

# Supporting Information for “Energy-Screened Many-Body Expansion: A Practical Yet Accurate Fragmentation Method for Quantum Chemistry”

Kuan-Yu Liu and John M. Herbert\*

*Department of Chemistry and Biochemistry, The Ohio State University, Columbus, Ohio 43210 USA*

(Dated: November 2, 2019)

---

\* [herbert@chemistry.ohio-state.edu](mailto:herbert@chemistry.ohio-state.edu)

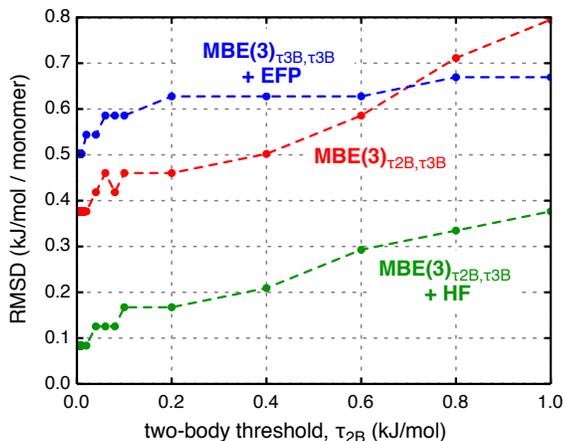


FIG. S1: Errors (with respect to a supersystem calculation) in B3LYP/aDZ calculations on clusters  $(\text{H}_2\text{O})_{N=6-34}$ , as a function of the cutoff  $\tau_{2B}$  that is applied to the two-body corrections  $\Delta E_{IJ}$ . The three-body threshold is fixed at  $\tau_{3B} = 0.25$  kJ/mol in all calculations. Higher-order induction is recovered by including a HF/aDZ or EFP correction in a two-layer scheme.

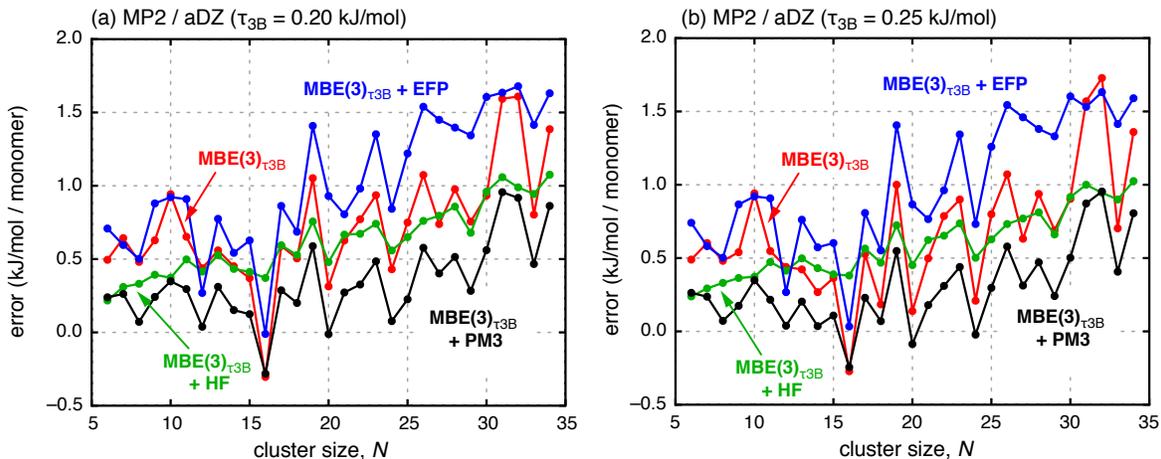


FIG. S2: Signed errors per monomer for  $\text{MBE}(3)_{\tau_{3B}}$  approximations at the MP2/aDZ level, using (a)  $\tau_{3B} = 0.20$  kJ/mol versus (b)  $\tau_{3B} = 0.25$  kJ/mol. The plot in (b) is the same as Fig. 5b, but repeated here to facilitate side-by-side comparison against results in (a) that use the tighter energy threshold. The results demonstrate that there is very little difference in the errors obtained using one threshold versus the other.

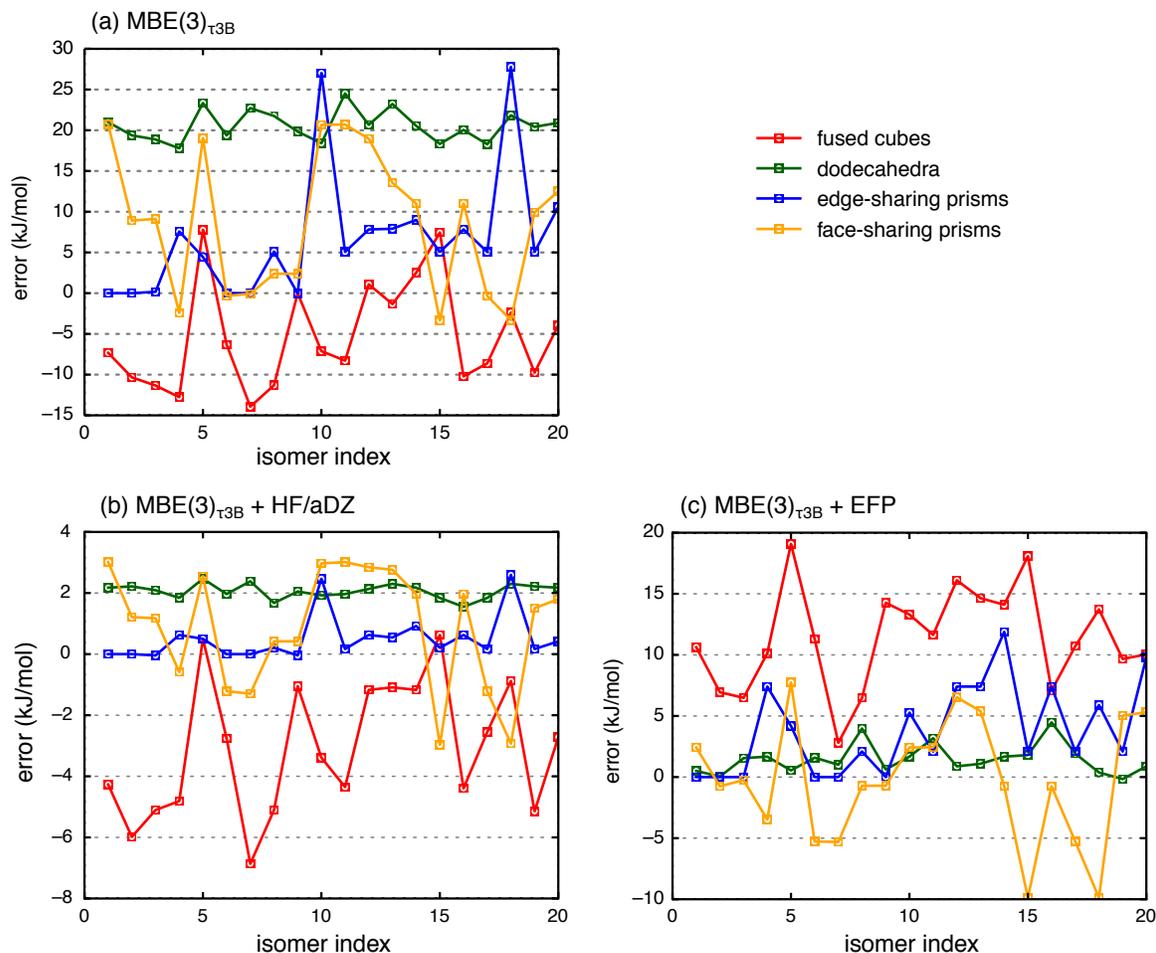


FIG. S3: Signed errors (relative to a supersystem calculation) for relative energies of  $(\text{H}_2\text{O})_{20}$  isomers computed at the  $\omega\text{B97X-V/aTZ}$  level of theory, using (a)  $\text{MBE}(3)_{\tau_{3B}}$ , (b)  $\text{MBE}(3)_{\tau_{3B}} + \text{HF/aDZ}$ , and (c)  $\text{MBE}(3)_{\tau_{3B}} + \text{EFP}$ . All fragment approximations used an energy threshold  $\tau_{3B} = 0.25$  kJ/mol. Note that the energy scale is different in each panel. The isomers and color scheme are the same as in Figs. 7 and 8.

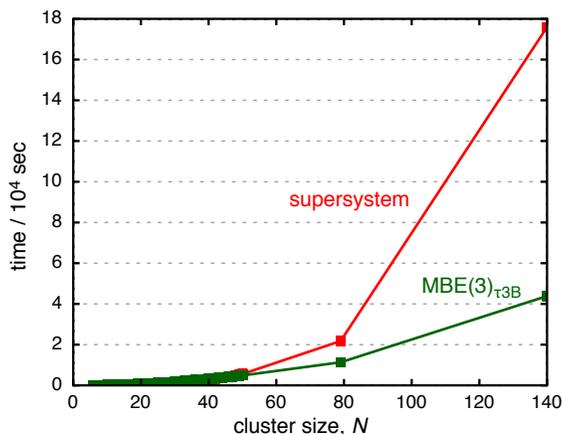


FIG. S4: Wall time for B3LYP/aDZ calculations on clusters  $(\text{H}_2\text{O})_N$  for  $N = 6-50, 79,$  and  $140$ . All calculations were performed on a single 40-core compute node, including all of the subsystem calculations for  $\text{MBE}(3)_{\tau_{3B}}$ . The latter method uses  $\tau_{3B} = 0.25$  kJ/mol as the energy threshold.