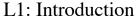
### **Lecture 1: Introduction**

#### **Some Definitions:**

- Current (I): Amount of electric charge (Q) moving past a point per unit time
  - I = dQ/dt = Coulombs/sec
  - units = Amps (1 Coulomb =  $6x10^{18}$  electrons)
    - ⇒ 1 A can do a lot of damage given the large number of electrons flowing through a wire
- Voltage (*V*):
  - Work needed to move charge from point a to b  $Work = V \bullet Q$ 
    - ⇒ Volt = Work/Charge = Joules/Coulomb
  - Voltage is always measured with respect to something
  - "ground" is defined as zero Volts
  - always capitalize the "V", e.g. 110 V, 2 kV, 13 eV
    - in honor of Alessandro Volta (1745 –1827) that invented the battery in 1799
- <u>Direct Current (DC)</u>: In a DC circuit the current and voltage are constant as a function of time
- Power (*P*): Rate of doing work
  - $\bullet$  P = dW/dt
  - units = Watts

K.K. Gan

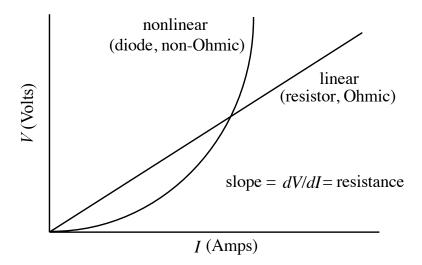






Tempio Voltiano, Como

- Ohms Law: Linear relationship between voltage and current
  - $\bullet$   $V = I \bullet R$
  - $\bullet$  R = Resistance
  - units = Ohms  $(\Omega)$



Joules Law: When current flows through a resistor energy is dissipated

$$W = QV$$

$$P = dW/dt = VdQ/dt + QdV/dt$$

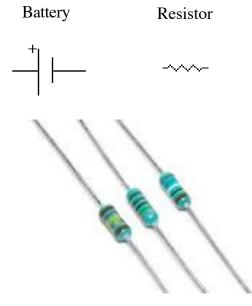
- dV/dt = 0 for DC circuit and averages to 0 for AC
- $\Rightarrow$  Power =  $VdQ/dt = V \bullet I$
- Using Ohms law

$$\Rightarrow P = I^2 R = V^2 / R$$

■ 100 Watts = 10 V and 10 Amps or 10 V through 1  $\Omega$ 

## **Simple Circuits**

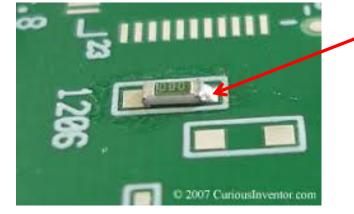
• Symbols:



- 4700 Lab resistors
- Stick the leads into "breadboard" to make connections



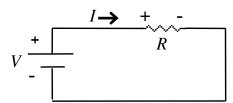




Solder paste

- Use in laptops/cell phones
- Place with "pick & place" machine
- Surface tension automatically aligns the component on their pads!
- Dimension of surface mount components (e.g. 1206):
  - length:  $120 \text{ mils} = 120 \text{ x } 25 \text{ } \mu\text{m} = 3 \text{ mm}$
  - width:  $60 \text{ mils} = 60 \text{ x } 25 \text{ } \mu\text{m} = 1.5 \text{ mm}$
  - smallest available: 01005 (0.4 mm  $\times$  0.2 mm, power rating = 0.03 W)
  - slightly less insane version: 0201 (0.6 mm  $\times$  0.3 mm, power rating = 0.05 W)

• Simple(st) Circuit:



- Convention: Current flow is in the direction of positive charge flow
  - When we go across a battery in direction of current  $(- \rightarrow +)$ 
    - **⇒** +V
  - Voltage drop across a resistor in direction of current (+ → -)
    - $\Rightarrow$  -IR
    - Conservation of Energy: sum of potential drops around the circuit should be zero
      - $\Rightarrow$  V IR = 0 or V = IR!!

• Next simple(st) circuit: two resistors in series

$$V \xrightarrow{I_1 \longrightarrow + - + - I_2 \longrightarrow} R_1 \xrightarrow{A} R_2$$

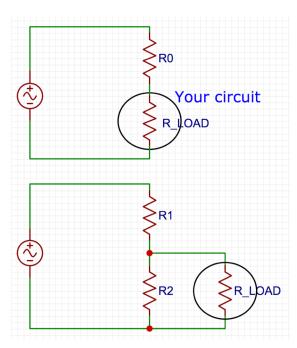
♦ Conservation of charge:  $I_1 = I_2 = I$  at point A

$$\Rightarrow$$
  $V = I(R_1 + R_2) = IR$ 

$$\Rightarrow$$
  $R = R_1 + R_2$ 

 $\Rightarrow$  Resistors in Series Add:  $R = R_1 + R_2 + R_3...$ 

- $\bullet$  What's voltage across  $R_2$ ?
  - $\Rightarrow$   $V_2 = I_2R_2 = VR_2/(R_1 + R_2)$  "Voltage Divider Equation"
- Use of voltage divider
  - When the signal from a signal generator is too large
    - $\Rightarrow$  don't use a large resistor ( $R_0$ ) to attenuate it
    - ⇒ use a voltage divider to control the signal size
    - $\Rightarrow$  choose  $R_2$  to be small compared to R\_LOAD
    - $\Rightarrow$  the ratio  $R_2/(R_1 + R_2)$  controls the size of the signal



• Two resistors in parallel

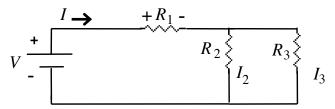
$$V \xrightarrow{I \rightarrow A} A$$

$$V \xrightarrow{+} I_1 \downarrow R_1 \quad I_2 \downarrow R_2$$

$$\therefore R = \frac{R_1 R_2}{R_1 + R_2}$$

 $\Rightarrow$  Parallel Resistors add like:  $1/R = 1/R_1 + 1/R_2 + 1/R_3 + \dots$ 

• In a circuit with 3 resistors (series and parallel), what's  $I_2 = V_2/R_2$ ?



• reduce to a simpler circuit:

$$V \xrightarrow{I} \xrightarrow{+R_1-} R_{23} = V \xrightarrow{I} \xrightarrow{+R_1-} R_{23}$$

• 
$$I = V/R = V/(R_1 + R_{23})$$

$$R_{23} = R_2 || R_3 = \frac{R_2 R_3}{R_2 + R_3}$$

$$V_2 = IR_{23}$$

$$= \frac{V}{R_1 + \frac{R_2R_3}{R_2 + R_3}} \times \frac{R_2R_3}{R_2 + R_3}$$

$$= \frac{VR_2R_3}{R_1R_2 + R_1R_2 + R_2R_3}$$

$$I_2 = \frac{V_2}{R_2}$$

$$= \frac{VR_3}{R_1R_2 + R_1R_3 + R_2R_3}$$

If 
$$R_3 \rightarrow \infty$$
 then  $I_2 = I = V/(R_1 + R_2)$  as expected!

#### Kirchoff's Laws

- We can formalize and generalize the previous examples using Kirchoff's Laws:
  - 1.  $\Sigma I = 0$  at a node: conservation of charge
  - 2.  $\Sigma V = 0$  around a closed loop: conservation of energy
  - example

- node B:  $I_1 = I_2 + I_3$   $I_1 I_2 I_3 = 0$
- loop ABEF:  $V I_1 R_1 I_2 R_2 = 0$
- loop ACDF:  $V I_1 R_1 I_3 R_3 = 0$ 
  - $\Rightarrow$  3 linear equations with 3 unknowns:  $I_1, I_2, I_3$
  - ⇒ always wind up with as many linear equations as unknowns!
- use matrix methods to solve these equations:

$$V = RI$$

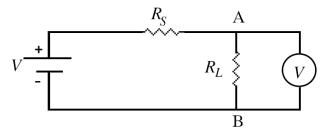
$$\begin{bmatrix} V \\ V \\ 0 \end{bmatrix} = \begin{bmatrix} R_1 & R_2 & 0 \\ R_1 & 0 & R_3 \\ 1 & -1 & -1 \end{bmatrix} \begin{bmatrix} I_1 \\ I_2 \\ I_3 \end{bmatrix}$$

$$I_{2} = \frac{\det \begin{bmatrix} R_{1} & V & 0 \\ R_{1} & V & R_{3} \\ 1 & 0 & -1 \end{bmatrix}}{\det \begin{bmatrix} R_{1} & R_{2} & 0 \\ R_{1} & 0 & R_{3} \\ 1 & -1 & -1 \end{bmatrix}} = \frac{VR_{3}}{R_{1}R_{2} + R_{1}R_{3} + R_{2}R_{3}}$$

$$\Rightarrow \text{ the } same \text{ solution as in page 7!}$$

# **Measuring Things**

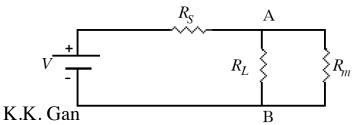
Voltmeter: Always put in parallel with what you want to measure



If no voltmeter we would have:

$$V_{AB} = \left[\frac{R_L}{R_S + R_L}\right] V$$

If the voltmeter has a finite resistance  $R_m$  then circuit looks like:



L1: Introduction

• From previous pages we have:

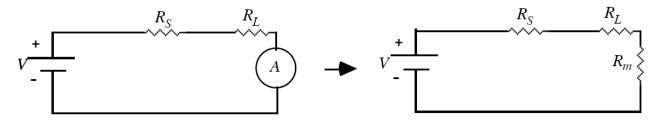
$$V_{AB}^* = \left[\frac{R_m \| R_L}{R_S + R_m \| R_L}\right] V$$

$$= \frac{VR_m R_L}{R_S R_L + R_m R_L + R_S R_m}$$

$$= \frac{VR_L}{R_L + R_S + \frac{R_S R_L}{R_m}}$$

$$\approx V_{AB} \quad \text{if } R_L << R_m$$

- $\Rightarrow$  good voltmeter has high resistance (> 10<sup>6</sup> Ω)
- Ammeter: measures current
  - Always put in series with what you want to measure



- Without meter:  $I = V/(R_S + R_L)$
- With meter:  $I^* = V/(R_S + R_L + R_m)$ 
  - ⇒ good ammeter has  $R_m \ll (R_S + R_L)$ , i.e. low resistance (0.1-1  $\Omega$ )

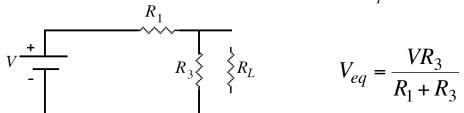
# **Thevenin's Equivalent Circuit Theorem**

- Any network of resistors and batteries having 2 output terminals may be replaced by a series combination of resistor and battery
  - Useful when solving complicated (!?) networks
  - Solve problems by finding  $V_{eq}$  and  $R_{eq}$  for circuit without load, then add load to circuit.
  - Use basic voltage divider equation:

$$V_{L} = \frac{V_{eq}R_{L}}{R_{L} + R_{eq}}$$

$$V \stackrel{R}{\longrightarrow} R_{3} \qquad R_{eq} \qquad R_{eq$$

- Two rules for using Thevenin's Thereom:
  - 1. Take the load out of the circuit to find  $V_{eq}$ :



2. Short circuit all power supplies (batteries) to find  $R_{eq}$ :

$$R_{eq} = \frac{R_1 R_3}{R_1 + R_3}$$

• Can now solve for  $I_L$  as in previous examples:

$$\begin{split} I_{L} &= \frac{V_{eq}}{R_{eq} + R_{L}} \\ &= \left[ \frac{VR_{3}}{R_{1} + R_{3}} \right] \times \frac{1}{\frac{R_{1}R_{3}}{R_{1} + R_{3}} + R_{L}} \\ &= \frac{VR_{3}}{R_{1}R_{L} + R_{1}R_{3} + R_{L}R_{3}} \end{split}$$

⇒ Same answer as previous examples!