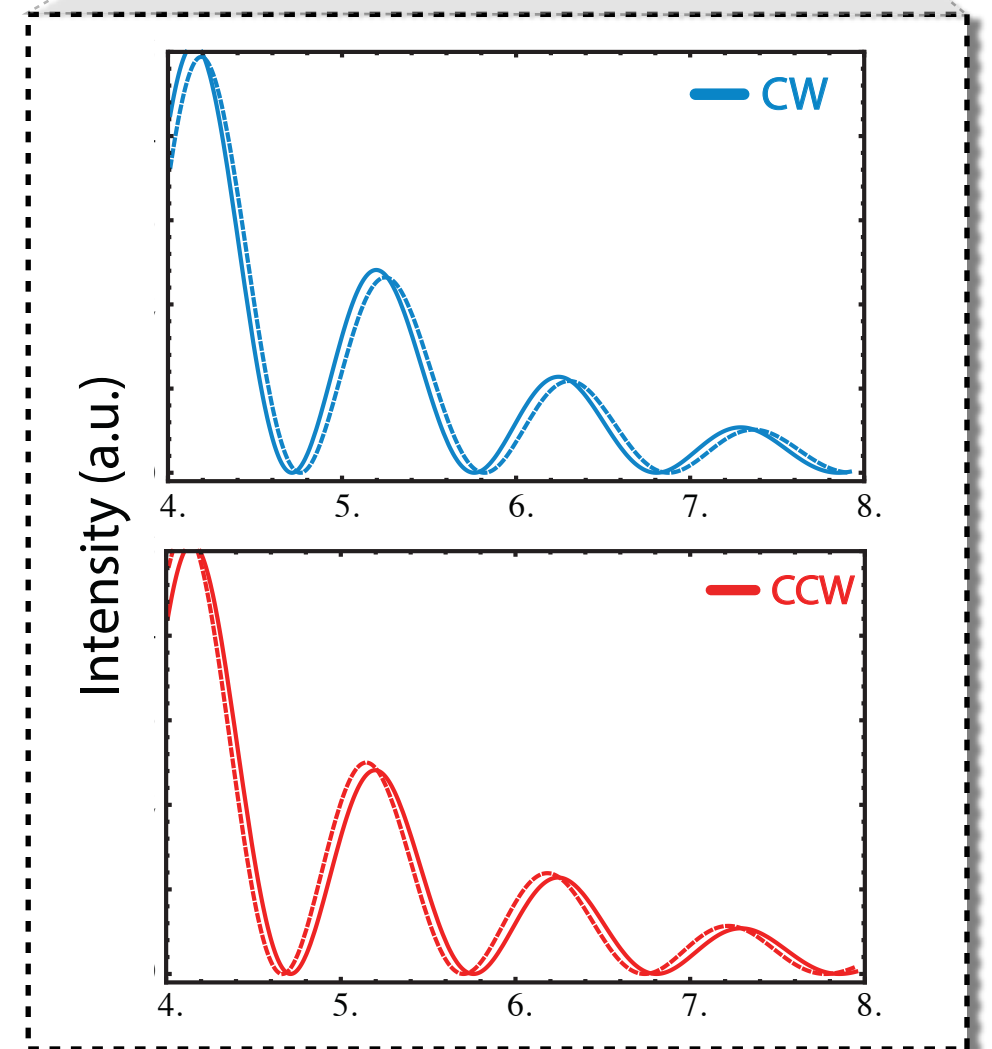
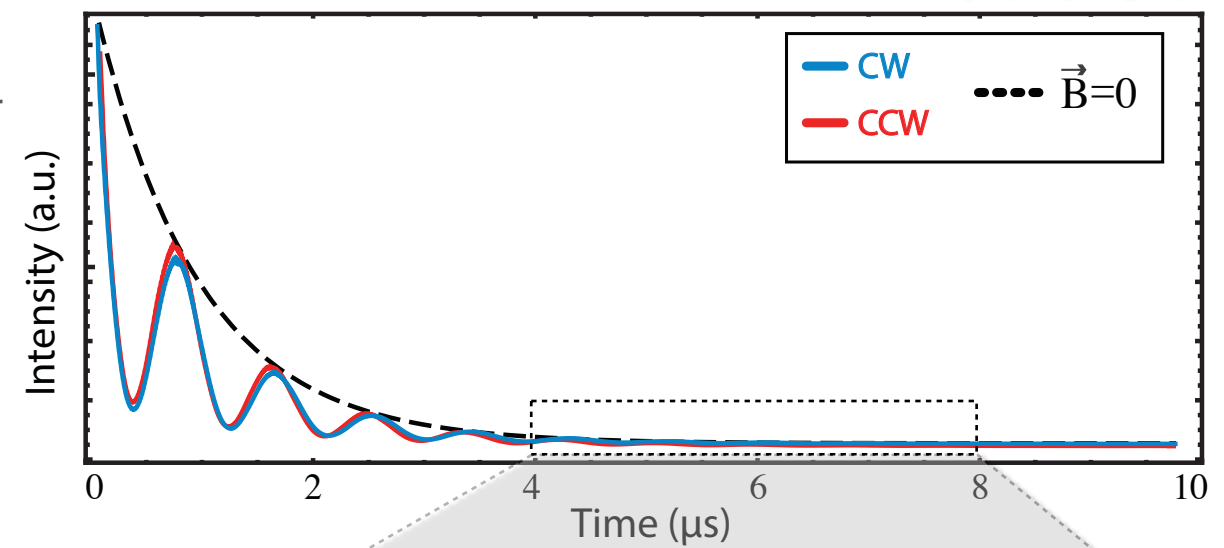
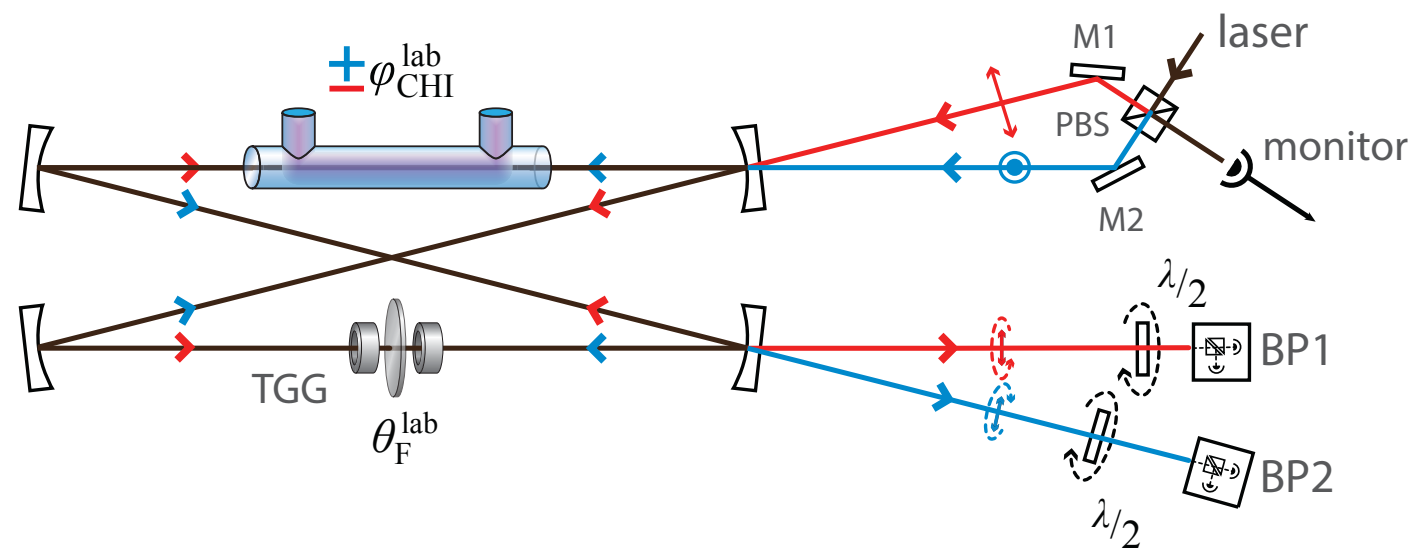
Chiral Cavity Ring Down

Experiment Gas Cell



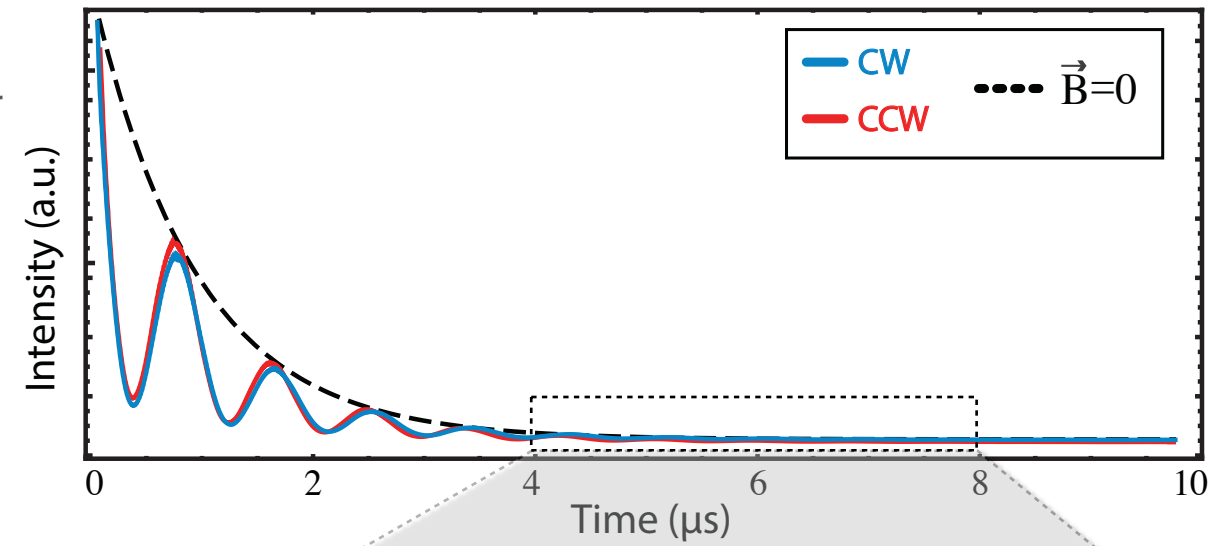
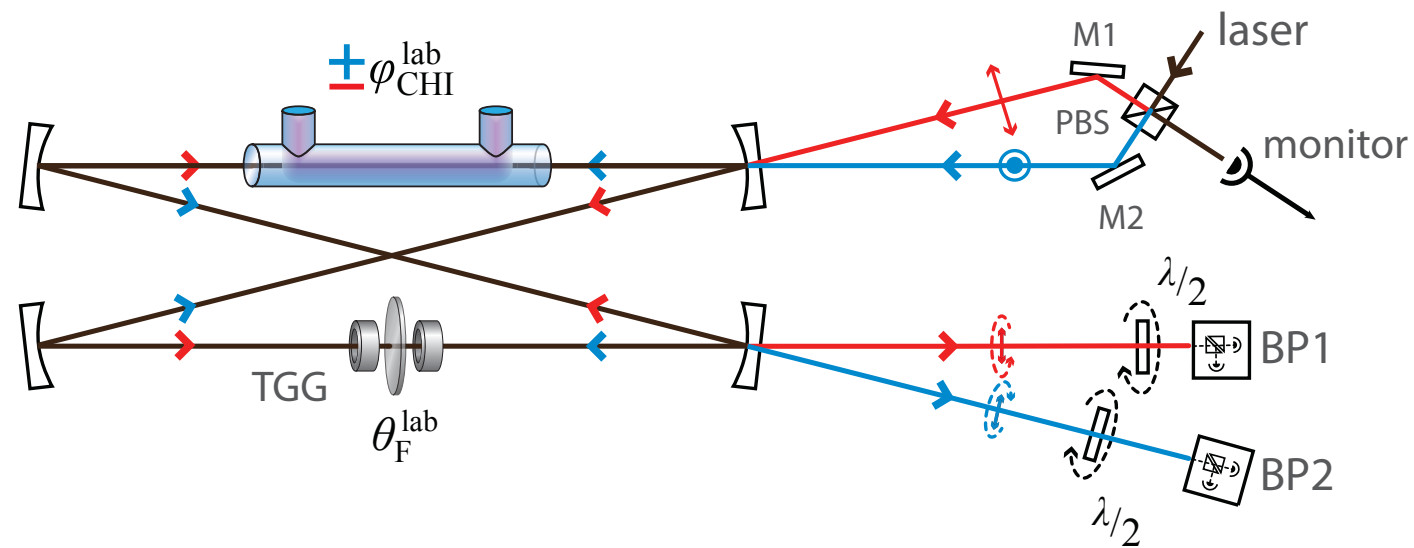
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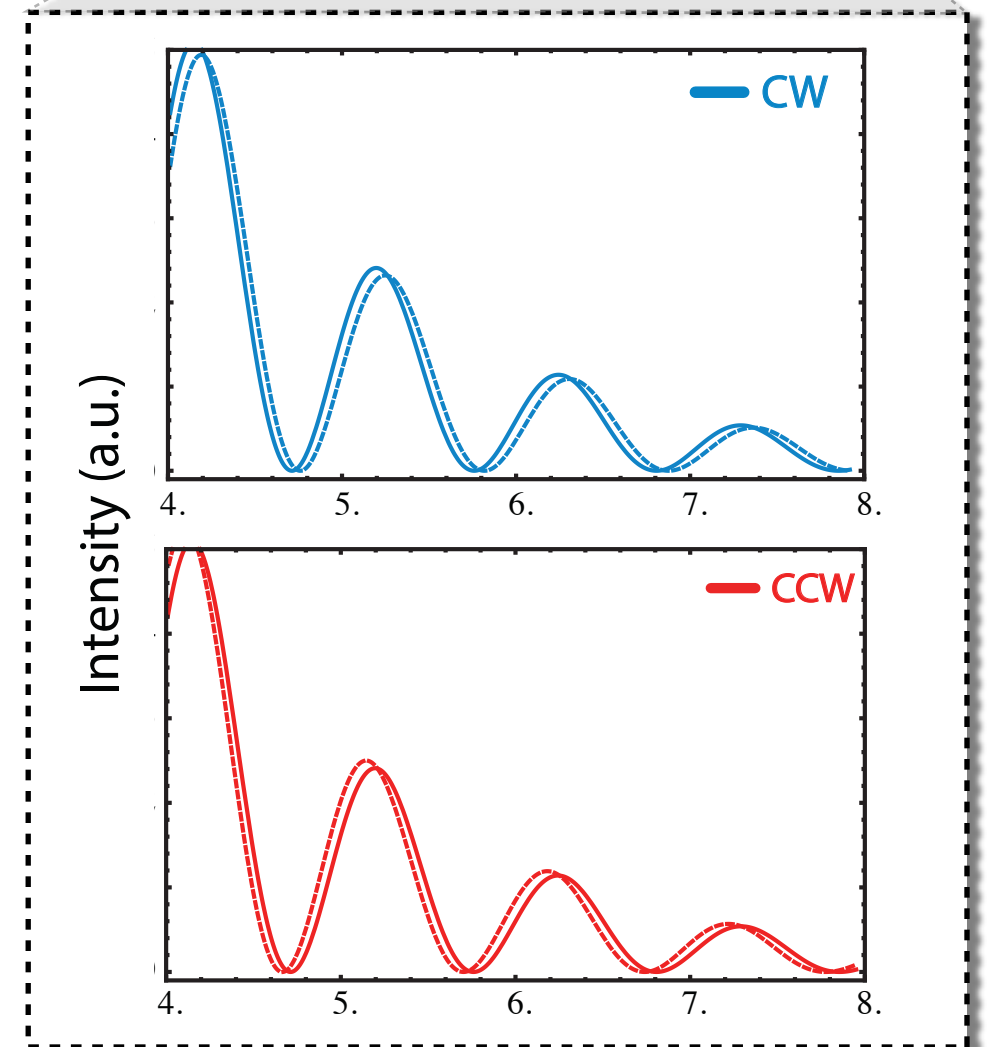
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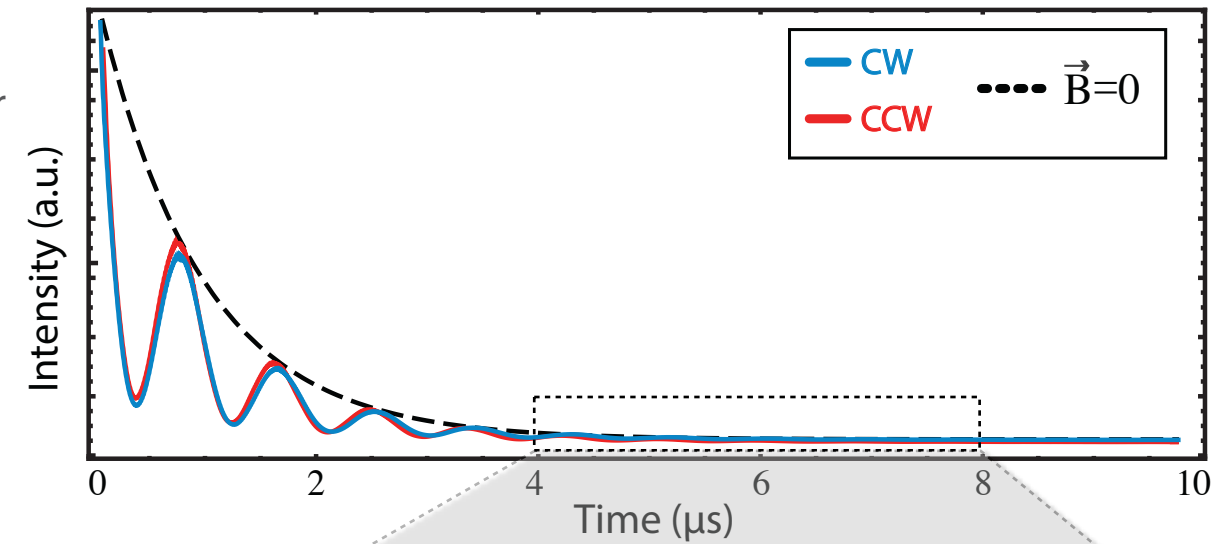
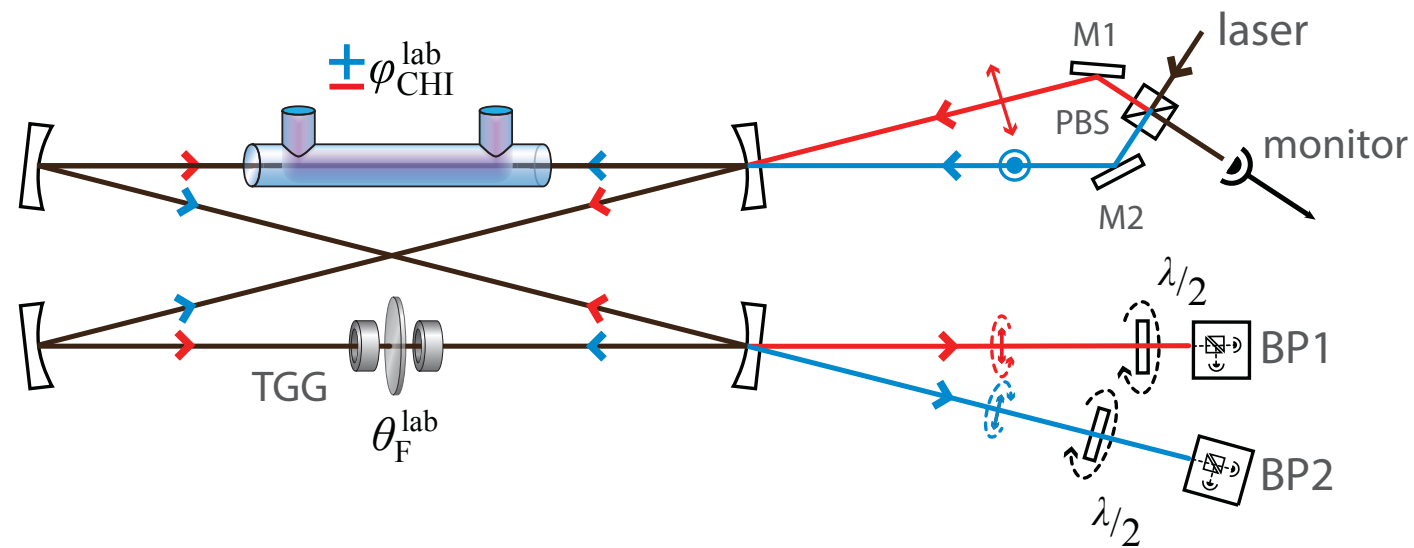
$$I(t) = I_0 e^{-t/\tau} [\cos^2(\omega t + \phi) + \beta]$$

$$\Rightarrow \omega = \alpha_{\text{CW,CCW}} (c/L)$$



Chiral Cavity Ring Down

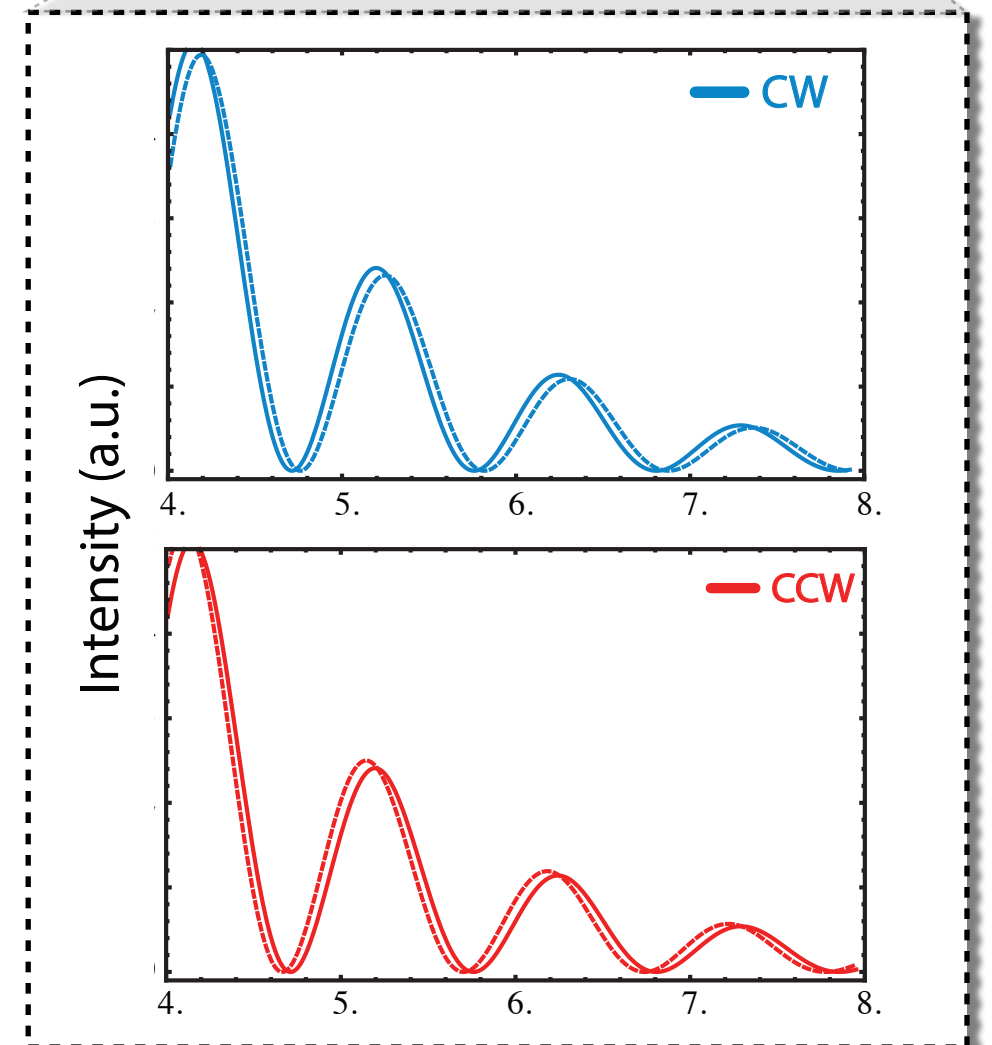
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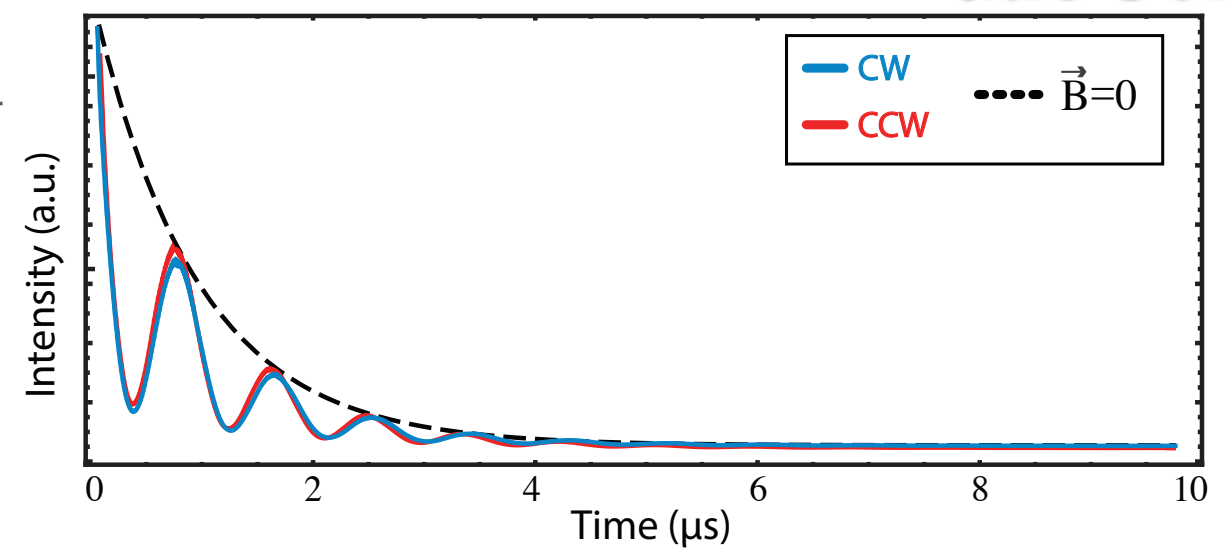
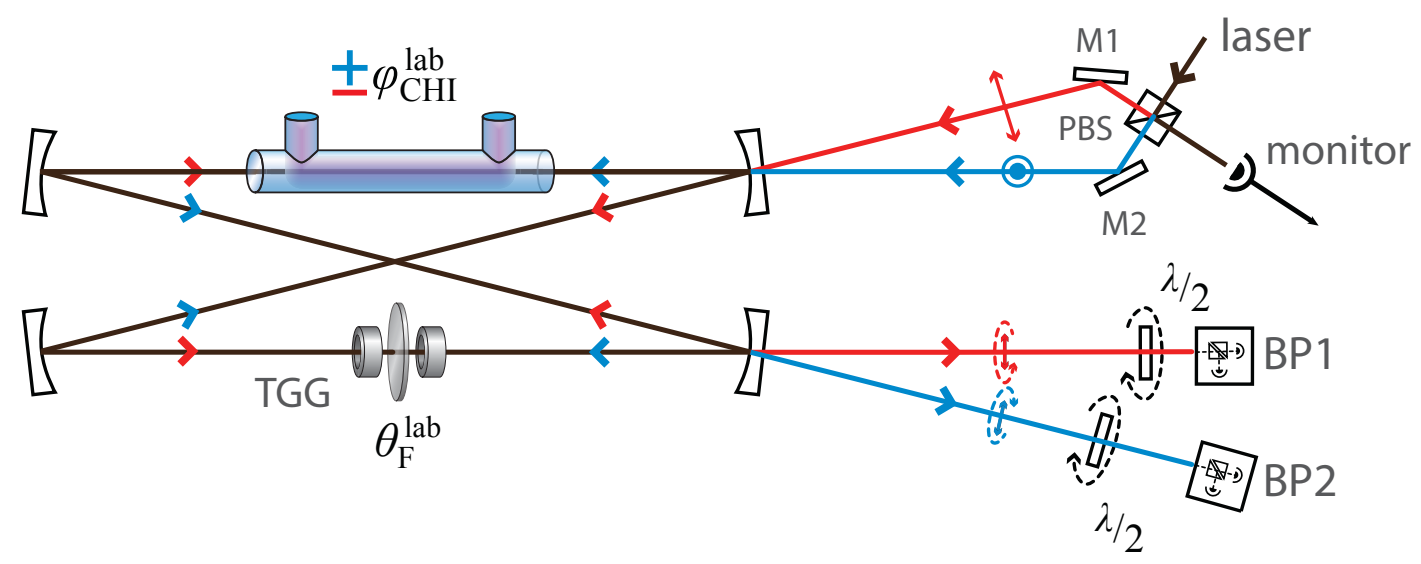
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Chiral Cavity Ring Down

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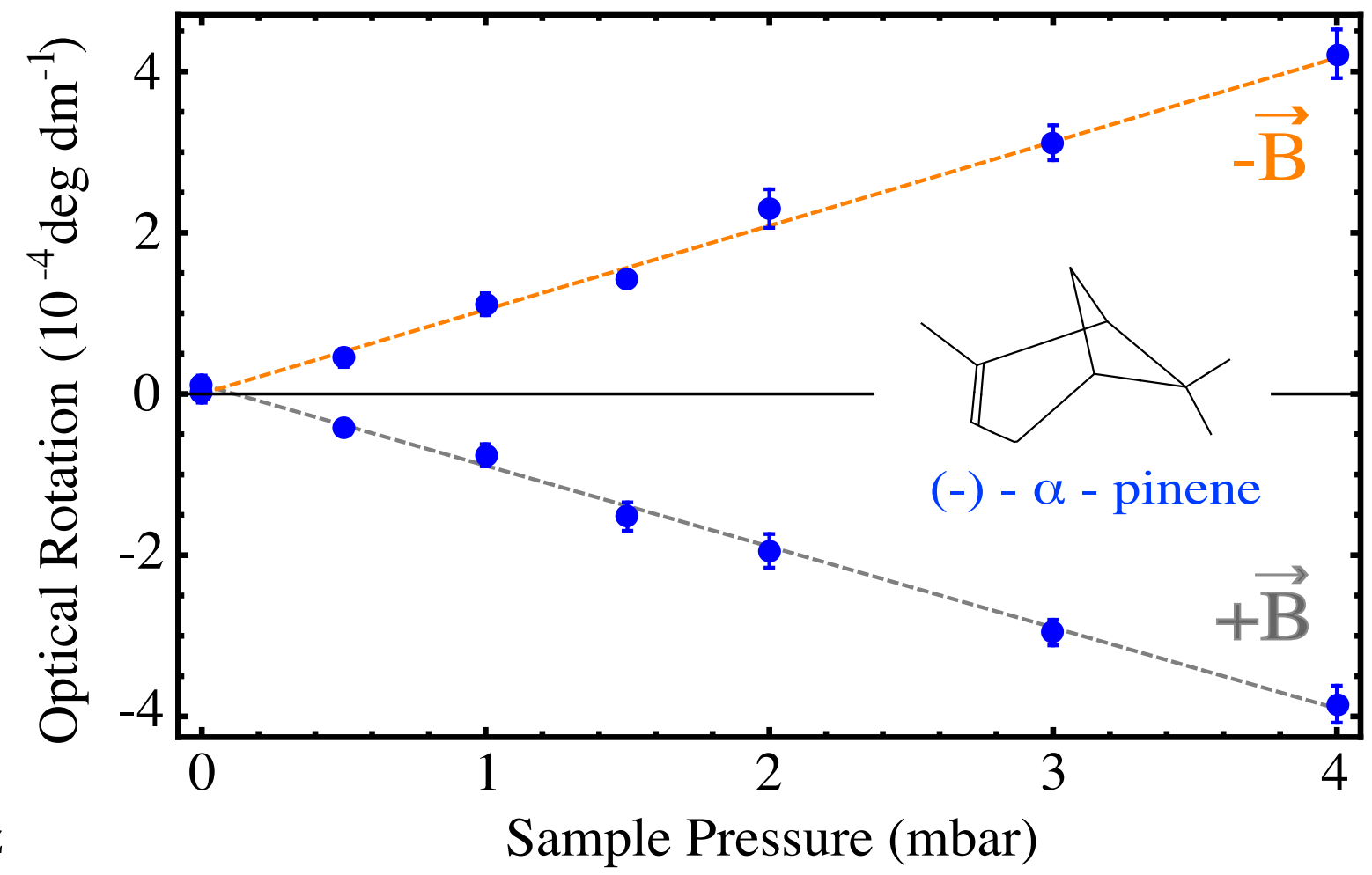


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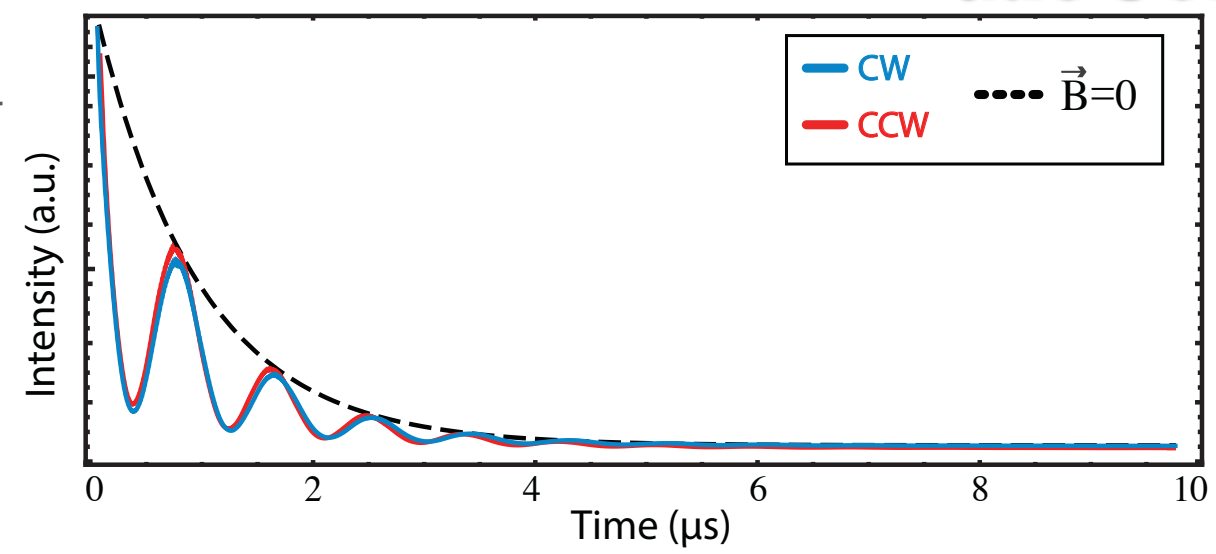
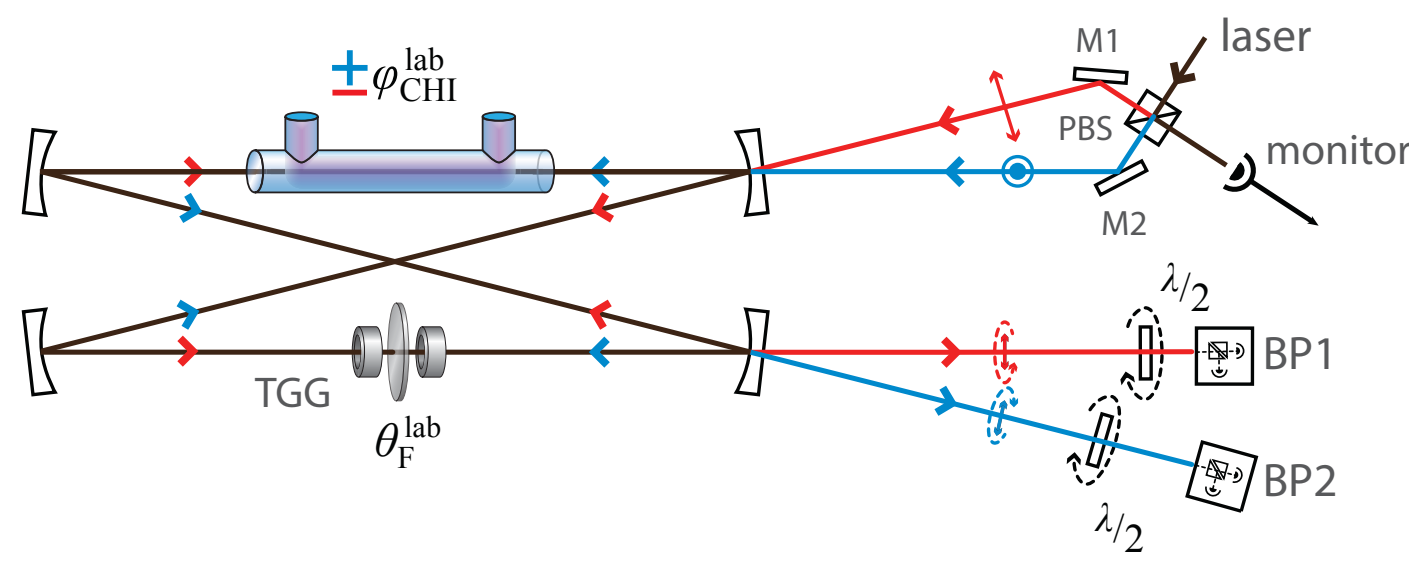
$$\Rightarrow \Delta \alpha_{\text{CW,CCW}} = \pm \phi_{\text{CHI}}$$

$f_{\text{reversal}}: 0.04 \text{ Hz}$
 $l_{\text{sample}} = 7.5 \text{ dm}$



Chiral Cavity Ring Down

Experiment Gas Cell

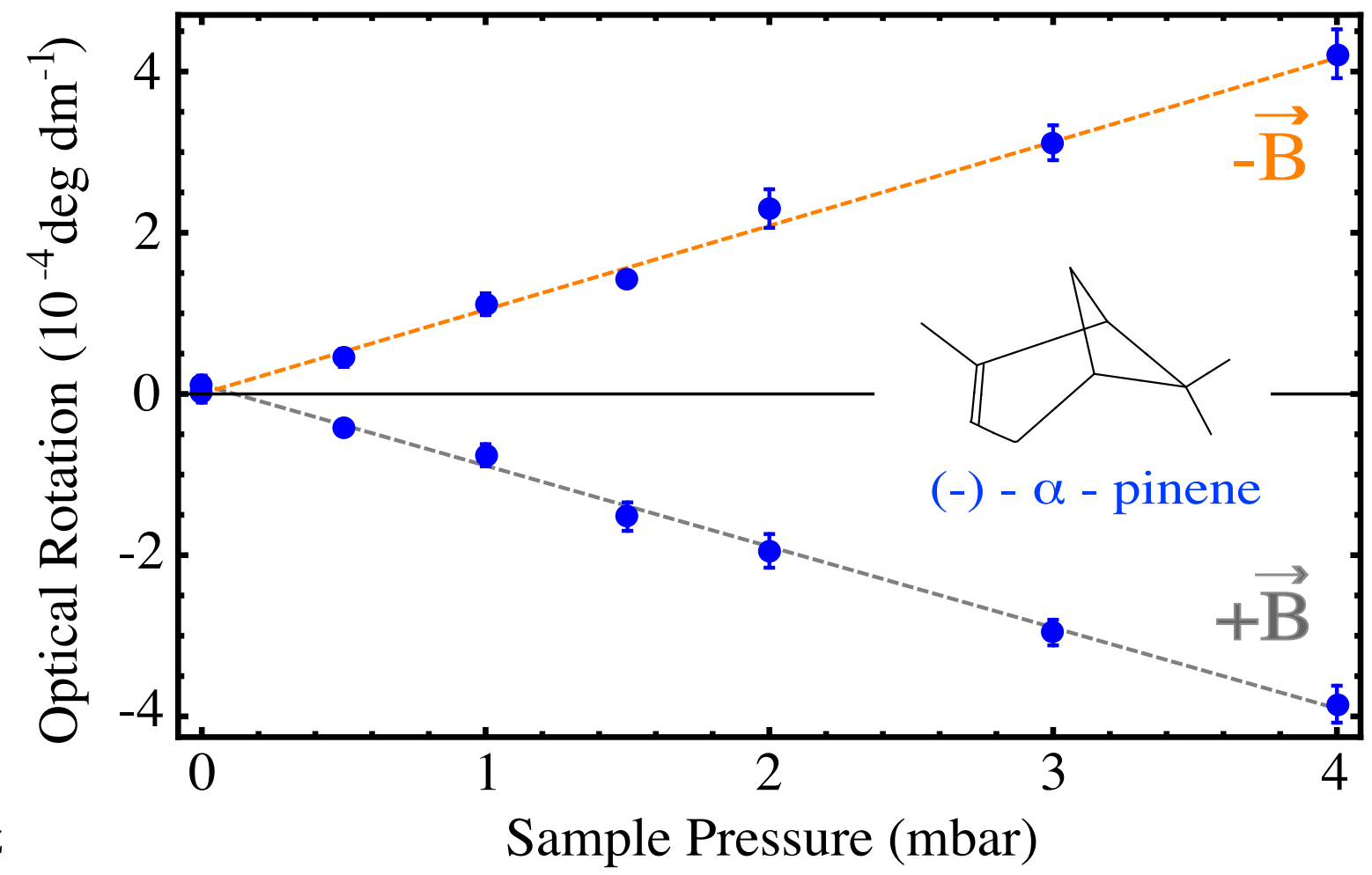


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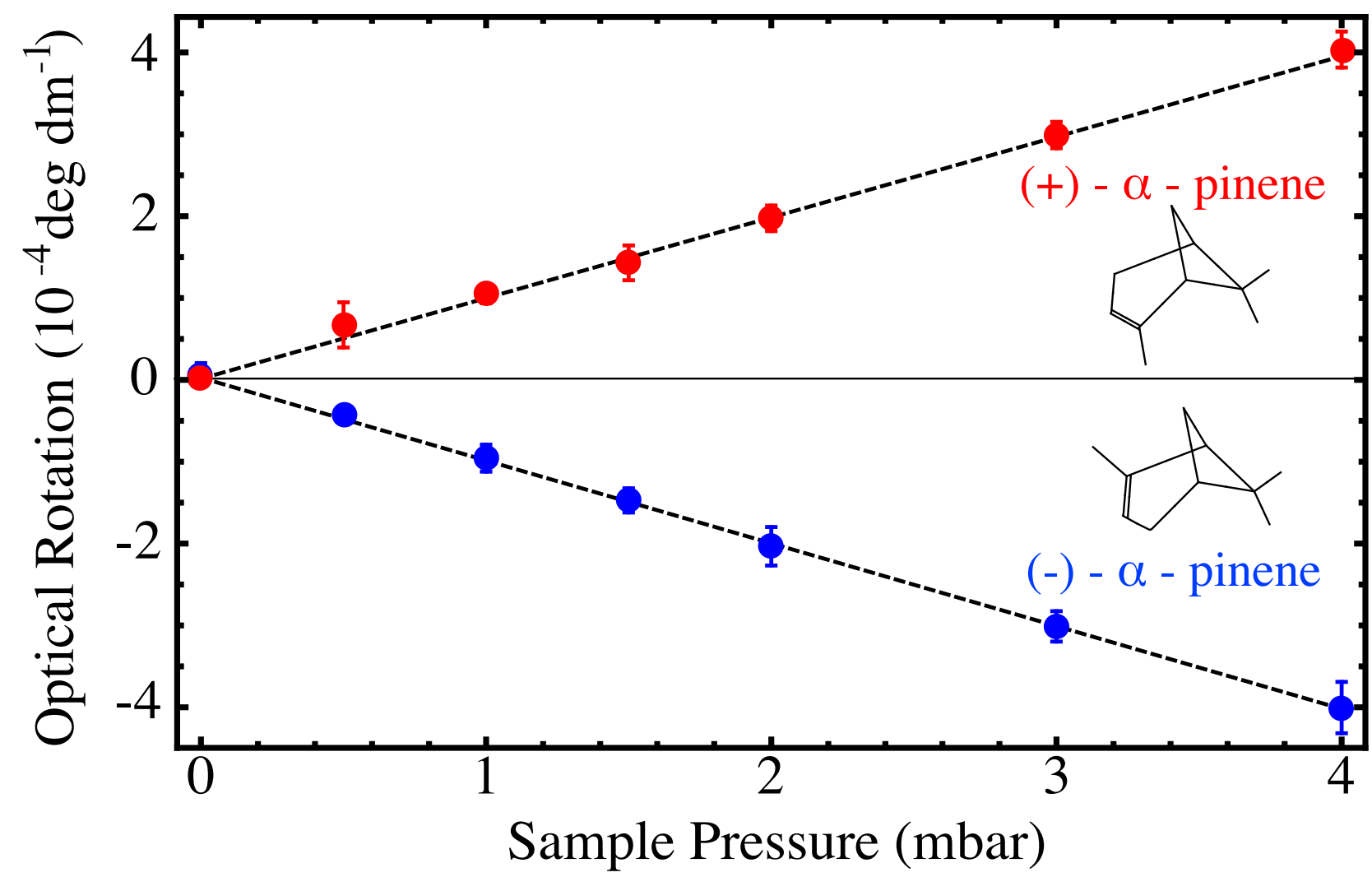
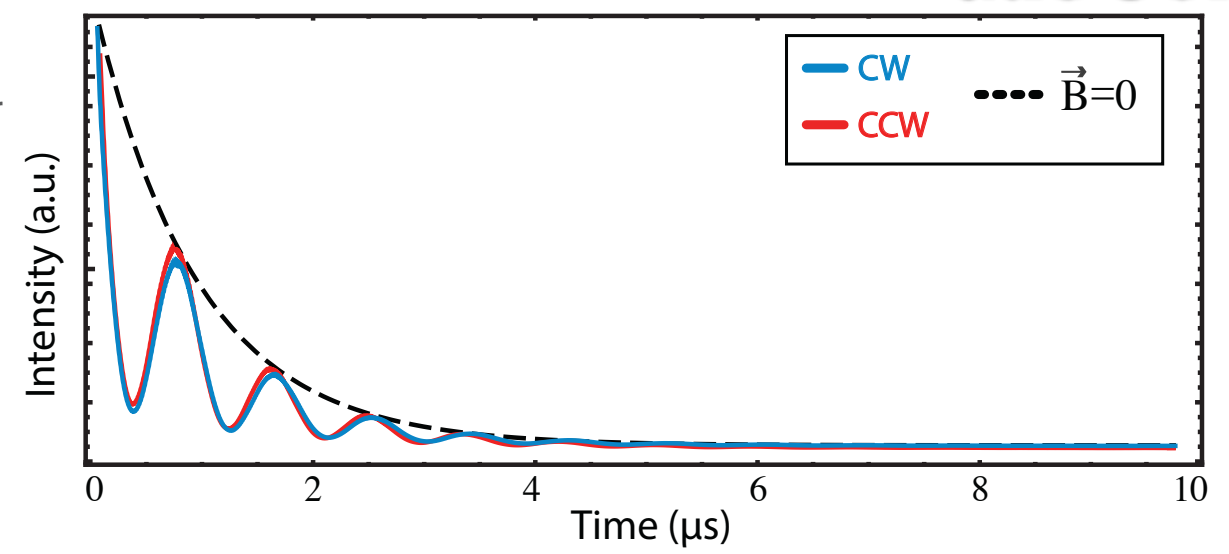
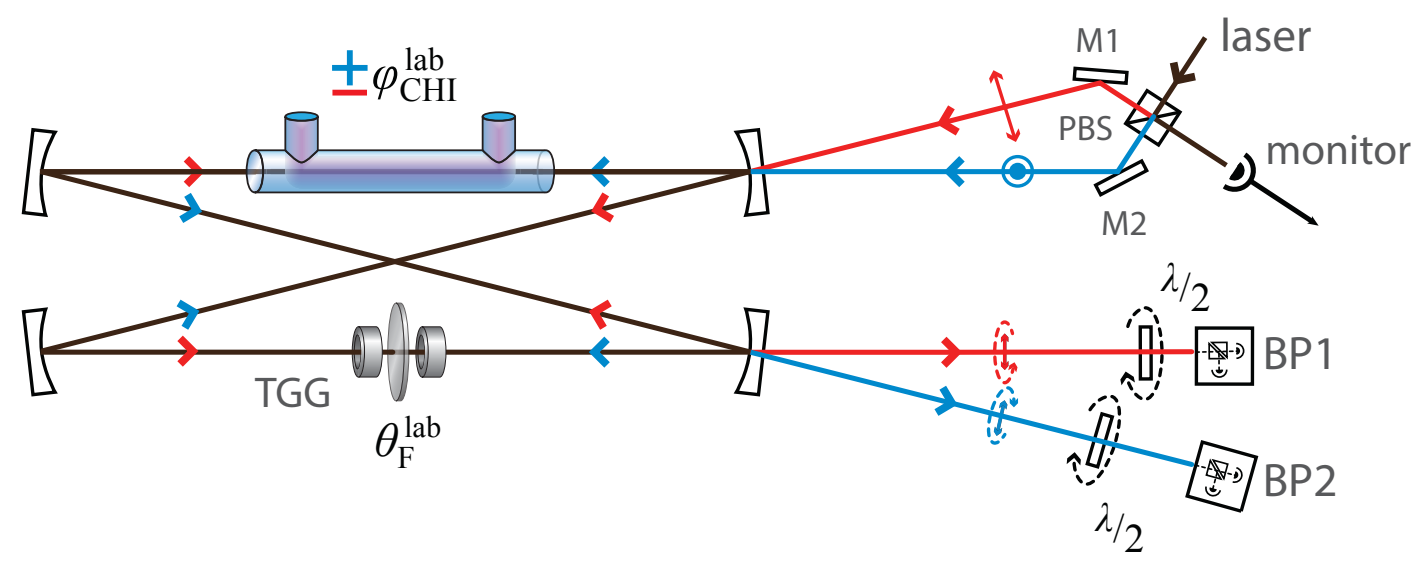
$$\Rightarrow \Delta\omega(\pm B)$$

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Chiral Cavity Ring Down

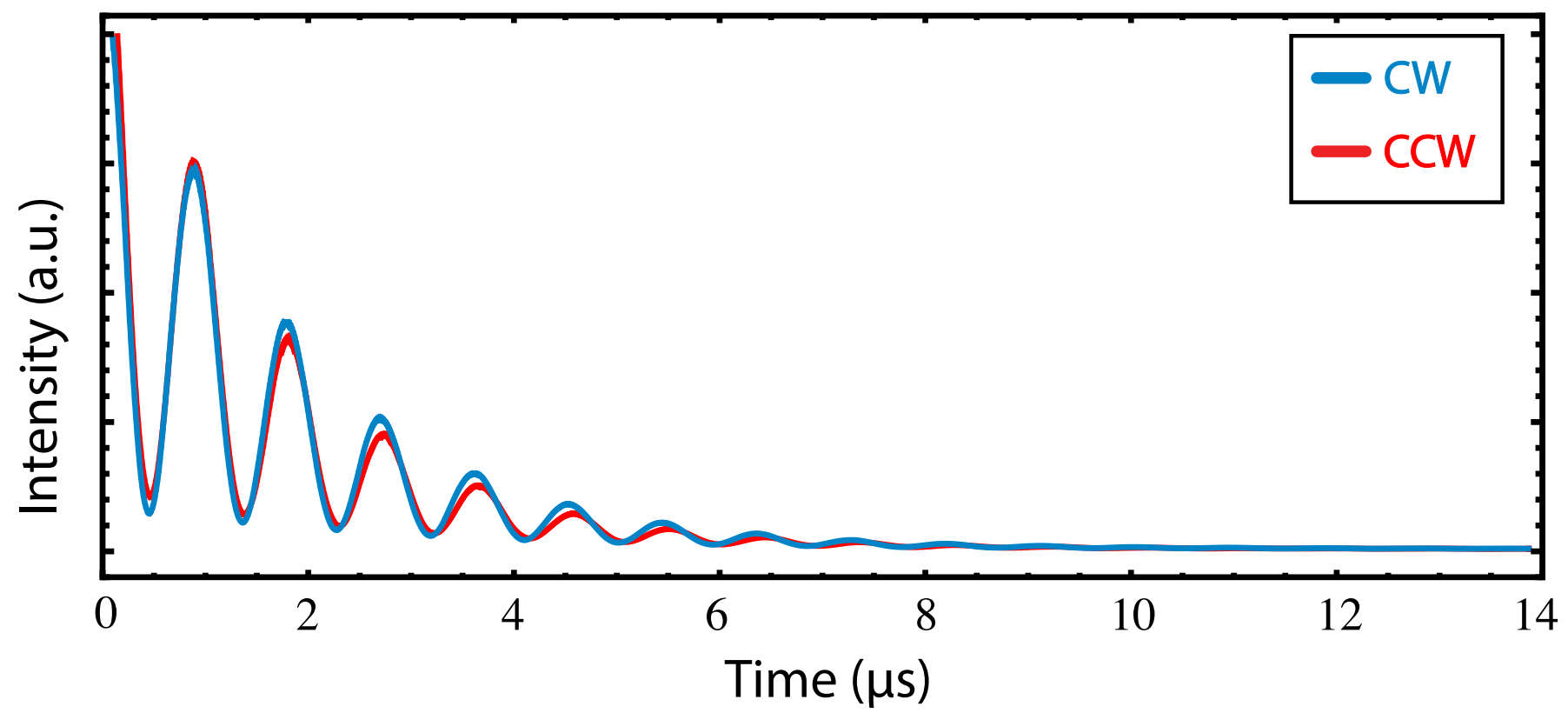
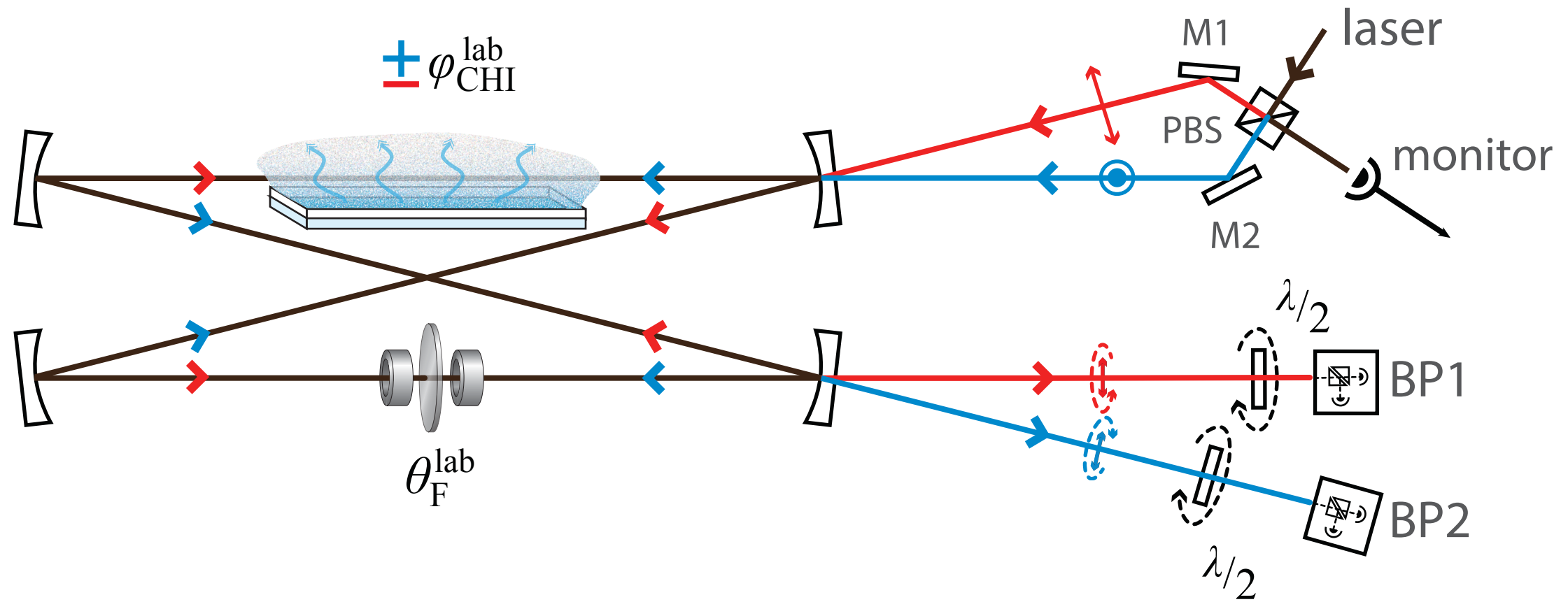
Experiment Gas Cell



different
enantiomers
of α -pinene

Chiral Cavity Ring Down

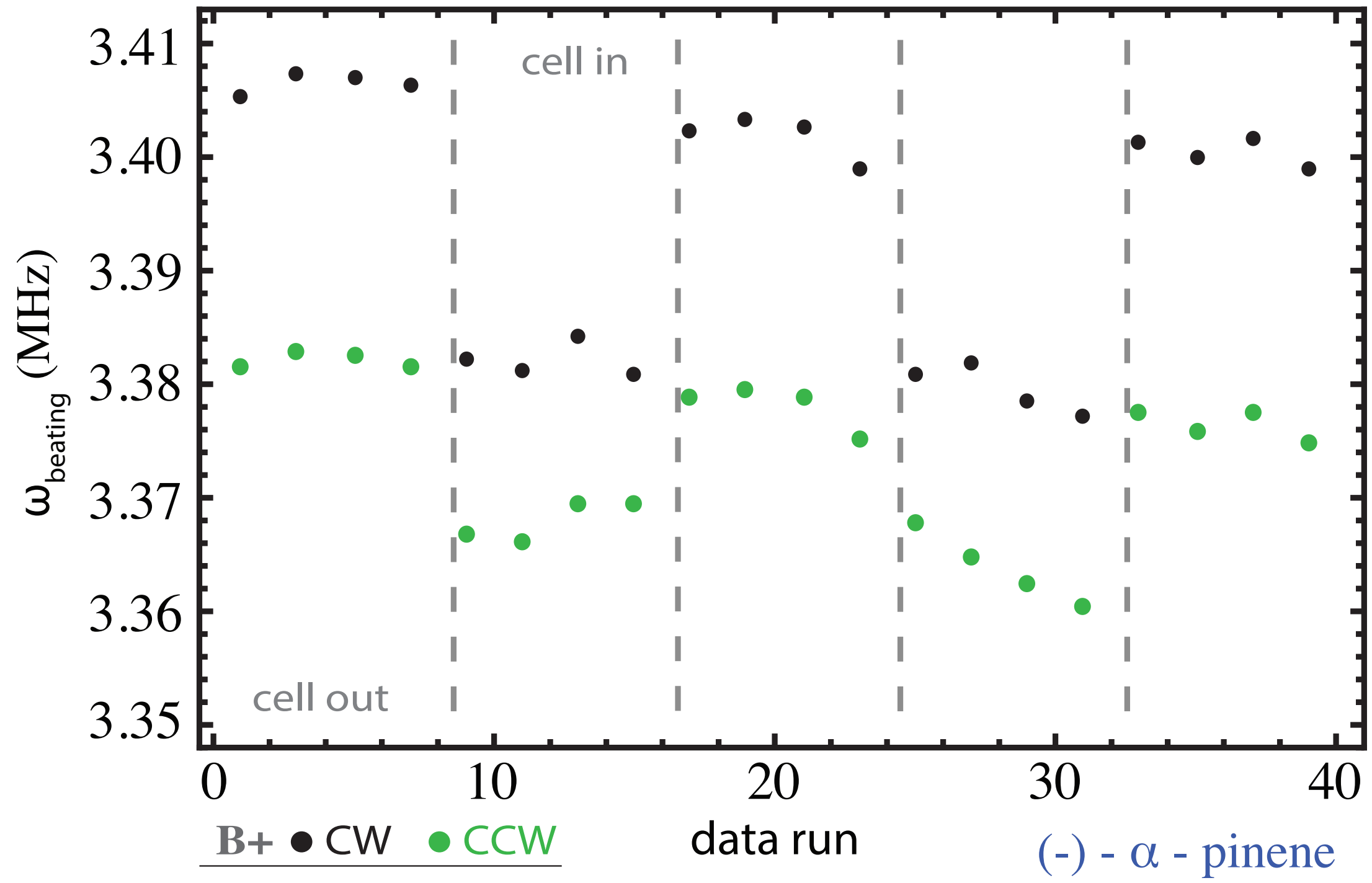
Experiment
Open air



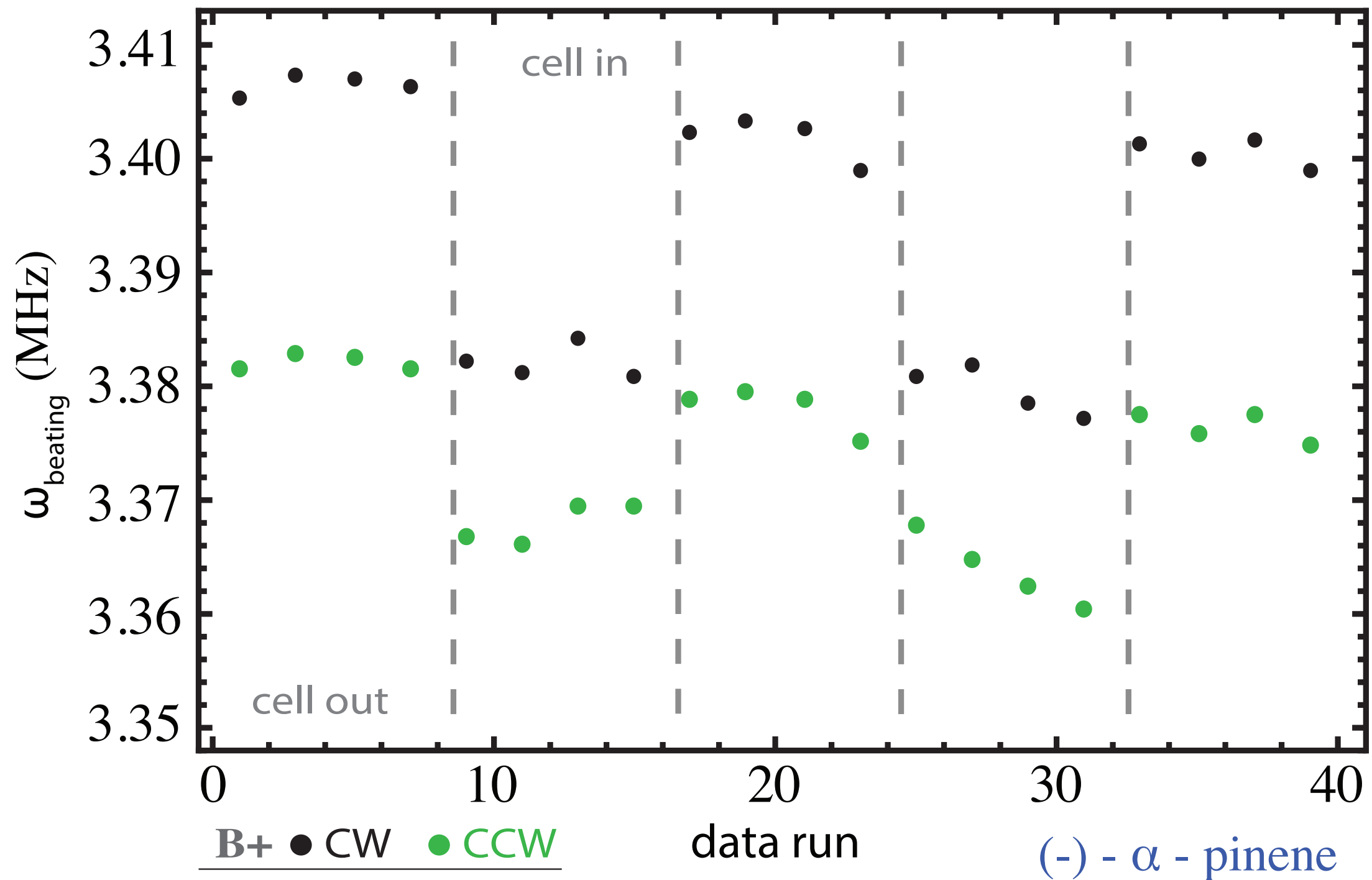
Chiral Cavity Ring Down

Experiment
Open air

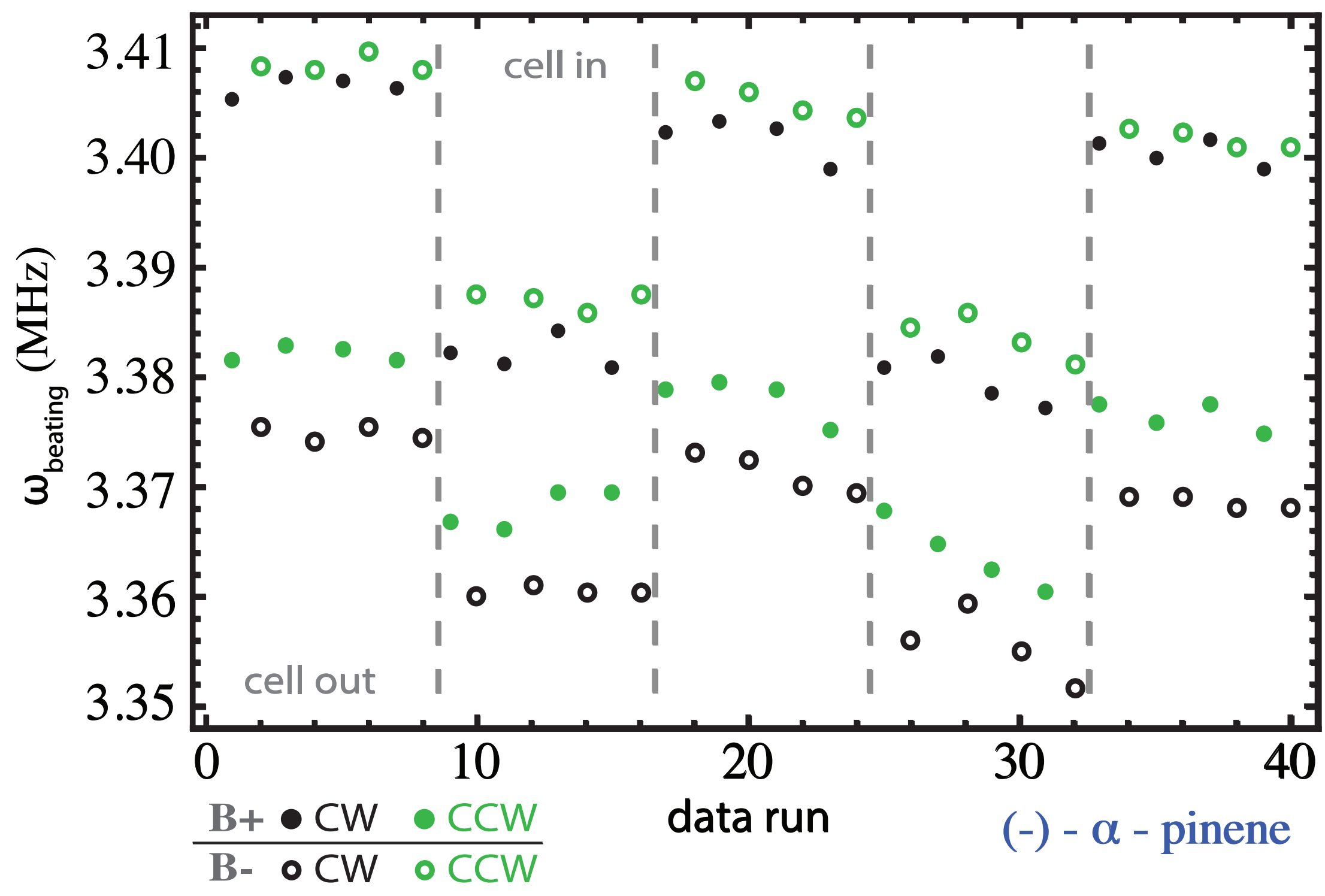
Raw Data:



Raw Data: **Single-channel signal gives the wrong answer !**

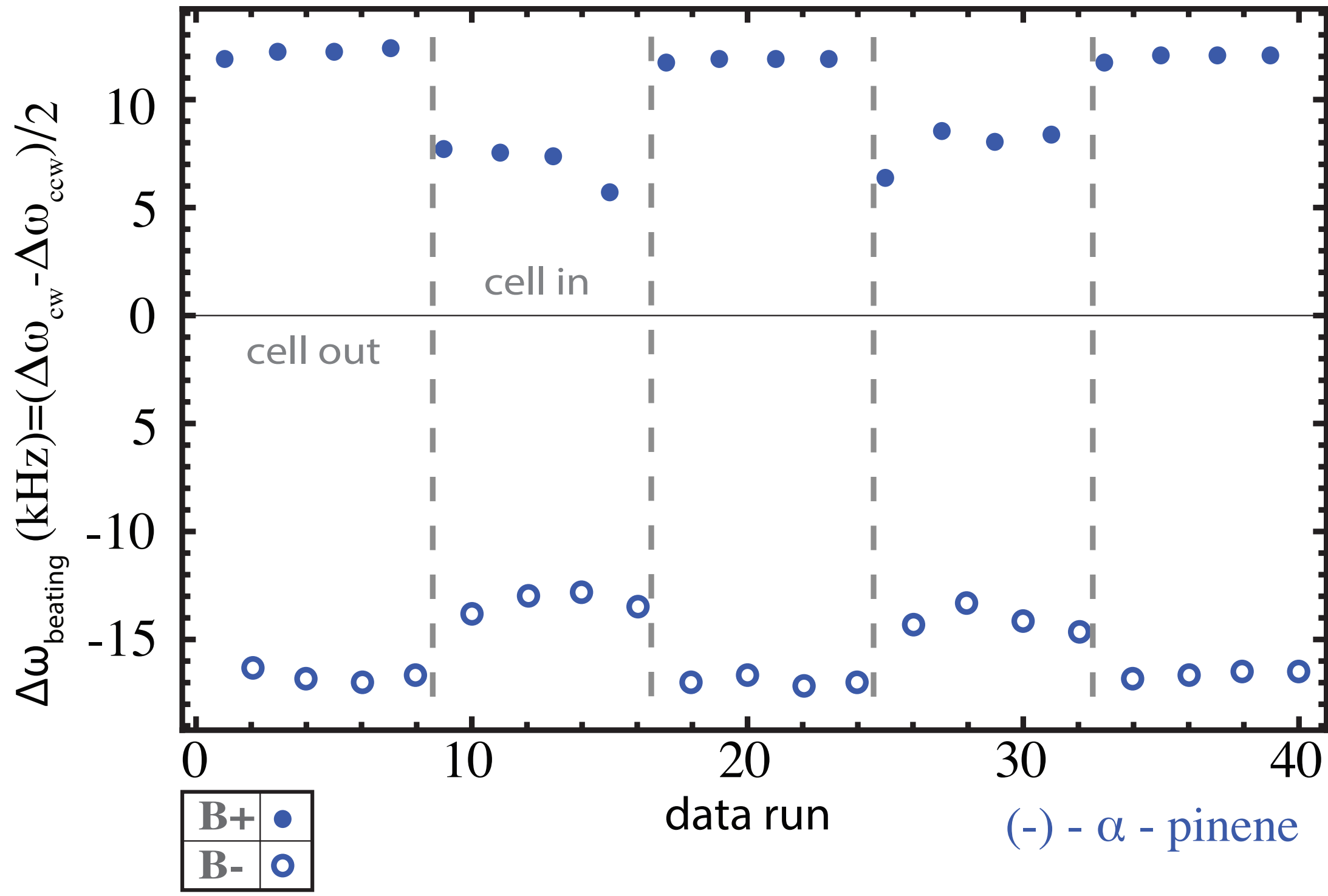


Raw Data: **Single-channel signal gives the wrong answer !**



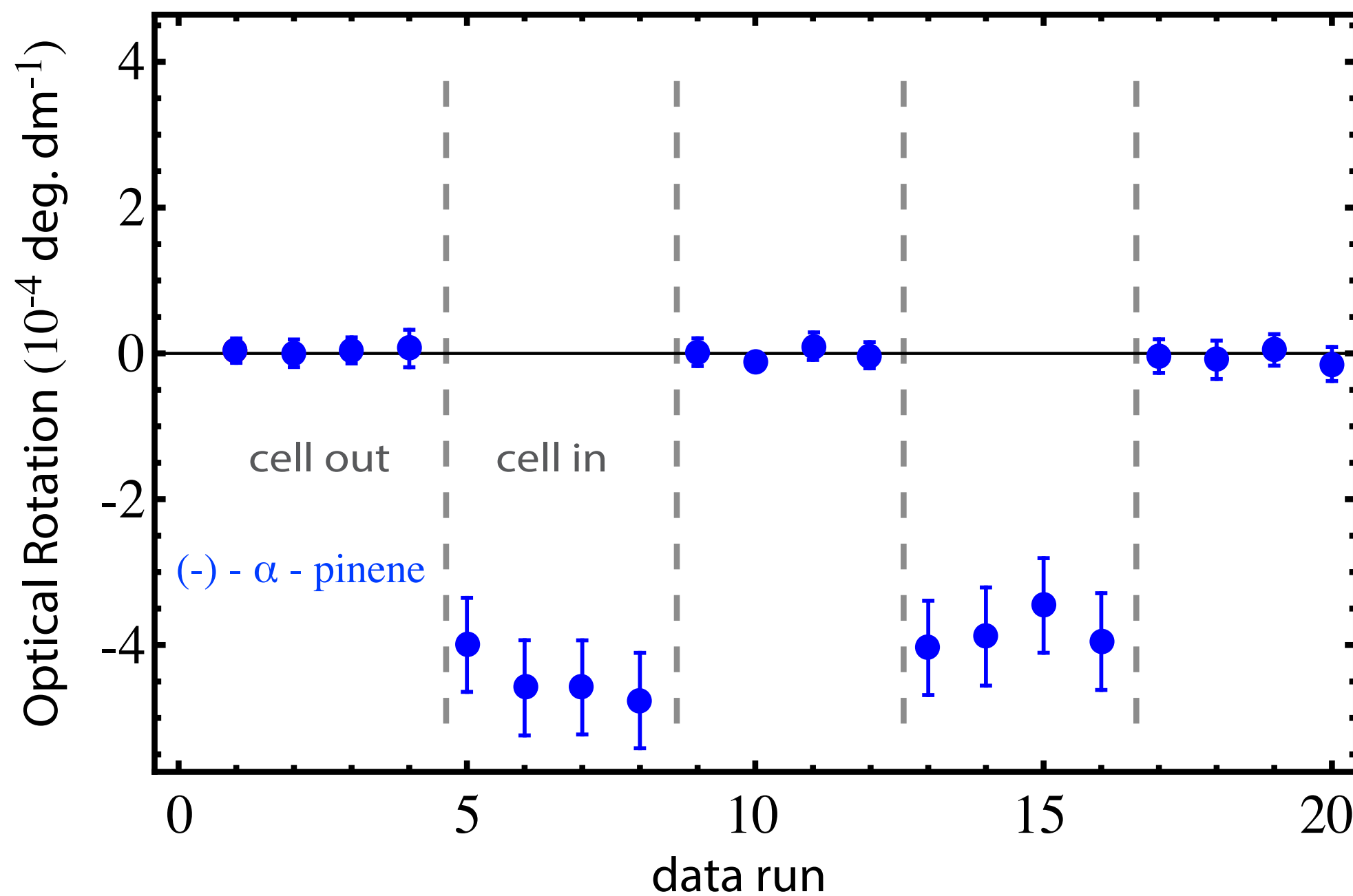
Chiral Cavity Ring Down

Experiment
Open air



Chiral Cavity Ring Down

Experiment
Open air

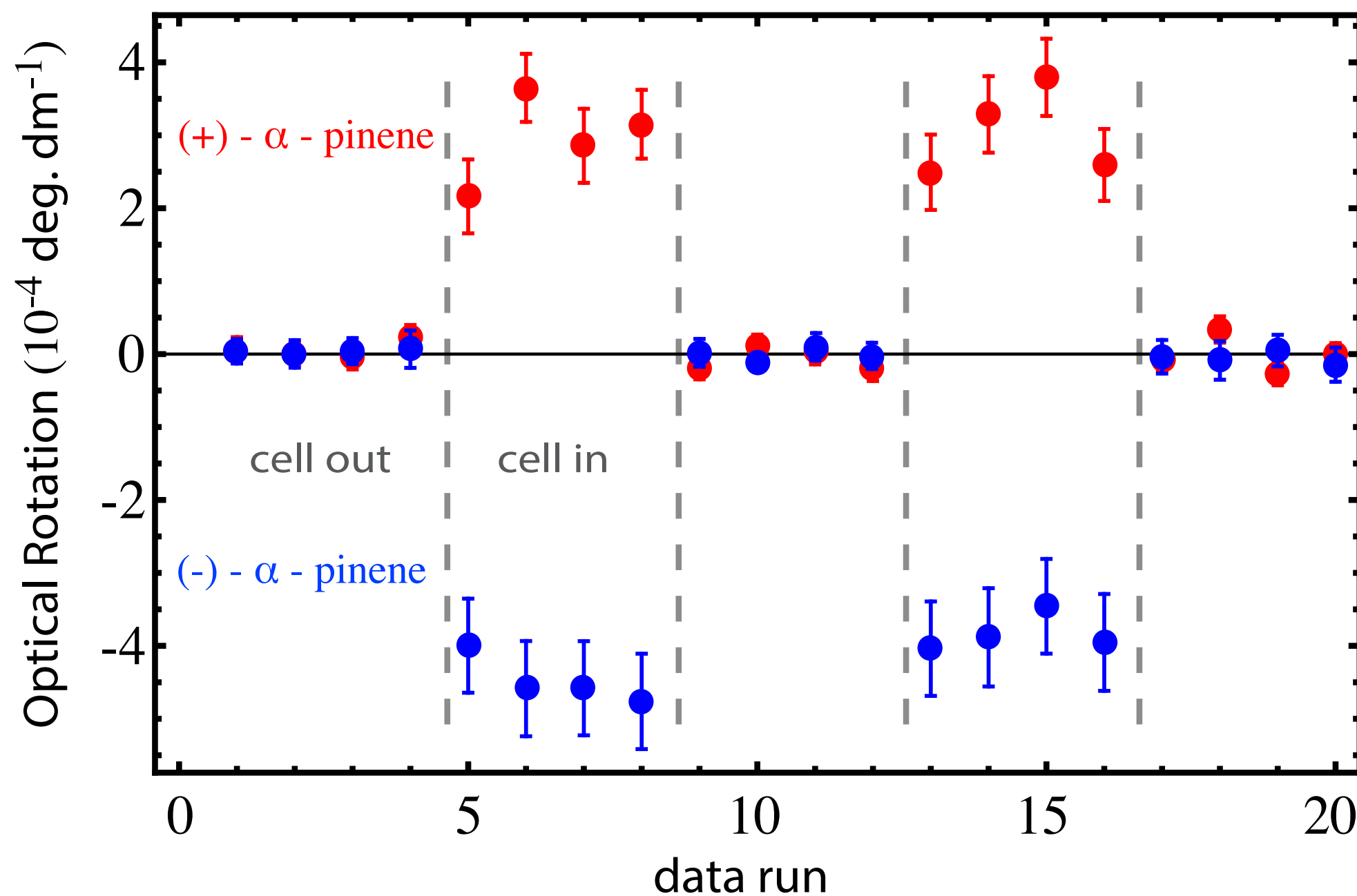


$V_{\text{sample}} \sim 4\text{mL}$

$$\Delta\alpha(+B) - \Delta\alpha(-B) = 4\phi_{\text{CHI}}$$

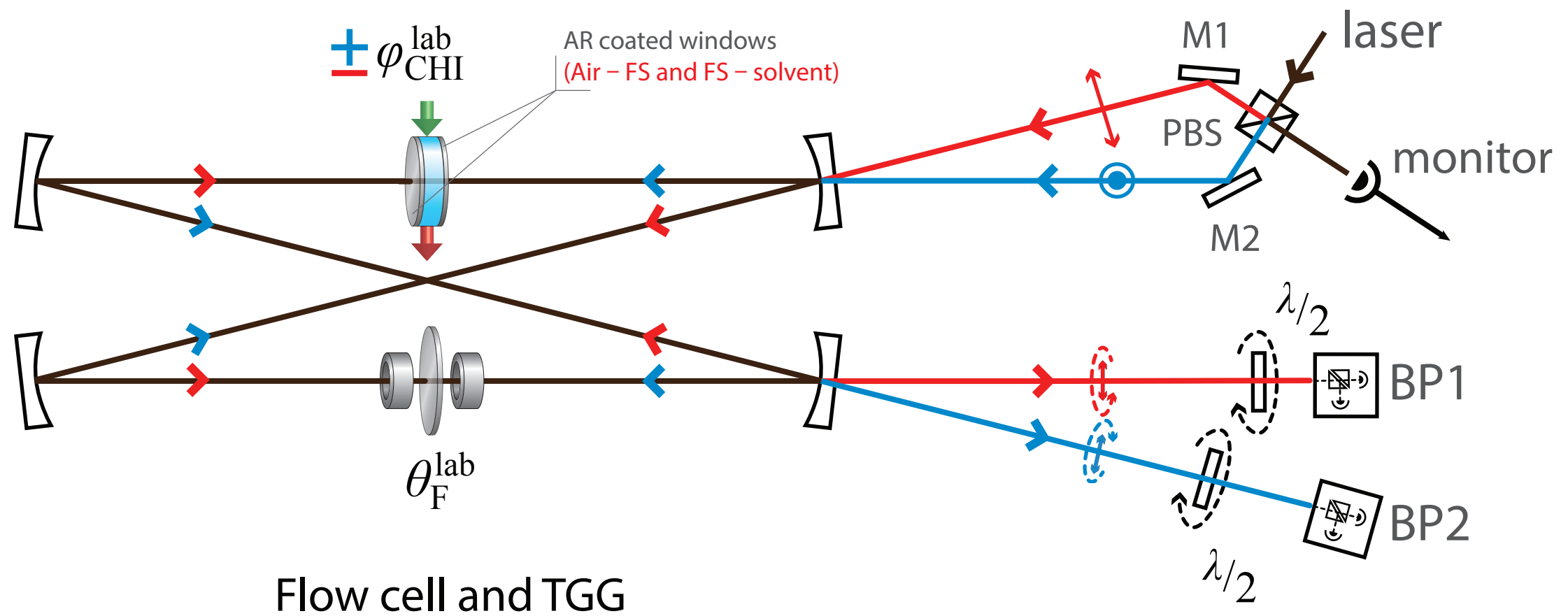
Chiral Cavity Ring Down

Experiment
Open air



$V_{\text{sample}} \sim 4\text{mL}$

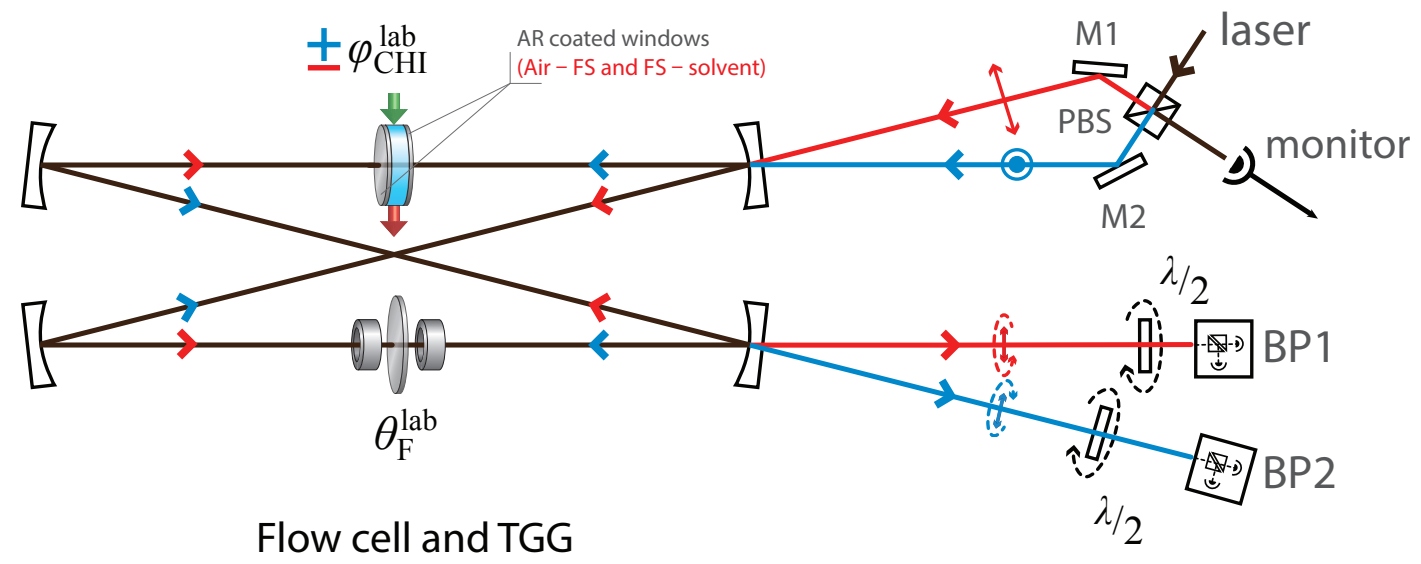
$$\Delta\alpha(+B) - \Delta\alpha(-B) = 4\phi_{\text{CHI}}$$



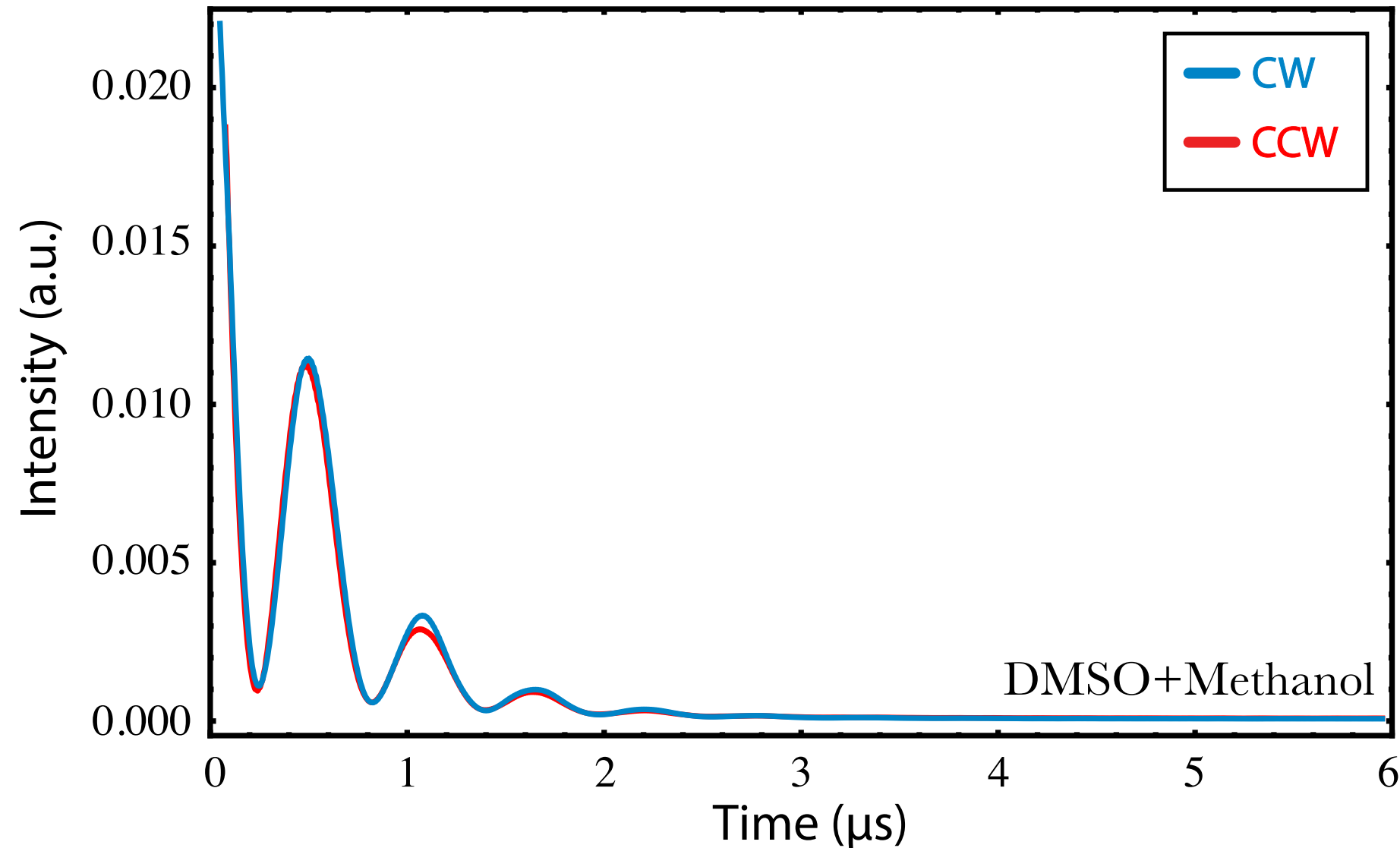
Chirality Measurements in Liquids

Chiral Cavity Ring Down

Experiment
Liquid

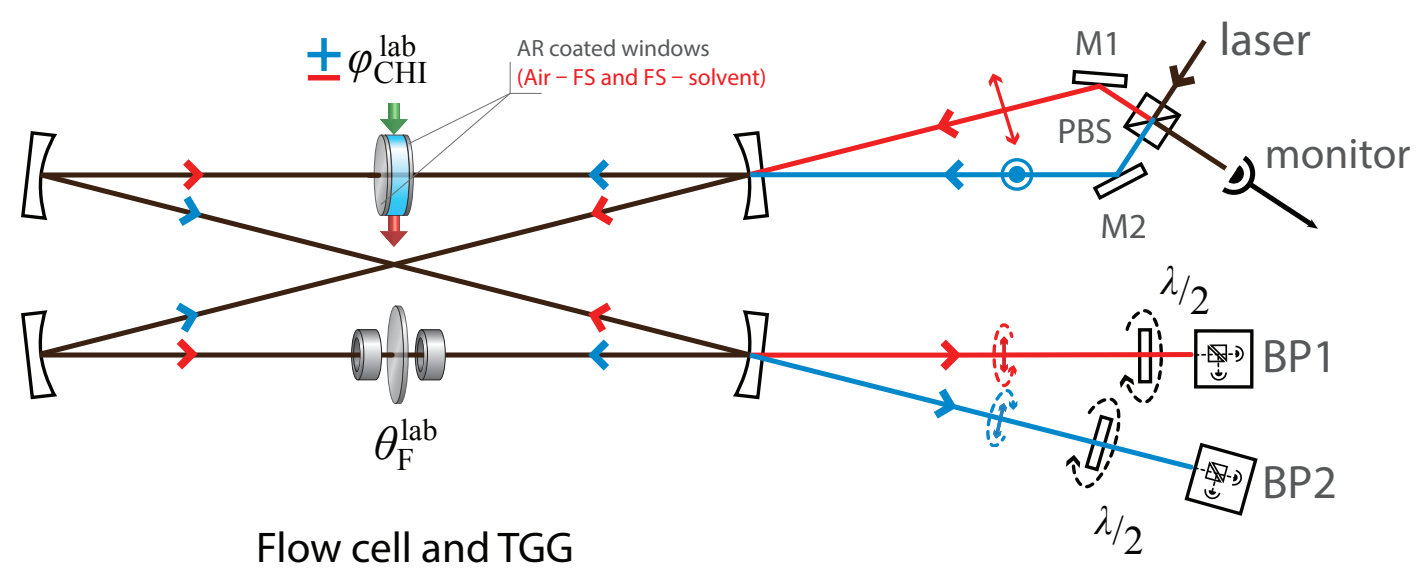


$d_{cell}=2.6mm$
 $V_{cell}\sim 200\mu L$

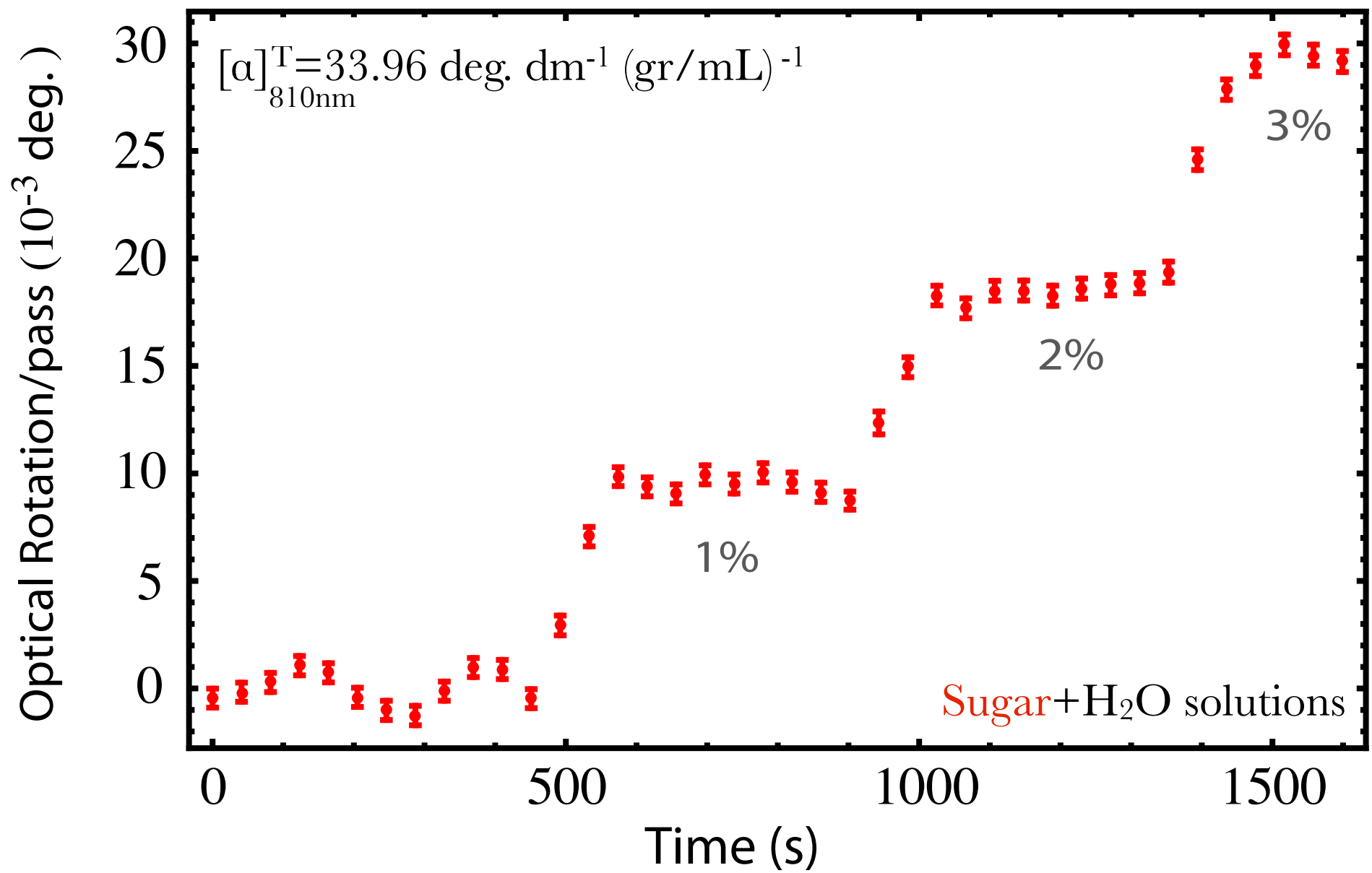


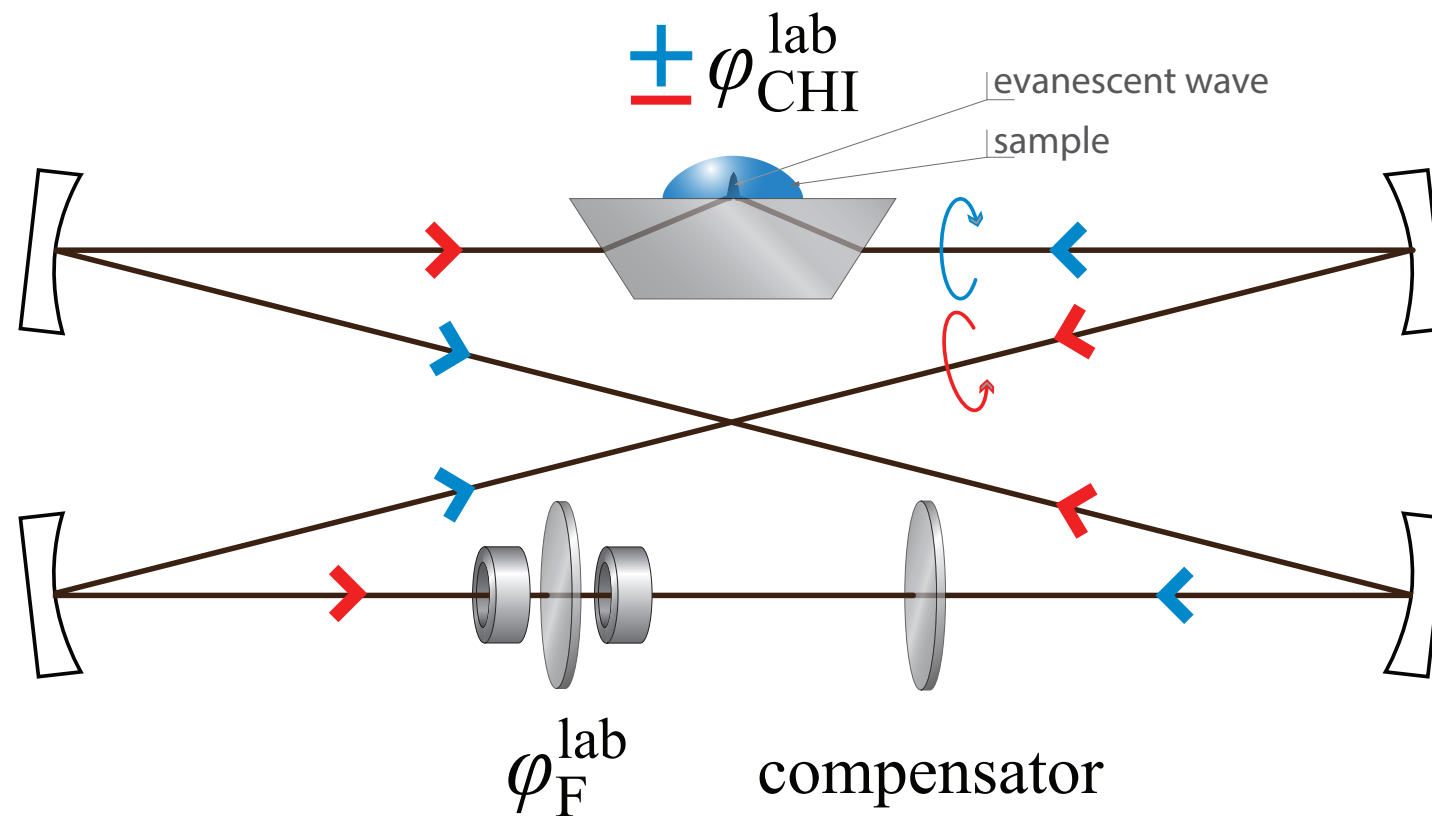
Chiral Cavity Ring Down

Experiment
Liquid



$d_{cell}=2.6mm$
 $V_{cell}\sim 200\mu L$



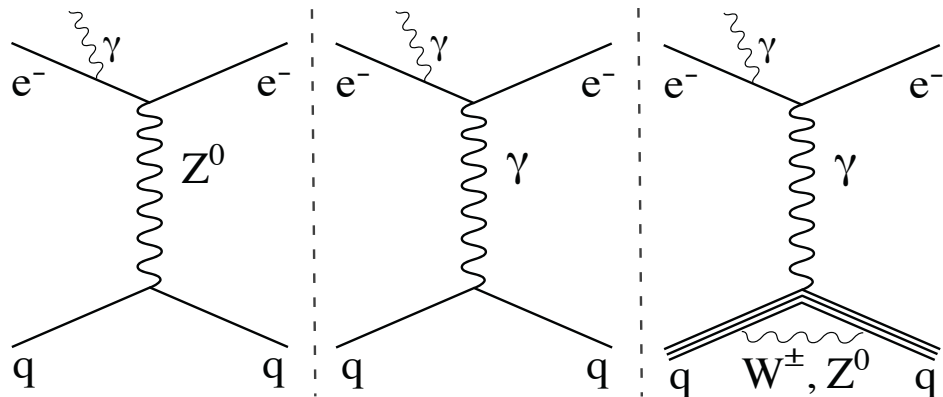
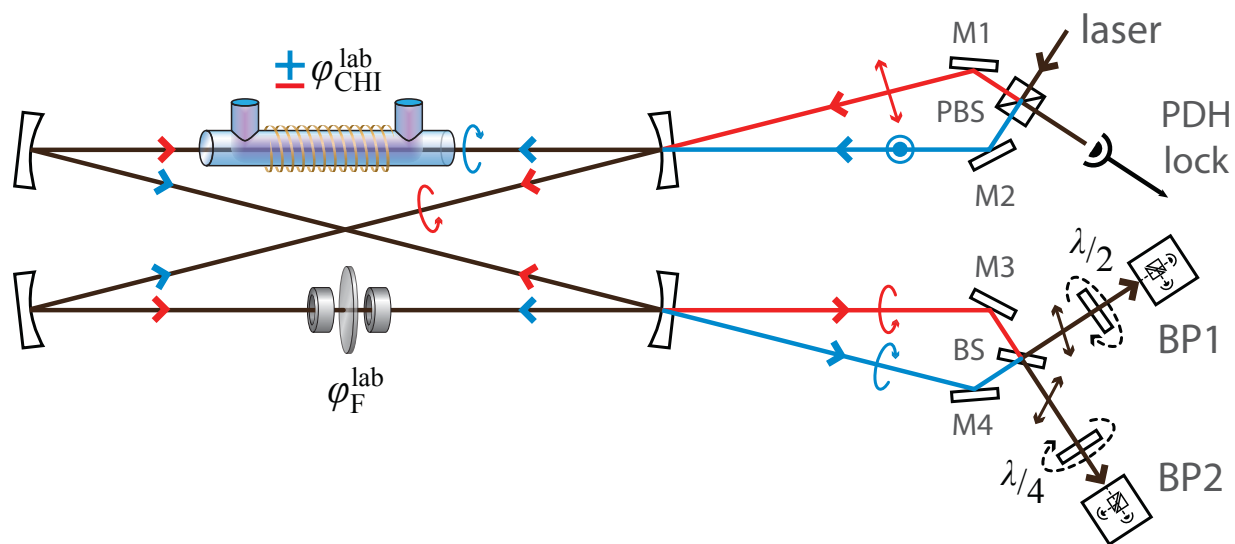


**future
work**

TIR prism, TGG and compensator

Evanescent-wave chirality measurements

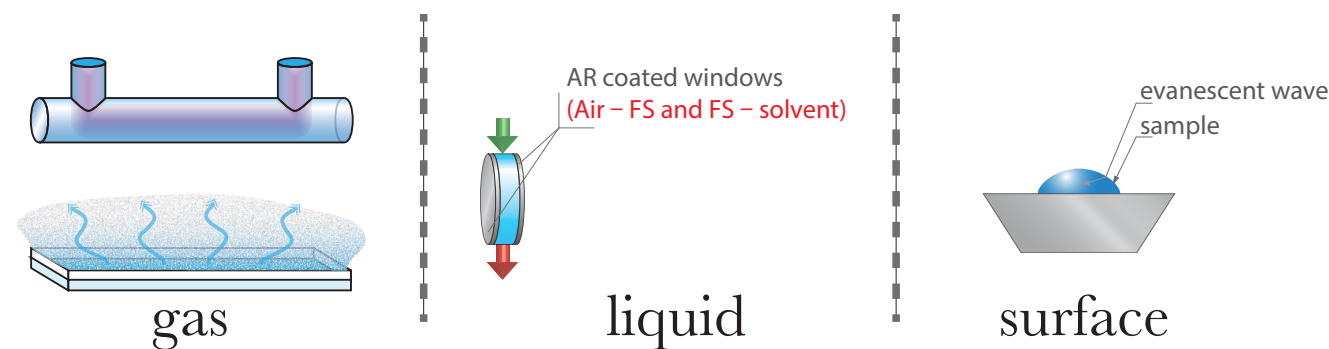
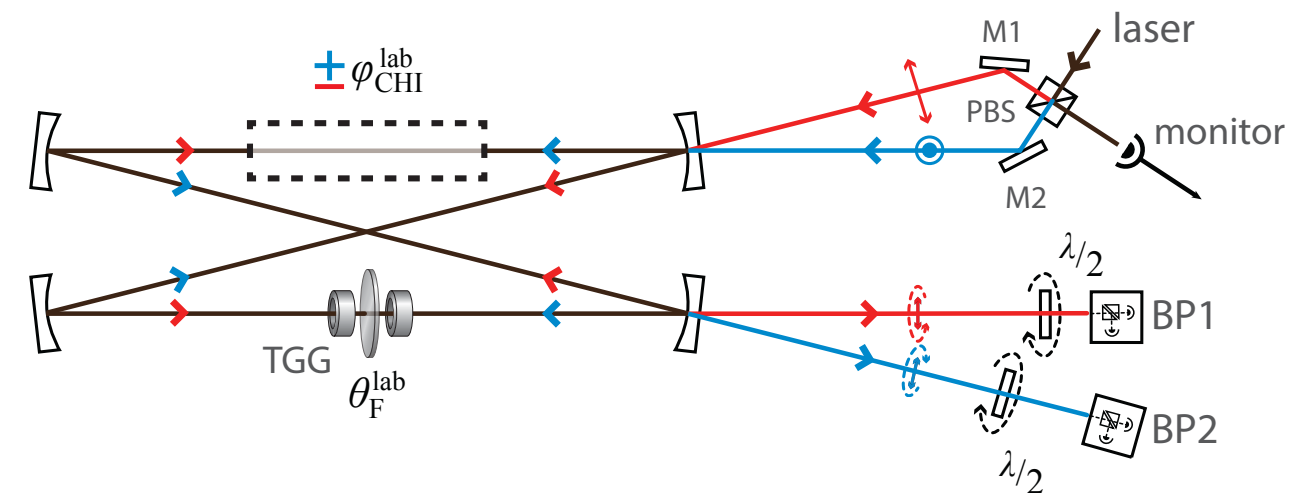
Parity Violation in Hg, Xe, I & Cs



Future goal:

- cw laser source / locked cavity
- fast reversals (100-1kHz)
- sensitivity \sim shot noise (< 1 nrad)

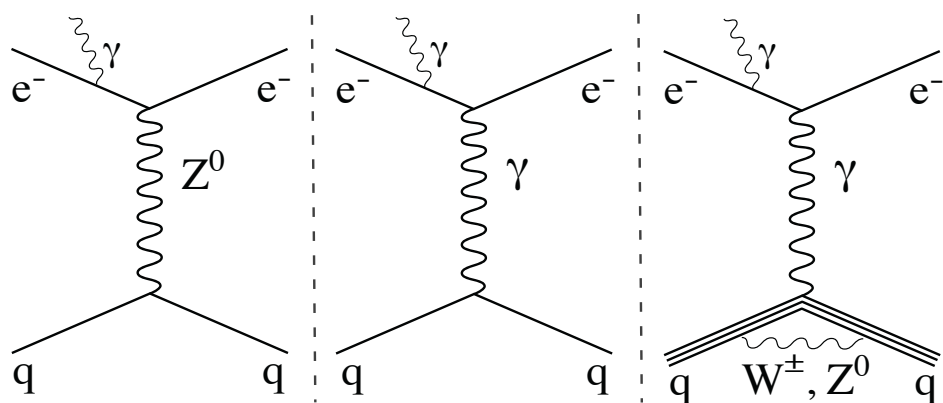
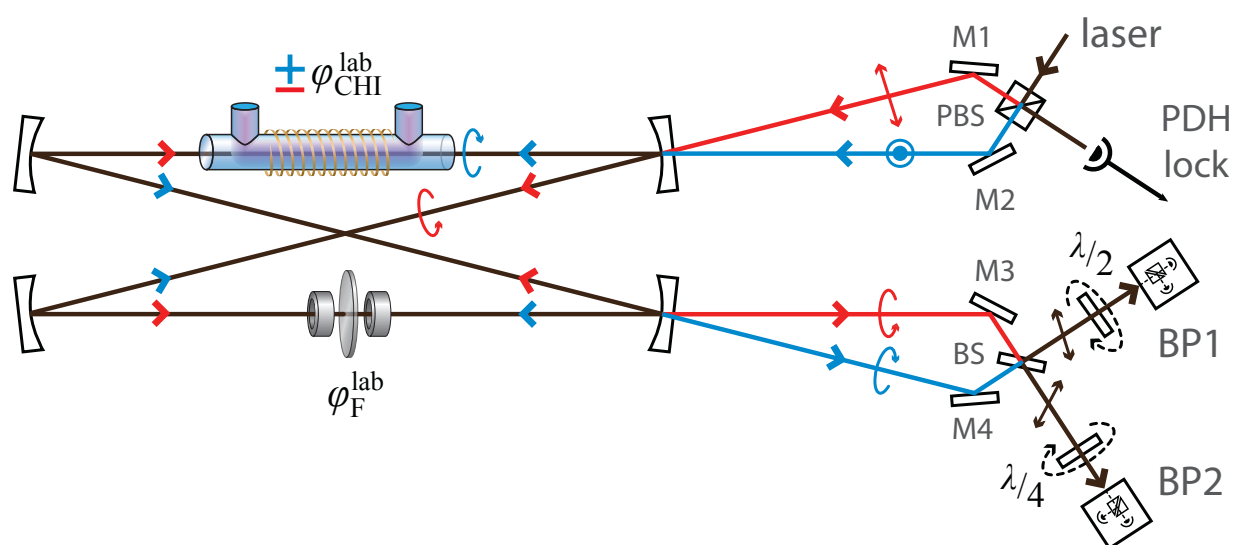
Chiral Cavity Ring Down measurements of chirality in gases and liquids



Present Status:

- pulsed laser source
- long acquisition times / slow reversals
- sensitivity $\sim 1 \mu\text{rad}$

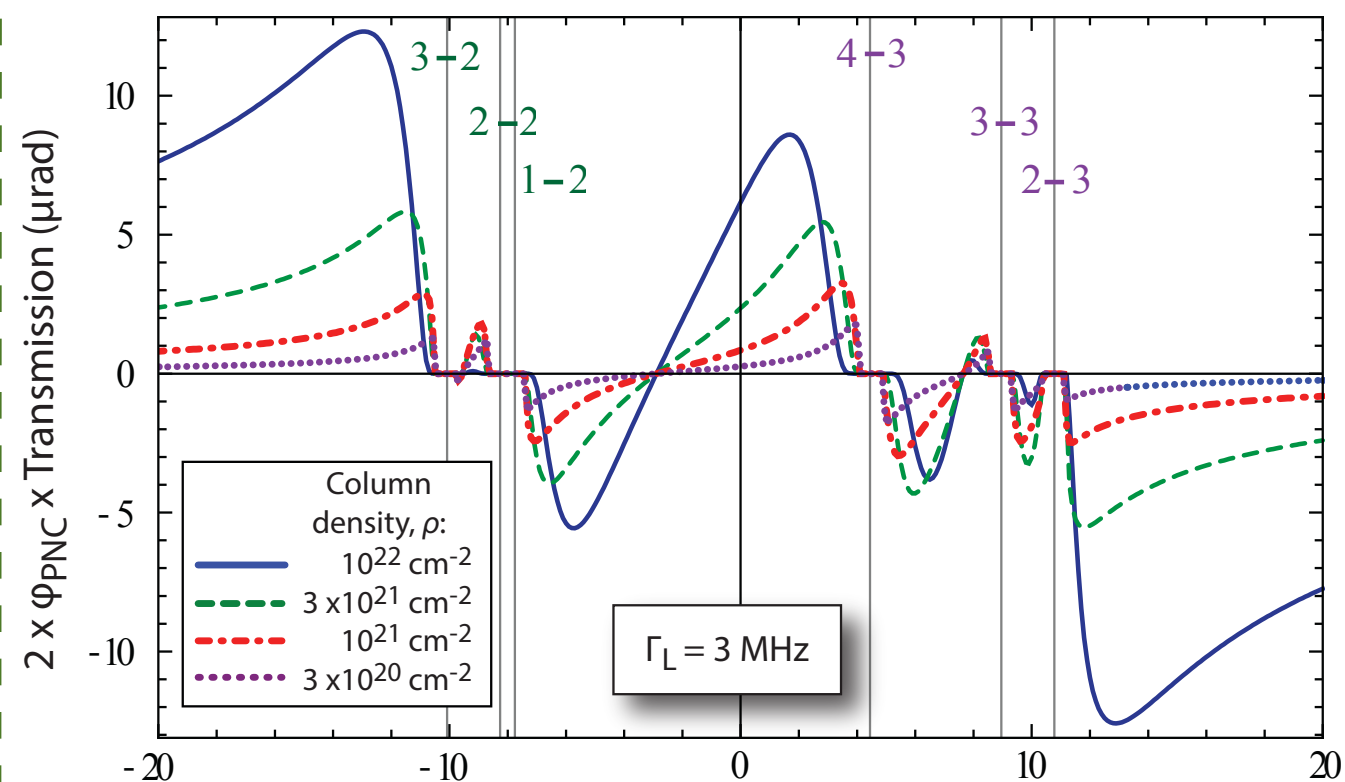
Parity Violation in Hg, Xe, I & Cs



Future goal:

- cw laser source / locked cavity
- fast reversals (100-1kHz)
- sensitivity \sim shot noise (< 1 nrad)

Iodine PNC optical rotation signal





European Union
European Social Fund



MINISTRY OF EDUCATION & RELIGIOUS AFFAIRS, CULTURE & SPORTS
MANAGING AUTHORITY

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W. von Klitzing



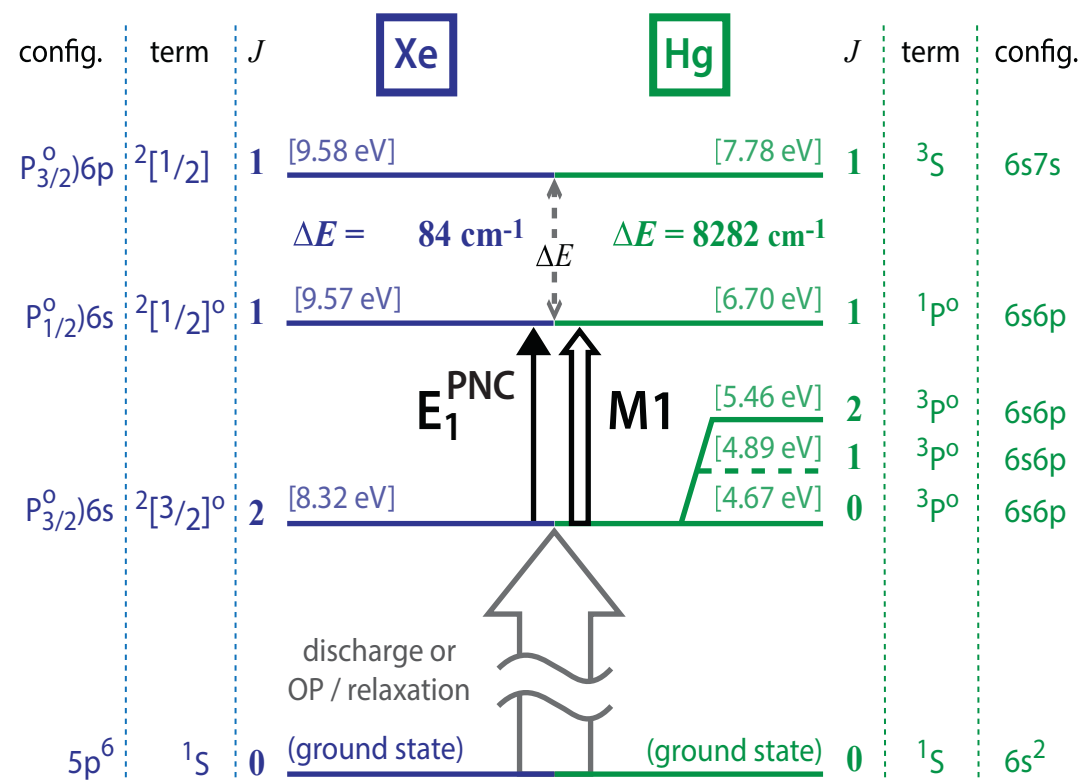
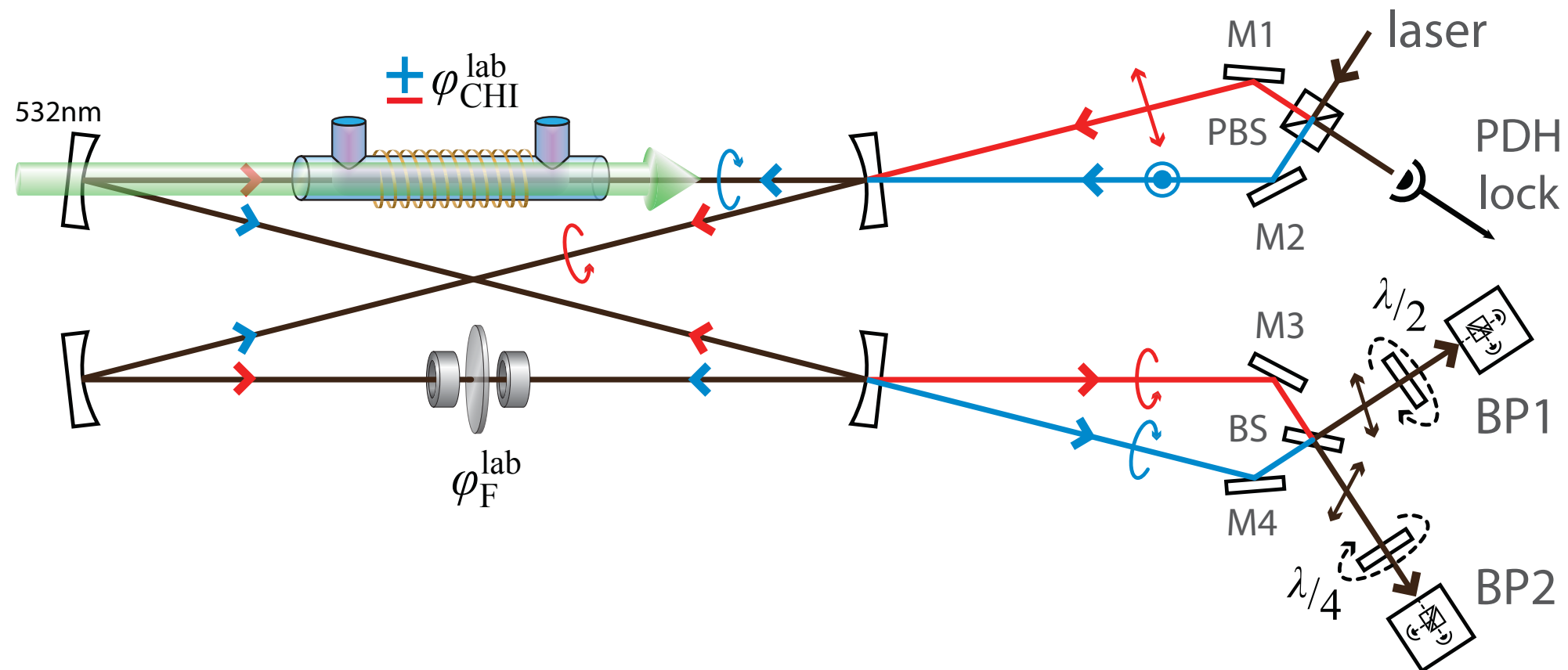
TABLE I. Review of recent experimental results concerning small birefringence measurements in gases. The reported γ_n is the noise equivalent birefringence at the detection frequency, while δn corresponds to the smallest measured birefringence value inferred from the published data.

Year	Group	Effect	Technique	γ_n ($1/\sqrt{\text{Hz}}$)	δn
2000	Tel-Aviv ^a	Kerr	Resonant cavity ellipsometer	3×10^{-15}	1×10^{-13}
2005	BMV ^b	Kerr	Resonant cavity ellipsometer	2×10^{-15}	1×10^{-15}
2009	PVLAS ^c	Cotton–Mouton	Resonant cavity ellipsometer	5×10^{-17}	1×10^{-17}
2009	Q & A ^d	Cotton–Mouton	Resonant cavity ellipsometer	1×10^{-15}	1×10^{-15}
2009	BMV ^e	Cotton–Mouton	Resonant cavity ellipsometer	2×10^{-18}	2×10^{-15}
2009	LASIM/LSP ^f	Kerr	Resonant cavity ellipsometer	8×10^{-19}	4×10^{-19}
2003	Tokyo ^g	Cotton–Mouton	Single pass ellipsometer	3×10^{-13}	2×10^{-15}
2000	JILA ^h	Sensitivity test	Frequency measurement	2×10^{-15}	1×10^{-17}
2009	This work	Sensitivity test	Frequency measurement	1×10^{-16}	2×10^{-18}

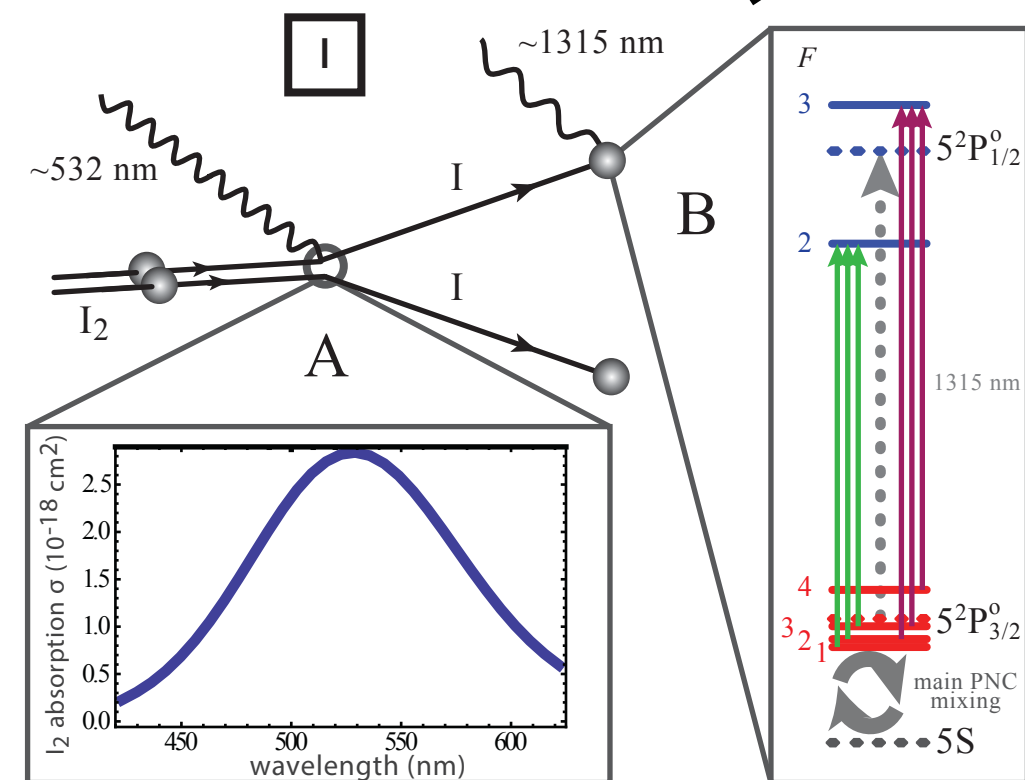
Bailly et. al. RevSciInstrum 81, 033105 (2010)

4 mirror ring cavity with counter-propagating beams

state-of-art 3×10^{-13} rad
(QED vacuum birefringence)
Durand et. al. PRA 82 (2010)



Metastable densities $\sim 10^{12} \text{ cm}^{-3}$
 (for discharge lamp pathlengths of 100cm
 column densities of $\sim 10^{14} \text{ cm}^{-2}$)



Steady state densities $\sim 10^{15}-10^{16} \text{ cm}^{-3}$
 (for pathlengths of 100cm
 column densities of $\sim 10^{17}-10^{18} \text{ cm}^{-2}$)

	Z	ΔE (cm^{-1})	Transition	λ (nm)	$M1$ (μ_B)	Isotopes with $I \neq 0$	$\text{Im}(E_1^{\text{PNC}})$ $\times 10^{-10} e\alpha_B$	\mathcal{R} $\times 10^{-8}$
I	53	53293.3	$^2\text{P}_{3/2} \rightarrow ^2\text{P}_{1/2}$	1315	1.15	^{127}I	0.335(67)	0.80(16)
Hg	80	8281.64	$^3\text{P}_0^\circ \rightarrow ^1\text{P}_1^\circ$	609	0.229	$\{^{199}\text{Hg}, ^{201}\text{Hg}\}$	3.4(2), 3.5(2)	41(2), 42(2)
			$^3\text{P}_1^\circ \rightarrow ^1\text{P}_1^\circ$	682	0.199		5.3(3), 5.4(3)	73(4), 74(4)
			$^3\text{P}_2^\circ \rightarrow ^1\text{P}_1^\circ$	997	0.272		3.7(2), 3.8(2)	37(2), 38(2)
Xe	54	84.1	$6s^2[3/2]_2^\circ \rightarrow 6s'^2[1/2]_1^\circ$	988	1.22	$\{^{129}\text{Xe}, ^{131}\text{Xe}\}$	3.16, 3.25	7.1(7), 7.3(7)

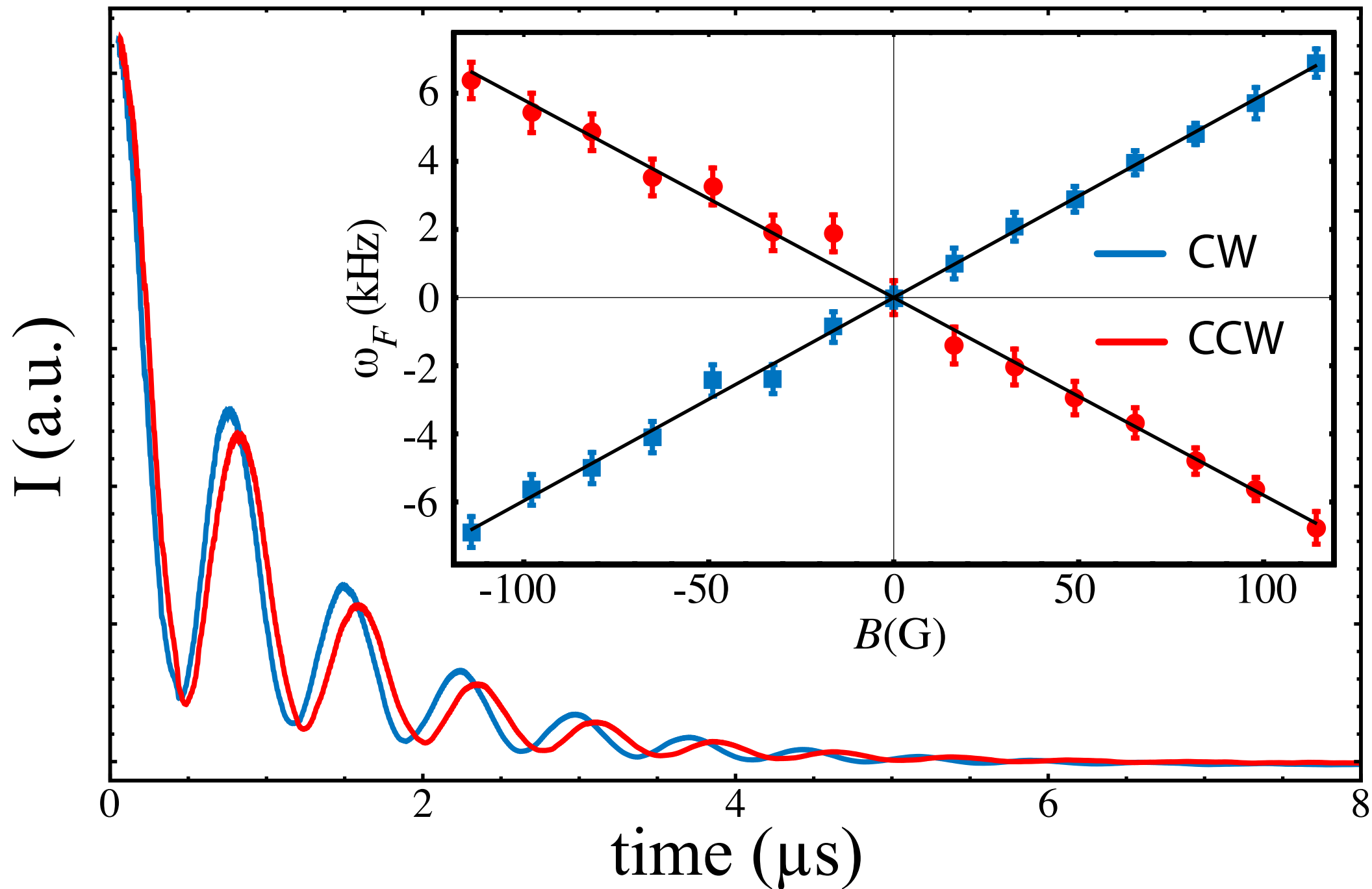
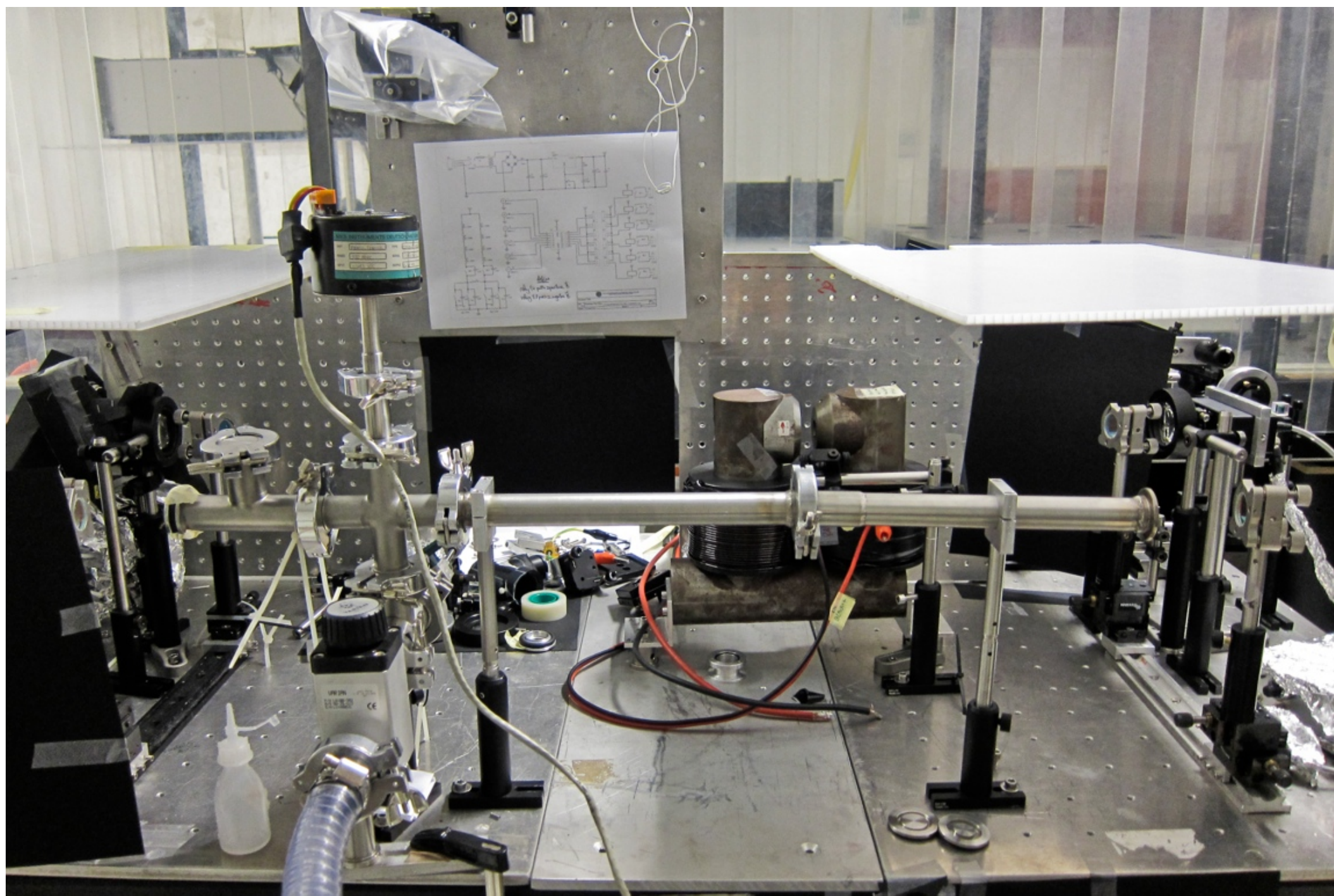


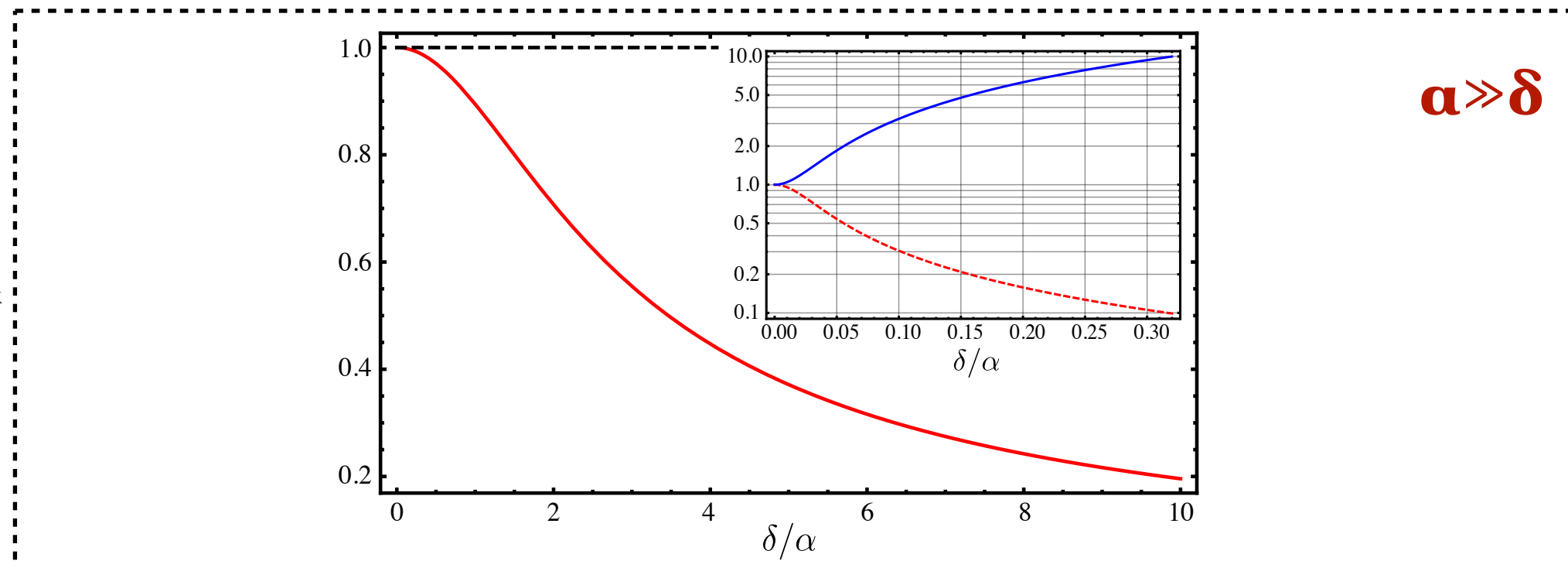
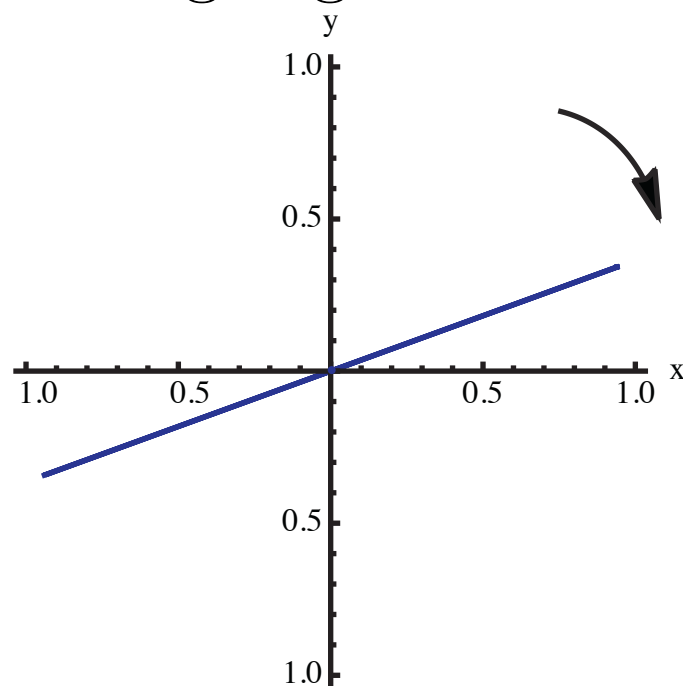
FIG. 4: Non-resonant Faraday effect of an intracavity SiO_2 window at 800 nm. The cavity ring-down polarization beating frequencies for counterpropagating beams are visibly different (magnetic field of 1000 G). The inset shows the linear and antisymmetric magnetic-field dependence of $\omega_{\text{CW}} - \omega_{\text{CCW}}$.



Linear birefringence δ :

linear birefringence presents an adversity to high precision optical rotation measurements using high-finesse cavities

$\delta = \pi / (2N) \Rightarrow$ after N passes light becomes circular



How?



**inducing a larger circular birefringence $\alpha \gg \delta$
keeps intracavity light linearly polarized**

magneto-optical rotation: Faraday effect $\theta_F = VBl$ (V =Verdet constant)

P even & T odd