## Supplementary Material for "Fractional-Electron and Transition-Potential Methods for Core-to-Valence Excitation Energies Using Density Functional Theory"

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| Molecule          | Atom         | Expt.          | $\Delta SCF$   | STM            | GSTM  | TPM            | GSTM  | FCHM  | XCHM  | IP-TPM@1/2     | IP-TPM@1/3 |
|-------------------|--------------|----------------|----------------|----------------|-------|----------------|-------|-------|-------|----------------|------------|
| $C_2H_4$          | С            | 284.7          | 286.9          | 287.1          | 288.0 | 288.5          | 289.9 | 283.3 | 285.9 | 288.0          | 286.4      |
| HCHO              | $\mathbf{C}$ | 285.6          | 287.0          | 287.7          | 287.0 | 290.2          | 289.6 | 284.7 | 279.2 | 289.6          | 287.7      |
| $C_2H_2$          | $\mathbf{C}$ | 285.9          | 287.9          | 288.1          | 289.2 | 289.6          | 291.3 | 284.4 | 287.4 | 289.1          | 287.4      |
| $C_2N_2$          | $\mathbf{C}$ | 286.3          | 288.1          | 288.2          | 289.1 | 290.1          | 290.7 | 285.4 | 287.8 | 289.6          | 288.3      |
| HCN               | С            | 286.4          | 287.5          | 288.2          | 287.6 | 290.6          | 290.0 | 285.5 | 280.2 | 290.1          | 288.2      |
| acetone           | C(CO)        | 286.4          | 287.5          | 288.3          | 287.6 | 290.7          | 290.2 | 284.9 | 279.7 | 290.1          | 288.5      |
| $C_2H_6$          | Č Ś          | 286.9          | 288.8          | 289.2          | 289.7 | 291.0          | 290.9 | 287.0 | 290.1 | 289.8          | 288.9      |
| cõ                | С            | 287.4          | 288.0          | 288.7          | 288.1 | 291.8          | 291.3 | 286.9 | 280.1 | 291.3          | 289.1      |
| $CH_4$            | $\mathbf{C}$ | 288.0          | 288.2          | 288.7          | 288.3 | 290.2          | 289.7 | 287.1 | 284.3 | 289.7          | 288.7      |
| MeOH              | С            | 288.0          | 289.7          | 290.4          | 289.8 | 291.7          | 291.4 | 288.2 | 285.5 | 291.2          | 289.7      |
| HCOOH             | С            | 288.1          | 289.1          | 289.8          | 289.2 | 292.5          | 291.9 | 287.0 | 281.3 | 291.9          | 290.0      |
| HCOF              | С            | 288.2          | 289.3          | 290.0          | 289.4 | 292.8          | 292.3 | 287.3 | 281.3 | 292.2          | 290.3      |
| $CO_2$            | Ċ            | 290.8          | 291.4          | 292.1          | 291.2 | 295.2          | 294.3 | 290.0 | 283.5 | 294.6          | 292.5      |
| $CF_2O$           | Ċ            | 290.9          | 291.7          | 292.4          | 291.8 | 295.5          | 297.0 | 289.9 | 283.3 | 294.9          | 294.0      |
| - 2 -             |              |                |                |                |       |                |       |       |       |                |            |
| MAE               | C(1s)        |                | 1.26           | 1.81           | 1.59  | 4.06           | 4.06  | 0.90  | 4.92  | 3.46           | 1.87       |
|                   | · · ·        |                |                |                |       |                |       |       |       |                |            |
|                   |              |                |                |                |       |                |       |       |       |                |            |
| $C_2N_2$          | N            | 398.9          | 400.0          | 400.7          | 402.1 | 403.8          | 403.8 | 395.6 | 400.1 | 401.9          | 400.4      |
| HCN               | Ν            | 399.7          | 400.7          | 401.5          | 400.8 | 403.8          | 403.2 | 396.8 | 391.9 | 403.2          | 401.3      |
| Imidazole         | N            | 399.9          |                |                |       |                |       |       |       |                |            |
| $NH_3$            | N            | 400.8          | 402.0          | 402.8          | 402.2 | 404.3          | 403.8 | 399.6 | 396.4 | 403.7          | 402.5      |
| $N_2$             | Ν            | 400.9          | 401.7          | 403.3          | 404.6 | 405.4          | 407.8 | 398.6 | 392.3 | 404.8          | 402.6      |
| $N_2O$            | Ν            | 401.0          |                |                |       |                |       |       |       |                |            |
| Glycine           | Ν            | 401.2          | 402.6          | 403.5          | 402.7 | 404.7          | 404.0 | 399.7 | 397.0 | 404.1          | 403.0      |
| Pyrrole           | Ν            | 402.3          | 403.5          | 404.5          | 403.9 | 405.4          | 404.7 | 399.5 | 397.0 | 404.8          | 403.7      |
| Imidazole         | NH           | 402.3          | 401.0          | 404.1          | 403.5 | 405.6          | 404.9 | 399.6 | 402.9 | 405.0          | 403.7      |
| $N_2O$            | N (center)   | 404.6          | 405.4          | 402.7          | 408.3 | 408.9          | 407.4 | 401.9 | 396.1 | 408.3          | 406.7      |
| MAE               | N(1s)        |                | 1.10           | 2.03           | 2.18  | 3.89           | 3.61  | 2.42  | 5.08  | 3.14           | 1.66       |
|                   |              |                | -              |                |       |                |       |       |       | -              |            |
|                   |              |                |                |                |       |                |       |       |       |                |            |
| HCHO              | О            | 530.8          | 531.8          | 532.5          | 532.0 | 534.7          | 534.1 | 527.0 | 522.8 | 534.0          | 532.3      |
| acetone           | О            | 531.4          | 532.1          | 532.7          | 532.3 | 534.8          | 534.3 | 527.3 | 523.5 | 534.1          | 532.7      |
| HCOF              | О            | 532.1          | 532.8          | 533.5          | 533.0 | 535.7          | 535.2 | 528.2 | 524.1 | 535.0          | 533.3      |
| HCOOH             | О            | 532.2          |                |                |       |                |       |       |       |                |            |
| $CF_2O$           | О            | 532.7          | 533.8          | 534.4          | 534.0 | 536.7          | 536.2 | 529.3 | 525.1 | 536.1          | 534.3      |
| $H_2O$            | О            | 534.0          | 535.2          | 536.0          | 535.4 | 537.8          | 537.3 | 532.2 | 528.5 | 537.2          | 535.8      |
| MeOH              | О            | 534.1          | 535.3          | 536.2          | 535.5 | 537.6          | 537.0 | 531.6 | 528.7 | 537.0          | 535.7      |
| CO                | О            | 534.2          | 534.9          | 535.6          | 535.0 | 538.0          | 537.4 | 530.5 | 525.8 | 537.4          | 535.4      |
| $N_2O$            | О            | 534.6          | 535.7          | 536.3          | 535.8 | 538.0          | 537.6 | 530.7 | 527.5 | 537.4          | 535.8      |
| Furan             | О            | 535.2          | 536.1          | 536.7          | 536.3 | 538.1          | 537.6 | 531.3 | 528.8 | 537.5          | 536.3      |
| HCOOH             | OH           | 535.4          | 536.5          | 533.4          | 536.7 | 538.4          | 538.9 | 532.1 | 529.7 | 537.8          | 535.5      |
| $CO_2$            | О            | 535.4          | 536.3          | 536.9          | 538.2 | 539.0          | 540.6 | 541.0 | 536.0 | 538.3          | 536.6      |
|                   |              |                |                |                |       |                |       |       |       |                |            |
| MAE               | O(1s)        |                | 0.97           | 1.67           | 1.29  | 3.54           | 3.30  | 3.62  | 6.43  | 2.90           | 1.24       |
|                   |              |                |                |                |       |                |       |       |       |                |            |
| F                 | F            | 600.0          | 600 0          | COF O          | COE 7 | 607 1          | 680.0 | 600 F | 670.4 | 696 7          | 694.0      |
| 1'2<br>11E        | г<br>Г       | 002.2<br>697 A | 002.0          | 680.2          | 000.1 | 001.4          | 601.0 | 000.0 | 070.4 | 000.7          | 004.0      |
| пг<br>ЦСОР        | r<br>F       | 001.4          | 000.0<br>699 7 | 009.3          | 688.0 | 091.0<br>600 7 | 600.0 | 684 5 | 680 1 | 600.9          | 009.2      |
| CEO               | F<br>F       | 081.1          | 088.7          | 089.4<br>600.0 | 601.2 | 602.6          | 690.2 | 084.0 | 082.1 | 690.0<br>601.6 | 088.0      |
| OF <sub>2</sub> O | Г            | 089.2          | 690.3          | 690.9          | 091.2 | 092.8          | 092.4 | 080.2 | 089.0 | 091.0          | 090.2      |
| MAE               | F(1s)        |                | 0.97           | 2.00           | 2.04  | 3.99           | 4.26  | 3.52  | 5.79  | 3.17           | 1.37       |
|                   | - ()         |                | 0.01           | 2.00           |       | 0.00           |       | 0.02  | 0.10  | 0.11           | 1.01       |
| MAE               | all          |                | 1.11           | 1.84           | 1.68  | 3.86           | 3.76  | 2.32  | 5.50  | 3.19           | 1.58       |
|                   |              |                | 1.11           | 1.04           | 1.00  | 5.00           | 5.10  | 2.02  | 5.00  | 0.10           | 1.00       |

Table S1: Excitation energies (in eV) for 37 K-edge (1s  $\rightarrow$  LUMO) transitions computed using various methods with the SRC1-r1 functional, including relativistic corrections.

Table S2: Excitation energies (in eV) for 20 higher-lying K-edge transitions computed using various methods with the SRC1-r1 functional, including relativistic corrections.

| Mologulo            | Atom         | Funt   | ASCE   | хсим   | VTDM   | VCTPM  | IP-     | IP-     |
|---------------------|--------------|--------|--------|--------|--------|--------|---------|---------|
| Molecule            | Atom         | Expt.  | ASCI   | ACHIM  | AITM   | AGITM  | TPM@1/2 | TPM@1/3 |
| NH <sub>3</sub>     | Ν            | 402.33 | 403.75 | 397.85 | 405.00 | 404.22 | 405.83  | 404.61  |
| NH <sub>3</sub>     | Ν            | 402.86 | 403.80 | 398.02 | 405.00 | 404.22 | 405.83  | 404.61  |
| NH <sub>3</sub>     | Ν            | 403.57 | 405.08 | 400.22 | 406.02 | 405.25 | 406.93  | 405.95  |
| HCHO (formaldehyde) | $\mathbf{C}$ | 290.18 | 291.72 | 287.57 | 291.24 | 290.52 | 293.30  | 292.20  |
| HCHO (formaldehyde) | $\mathbf{C}$ | 291.25 | 293.30 | 289.61 | 292.50 | 291.75 | 294.61  | 293.50  |
| HCHO (formaldehyde) | $\mathbf{C}$ | 291.73 | 292.73 | 288.06 | 292.60 | 291.87 | 294.77  | 293.79  |
| HCHO (formaldehyde) | 0            | 535.43 | 536.55 | 530.88 | 536.02 | 535.00 | 537.85  | 536.91  |
| HCHO (formaldehyde) | 0            | 536.34 | 537.45 | 531.18 | 537.20 | 536.15 | 539.02  | 537.99  |
| CO                  | $\mathbf{C}$ | 292.37 | 294.40 | 292.34 | 292.66 | 291.93 | 296.03  | 295.07  |
| CO                  | $\mathbf{C}$ | 293.33 | 295.63 | 294.27 | 293.70 | 292.97 | 297.26  | 296.38  |
| CO                  | $\mathbf{C}$ | 293.49 | 295.45 | 293.93 | 293.76 | 293.04 | 297.33  | 296.49  |
| CO                  | 0            | 538.91 | 539.97 | 534.81 | 539.04 | 537.97 | 541.57  | 540.63  |
| CO                  | 0            | 539.91 | 541.21 | 536.70 | 540.13 | 539.05 | 542.84  | 542.00  |
| N <sub>2</sub>      | Ν            | 406.10 | 408.16 | 403.89 | 409.47 | 409.00 | 412.15  | 411.11  |
| $N_2$               | Ν            | 407.00 | 409.11 | 405.72 | 409.94 | 409.47 | 412.77  | 411.58  |
| $N_2O$              | NC           | 407.60 | 410.61 | 403.76 | 409.34 | 410.82 | 412.49  | 411.05  |
| $C_2H_4$ (ethylene) | $\mathbf{C}$ | 287.24 | 288.74 | 284.55 | 290.15 | 289.84 | 290.33  | 289.41  |
| $C_2H_4$ (ethylene) | $\mathbf{C}$ | 287.88 | 289.47 | 285.82 | 290.62 | 290.32 | 291.14  | 290.19  |
| H <sub>2</sub> O    | 0            | 535.90 | 536.77 | 530.02 | 537.91 | 536.85 | 539.08  | 537.76  |
| $H_2O$              | О            | 537.00 | 538.31 | 533.42 | 539.00 | 537.93 | 540.28  | 539.35  |
| MAE                 |              |        | 1.59   | 3.96   | 1.54   | 1.34   | 3.55    | 2.51    |

| Malaaula            | Atom         | Transition                  | Errot  | $\Delta S$ | SCF (B3LYP)              |                            |
|---------------------|--------------|-----------------------------|--------|------------|--------------------------|----------------------------|
| Molecule            | Atom         | Transition                  | Expt.  | def2-QZVPD | double-aug. <sup>a</sup> | $\operatorname{diff.}^{b}$ |
| NH <sub>3</sub>     | Ν            | $1s \rightarrow 3s$         | 400.66 | 400.57     | 400.49                   | 0.08                       |
| $ m NH_3$           | Ν            | $1s \to 3p(E)$              | 402.33 | 402.30     | 402.09                   | 0.21                       |
| $ m NH_3$           | Ν            | $1s \to 3p(A_1)$            | 402.86 | 402.35     | 402.12                   | 0.23                       |
| $ m NH_3$           | Ν            | $1s \to 4s(A_1)$            | 403.57 | 403.71     | 403.07                   | 0.64                       |
| HCHO (formaldehyde) | $\mathbf{C}$ | $1s \to \pi^*$              | 285.59 | 285.56     | 285.55                   | 0.01                       |
| HCHO (formaldehyde) | $\mathbf{C}$ | $1s \rightarrow 3s$         | 290.18 | 290.22     | 290.18                   | 0.04                       |
| HCHO (formaldehyde) | $\mathbf{C}$ | $1s \to 3p(B_2)$            | 291.25 | 291.82     | 291.06                   | 0.76                       |
| HCHO (formaldehyde) | $\mathbf{C}$ | $1s \to 3p(B_1)$            | 291.73 | 291.22     | 291.55                   | -0.33                      |
| HCHO (formaldehyde) | Ο            | $1s \to \pi^a st$           | 530.82 | 530.73     | 530.73                   | 0.00                       |
| HCHO (formaldehyde) | Ο            | $1s \rightarrow 3s$         | 535.43 | 535.51     | 535.44                   | 0.07                       |
| HCHO (formaldehyde) | Ο            | $1s \rightarrow 3p$         | 536.34 | 536.34     | 536.32                   | 0.02                       |
| CO                  | $\mathbf{C}$ | $1s \rightarrow 2p\pi^*$    | 287.40 | 286.58     | 286.58                   | 0.00                       |
| CO                  | $\mathbf{C}$ | $1s \rightarrow 3s\sigma$   | 292.37 | 292.86     | 292.77                   | 0.09                       |
| CO                  | $\mathbf{C}$ | $1s \rightarrow 3p\pi$      | 293.33 | 293.90     | 293.83                   | 0.07                       |
| CO                  | $\mathbf{C}$ | $1s \rightarrow 3p\sigma$   | 293.49 | 294.11     | 293.67                   | 0.44                       |
| CO                  | Ο            | $1s \to \pi^*$              | 534.21 | 533.84     | 533.84                   | 0.00                       |
| CO                  | Ο            | $1s \rightarrow 3s$         | 538.91 | 538.92     | 538.81                   | 0.11                       |
| CO                  | Ο            | $1s \rightarrow 3p\pi$      | 539.91 | 539.98     | 539.86                   | 0.12                       |
| $N_2$               | Ν            | $1s \to 2p\pi_q$            | 401.00 | 400.45     | 400.45                   | 0.00                       |
| $N_2$               | Ν            | $1s \rightarrow 3s\sigma_g$ | 406.10 | 406.76     | 406.32                   | 0.44                       |
| $N_2$               | Ν            | $1s \rightarrow 3p\pi_u$    | 407.00 | 407.72     | 407.31                   | 0.41                       |
| $N_2O$              | NC           | $1s \rightarrow 3p\pi^*$    | 404.70 | 404.01     | 404.01                   | 0.00                       |
| $N_2O$              | NC           | $1s \rightarrow 3p\sigma$   | 407.60 | 407.99     | 407.92                   | 0.07                       |
| $C_2H_4$ (ethylene) | $\mathbf{C}$ | $1s \to \pi^*$              | 284.67 | 284.72     | 284.71                   | 0.01                       |
| $C_2H_4$ (ethylene) | $\mathbf{C}$ | $1s \rightarrow 3s$         | 287.24 | 287.32     | 287.23                   | 0.09                       |
| $C_2H_4$ (ethylene) | $\mathbf{C}$ | $1s \rightarrow 3p\pi$      | 287.88 | 288.09     | 287.95                   | 0.14                       |
| $H_2O$              | Ο            | $1s \rightarrow 4a_1/3s$    | 534.00 | 533.89     | 533.84                   | 0.05                       |
| $H_2O$              | Ο            | $1s \rightarrow 3p(b_2)$    | 537.00 | 537.14     | 536.92                   | 0.22                       |
| MAE                 |              |                             |        | 0.31       | 0.25                     | $0.17^{c}$                 |

Table S3: Excitation energies (in eV) for 28 K-edge transitions from Ref. 1, including some higher-lying transitions, computed at the  $\Delta$ SCF level using B3LYP in two different basis sets. All theoretical calculations include relativistic corrections.

<sup>*a*</sup> def2-QZVPD with additional *s* and *p* functions on non-hydrogen atoms, whose exponents are scaled by 1/3 relative to the most diffuse *s* and *p* exponents in def2-QZVPD. <sup>*b*</sup>Difference in the excitation energies computed in the two basis sets. <sup>*c*</sup>Mean absolute difference between excitation energies in either basis set.

| Molecule   | Atom         | Expt.              | SCAN  | SCAN0 | B3LYP | BH&HLYP | CAM-B3LYP | $LRC-\omega PBE$ | $LRC-\omega PBEh$ | $\omega B97X-V$ |
|------------|--------------|--------------------|-------|-------|-------|---------|-----------|------------------|-------------------|-----------------|
| $C_2H_4$   | С            | $284.7^{2}$        | 284.5 | 284.5 | 284.7 | 285.1   | 284.6     | 283.6            | 284.0             | 285.0           |
| HCHO       | $\mathbf{C}$ | 285.6 <sup>3</sup> | 285.4 | 285.5 | 285.6 | 286.0   | 285.5     | 284.5            | 284.8             | 285.9           |
| $C_2H_2$   | $\mathbf{C}$ | $285.9^{2}$        | 285.4 | 285.5 | 285.6 | 286.1   | 285.5     | 284.5            | 284.9             | 285.9           |
| $C_2N_2$   | $\mathbf{C}$ | $286.3^{4}$        | 285.9 | 286.0 | 286.1 | 286.4   | 286.0     | 285.1            | 285.4             | 286.5           |
| HCN        | $\mathbf{C}$ | $286.4^{4}$        | 286.0 | 286.1 | 286.1 | 286.6   | 286.0     | 285.1            | 285.5             | 286.4           |
| acetone    | C(CO)        | $286.4^{5}$        | 286.1 | 286.2 | 286.1 | 287.9   | 286.1     | 285.2            | 285.5             | 286.5           |
| C2H6       | C            | 286.9 <sup>2</sup> | 286.8 | 287.0 | 286.9 | 287.2   | 287.2     | 286.2            | 286.4             | 287.5           |
| CO         | $\mathbf{C}$ | 287.4 <sup>6</sup> | 286.5 | 286.6 | 286.6 | 287.1   | 286.5     | 285.6            | 285.9             | 286.9           |
| $CH_4$     | $\mathbf{C}$ | $288^{7}$          | 286.7 | 286.8 | 286.7 | 287.3   | 286.7     | 286.0            | 286.2             | 287.3           |
| MeOH       | $\mathbf{C}$ | $288^{5}$          | 288.2 | 288.4 | 288.2 | 288.9   | 288.3     | 287.5            | 287.7             | 288.8           |
| HCOOH      | $\mathbf{C}$ | $288.1^{5}$        | 287.6 | 287.7 | 287.7 | 288.2   | 287.6     | 286.6            | 287.0             | 288.0           |
| HCOF       | $\mathbf{C}$ | 288.2 <sup>8</sup> | 287.8 | 287.9 | 287.8 | 288.4   | 287.8     | 286.8            | 287.2             | 288.2           |
| $CO_2$     | $\mathbf{C}$ | 290.8 <sup>9</sup> | 289.8 | 290.0 | 289.9 | 290.6   | 289.9     | 288.8            | 289.2             | 290.2           |
| $CF_2O$    | $\mathbf{C}$ | 290.9 <sup>8</sup> | 290.2 | 290.3 | 290.2 | 290.9   | 290.2     | 289.1            | 289.5             | 290.5           |
| $C_2N_2$   | Ν            | $398.9^{4}$        | 398.5 | 398.6 | 398.6 | 399.1   | 398.6     | 397.7            | 398.0             | 399.1           |
| HCN        | Ν            | $399.7^{4}$        | 399.3 | 399.4 | 399.4 | 399.8   | 399.3     | 398.4            | 398.7             | 399.8           |
| $NH_3$     | Ν            | $400.8^{7}$        | 400.6 | 400.8 | 400.6 | 401.2   | 400.6     | 399.8            | 400.1             | 401.2           |
| $N_2$      | Ν            | $400.9^{10}$       | 400.5 | 400.5 | 400.5 | 401.1   | 400.4     | 399.5            | 399.8             | 400.9           |
| Glycine    | Ν            | $401.2^{11}$       | 401.2 | 401.4 | 401.2 | 401.9   | 401.3     | 400.5            | 400.8             | 402.2           |
| Pyrrole    | Ν            | $402.3^{12}$       | 402.1 | 402.2 | 402.1 | 403.0   | 402.4     | 401.6            | 401.9             | 402.9           |
| Imidazole  | NH           | $402.3^{13}$       | 402.2 | 402.3 | 402.1 | 403.3   | 402.7     | 401.9            | 402.2             | 403.2           |
| $N_2O$     | N (center)   | $404.6^{9}$        | 404.2 | 404.2 | 404.0 | 404.5   | 404.0     | 403.1            | 403.5             | 404.5           |
| HCHO       | O Ó          | 530.8 <sup>3</sup> | 530.8 | 530.7 | 530.7 | 531.0   | 530.7     | 529.8            | 530.0             | 531.1           |
| acetone    | Ο            | $531.4^{5}$        | 531.1 | 531.0 | 531.0 | 531.4   | 531.0     | 530.1            | 530.4             | 531.4           |
| HCOF       | О            | 532.1 <sup>8</sup> | 531.9 | 531.8 | 531.8 | 532.1   | 531.8     | 530.8            | 531.1             | 532.2           |
| $CF_2O$    | О            | 532.7 <sup>8</sup> | 532.9 | 532.8 | 532.7 | 533.1   | 532.7     | 531.8            | 532.1             | 533.2           |
| $H_2O$     | О            | $534^{7}$          | 534.1 | 534.1 | 533.9 | 534.5   | 534.0     | 533.1            | 533.4             | 534.5           |
| MeOH       | О            | $534.1^{-5}$       | 534.2 | 534.3 | 534.0 | 534.7   | 534.2     | 533.2            | 533.5             | 534.6           |
| CO         | О            | 534.2 <sup>6</sup> | 534.0 | 533.9 | 533.8 | 534.2   | 533.9     | 533.0            | 533.2             | 534.3           |
| $N_2O$     | О            | $534.6^{9}$        | 535.0 | 534.7 | 534.6 | 534.8   | 534.5     | 533.7            | 534.0             | 535.0           |
| Furan      | Ο            | $535.2^{14}$       | 535.1 | 535.1 | 534.9 | 535.4   | 535.0     | 536.4            | 536.6             | 535.5           |
| HCOOH      | OH           | $535.4^{5}$        | 535.4 | 535.4 | 535.2 | 536.4   | 535.8     | 534.8            | 535.2             | 536.2           |
| $CO_2$     | Ο            | $535.4^{9}$        | 535.4 | 535.3 | 535.7 | 536.0   | 535.8     | 534.8            | 535.2             | 536.2           |
| $F_2$      | $\mathbf{F}$ | $682.2^{15}$       | 682.5 | 682.1 | 682.2 | 682.9   | 682.3     | 681.4            | 681.5             | 682.7           |
| $_{ m HF}$ | F            | $687.4^{15}$       | 687.8 | 687.8 | 687.5 | 688.1   | 687.7     | 686.6            | 686.8             | 688.0           |
| HCOF       | F            | 687.7 <sup>8</sup> | 688.0 | 687.9 | 687.7 | 688.2   | 687.9     | 686.8            | 687.1             | 688.2           |
| $CF_2O$    | F            | 689.2 <sup>8</sup> | 689.7 | 689.5 | 689.3 | 690.5   | 690.2     | 689.1            | 689.5             | 690.6           |

Table S4: Excitation energies (in eV) for 37 K-edge (1s  $\rightarrow$  LUMO) transitions computed using  $\Delta$ SCF, including relativistic corrections.

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| Molecule  | Atom         | Expt. | SCAN  | SCAN0 | B3LYP | BH&HLYP | CAM-B3LYP | $LRC-\omega PBE$ | $LRC-\omega PBEh$ | $\omega B97X-V$ |
|-----------|--------------|-------|-------|-------|-------|---------|-----------|------------------|-------------------|-----------------|
| $C_2H_4$  | С            | 284.7 | 286.7 | 286.3 | 285.8 | 285.3   | 285.7     | 285.3            | 285.4             | 286.3           |
| HCHO      | $\mathbf{C}$ | 285.6 | 287.7 | 287.3 | 286.7 | 286.9   | 286.7     | 286.2            | 286.3             | 287.2           |
| $C_2H_2$  | $\mathbf{C}$ | 285.9 | 287.7 | 287.3 | 286.7 | 286.4   | 286.7     | 286.2            | 286.3             | 287.3           |
| $C_2N_2$  | $\mathbf{C}$ | 286.3 | 288.4 | 288.0 | 287.3 | 287.4   | 287.3     | 286.9            | 284.7             | 287.9           |
| HCN       | $\mathbf{C}$ | 286.4 | 288.4 | 288.0 | 287.3 | 287.5   | 287.3     | 286.8            | 286.9             | 287.9           |
| acetone   | C(CO)        | 286.4 | 288.4 | 288.0 | 287.3 | 287.4   | 287.3     | 286.9            | 286.9             | 287.8           |
| $C_2H_6$  | $\mathbf{C}$ | 286.9 | 289.1 | 285.2 | 288.0 | 287.7   | 288.1     | 288.1            | 287.9             | 287.9           |
| CO        | $\mathbf{C}$ | 287.4 | 288.8 | 288.5 | 287.8 | 288.0   | 287.8     | 287.2            | 287.3             | 288.3           |
| $CH_4$    | $\mathbf{C}$ | 288.0 | 288.9 | 288.6 | 287.8 | 288.0   | 287.9     | 287.7            | 287.6             | 288.6           |
| MeOH      | $\mathbf{C}$ | 288.0 | 290.6 | 290.3 | 289.4 | 289.7   | 289.5     | 289.3            | 289.3             | 290.3           |
| HCOOH     | $\mathbf{C}$ | 288.1 | 289.9 | 289.5 | 288.8 | 289.0   | 288.8     | 288.3            | 288.4             | 289.3           |
| HCOF      | $\mathbf{C}$ | 288.2 | 290.1 | 289.7 | 289.0 | 289.2   | 289.0     | 288.5            | 288.6             | 289.5           |
| $CO_2$    | $\mathbf{C}$ | 290.8 | 292.1 | 291.8 | 291.0 | 291.3   | 291.0     | 290.4            | 290.5             | 294.8           |
| $CF_2O$   | $\mathbf{C}$ | 290.9 | 292.5 | 292.1 | 291.3 | 291.6   | 291.3     | 290.7            | 290.9             | 291.8           |
| $C_2N_2$  | Ν            | 398.9 | 401.2 | 400.7 | 399.9 | 401.2   | 400.0     | 399.5            | 399.6             | 400.5           |
| HCN       | Ν            | 399.7 | 401.9 | 401.4 | 400.7 | 400.7   | 400.7     | 400.3            | 400.3             | 401.3           |
| $NH_3$    | Ν            | 400.8 | 403.1 | 402.7 | 401.8 | 402.0   | 402.0     | 401.7            | 401.7             | 402.7           |
| $N_2$     | Ν            | 400.9 | 403.2 | 402.6 | 401.7 | 401.4   | 401.8     | 401.3            | 401.4             | 402.3           |
| Glycine   | Ν            | 401.2 | 404.9 | 403.5 | 402.5 | 402.8   | 402.8     | 402.7            | 402.6             | 403.6           |
| Pyrrole   | Ν            | 402.3 | 404.7 | 404.5 | 403.6 | 403.8   | 403.8     | 403.6            | 403.5             | 404.6           |
| Imidazole | NH           | 402.3 | 404.7 | 404.8 | 403.3 | 404.1   | 404.1     | 403.8            | 403.8             | 404.8           |
| $N_2O$    | N (center)   | 404.6 | 406.8 | 406.3 | 405.3 | 405.3   | 405.3     | 404.9            | 405.0             | 405.9           |
| HCHO      | Ο            | 530.8 | 533.6 | 532.8 | 532.0 | 531.8   | 532.1     | 531.7            | 531.6             | 532.6           |
| acetone   | Ο            | 531.4 | 533.9 | 533.1 | 532.3 | 532.1   | 532.4     | 531.9            | 531.9             | 532.9           |
| HCOF      | Ο            | 532.1 | 534.7 | 533.9 | 533.0 | 532.8   | 533.1     | 532.7            | 532.6             | 533.6           |
| $CF_2O$   | Ο            | 532.7 | 535.7 | 534.8 | 533.9 | 533.7   | 534.0     | 533.6            | 533.5             | 534.6           |
| $H_2O$    | Ο            | 534.0 | 536.9 | 536.4 | 535.3 | 535.4   | 535.5     | 535.2            | 535.1             | 536.2           |
| MeOH      | Ο            | 534.1 | 537.1 | 536.6 | 535.5 | 535.6   | 535.7     | 535.4            | 535.3             | 536.4           |
| CO        | Ο            | 534.2 | 536.8 | 536.0 | 535.1 | 535.0   | 535.2     | 534.9            | 534.8             | 535.8           |
| $N_2O$    | Ο            | 534.6 | 537.8 | 536.8 | 535.9 | 535.5   | 535.8     | 535.5            | 535.5             | 538.7           |
| Furan     | Ο            | 535.2 | 538.0 | 537.2 | 536.2 | 536.1   | 536.3     | 536.0            | 535.9             | 536.9           |
| HCOOH     | OH           | 535.4 | 538.2 | 537.5 | 536.5 | 537.3   | 537.4     | 537.0            | 536.9             | 538.1           |
| $CO_2$    | О            | 535.4 | 538.2 | 537.4 | 537.2 | 538.5   | 537.4     | 537.1            | 531.8             | 533.7           |
| $F_2$     | F            | 682.2 | 685.6 | 684.4 | 683.6 | 683.1   | 683.7     | 683.4            | 683.2             | 684.2           |
| HF        | F            | 687.4 | 690.8 | 690.1 | 689.0 | 689.0   | 689.2     | 688.7            | 688.5             | 689.7           |
| HCOF      | F            | 687.7 | 691.1 | 690.2 | 689.1 | 688.9   | 689.2     | 688.7            | 688.6             | 689.7           |
| $CF_2O$   | F            | 689.2 | 692.7 | 691.8 | 690.6 | 692.1   | 692.1     | 691.7            | 691.5             | 692.7           |

Table S5: Excitation energies (in eV) for 37 K-edge (1s  $\rightarrow$  LUMO) transitions computed using STM, including relativistic corrections.

| Molecule         | Atom         | Expt. | SCAN  | SCAN0 | B3LYP | BH&HLYP | CAM-B3LYP | $LRC-\omega PBE$ | $LRC-\omega PBEh$ | $\omega B97X-V$ |
|------------------|--------------|-------|-------|-------|-------|---------|-----------|------------------|-------------------|-----------------|
| $C_2H_4$         | С            | 284.7 | 285.4 | 285.2 | 285.1 | 285.0   | 284.9     | 284.2            | 284.5             | 285.4           |
| HCHO             | $\mathbf{C}$ | 285.6 | 286.4 | 286.1 | 285.9 | 286.1   | 285.8     | 285.1            | 285.3             | 286.3           |
| $C_2H_2$         | $\mathbf{C}$ | 285.9 | 286.3 | 286.1 | 285.9 | 285.9   | 285.8     | 285.2            | 285.4             | 286.3           |
| $C_2N_2$         | $\mathbf{C}$ | 286.3 | 286.8 | 286.7 | 286.4 | 287.2   | 286.4     | 285.7            | 285.9             | 286.8           |
| HCN              | $\mathbf{C}$ | 286.4 | 286.9 | 286.7 | 286.5 | 286.5   | 286.3     | 285.5            | 285.8             | 286.6           |
| acetone          | C(CO)        | 286.4 | 287.0 | 286.8 | 286.5 | 286.0   | 286.3     | 285.7            | 285.9             | 286.7           |
| $C_2H_6$         | $\mathbf{C}$ | 286.9 | 287.8 | 287.8 | 287.3 | 287.4   | 287.5     | 286.8            | 286.9             | 287.9           |
| CO               | $\mathbf{C}$ | 287.4 | 287.3 | 287.2 | 286.9 | 287.2   | 286.9     | 286.1            | 286.4             | 287.3           |
| $CH_4$           | $\mathbf{C}$ | 288.0 | 287.7 | 287.6 | 287.1 | 287.5   | 287.1     | 286.5            | 286.7             | 287.7           |
| MeOH             | $\mathbf{C}$ | 288.0 | 289.2 | 289.1 | 288.6 | 289.1   | 288.6     | 288.0            | 288.2             | 289.3           |
| HCOOH            | $\mathbf{C}$ | 288.1 | 288.6 | 288.4 | 288.0 | 288.1   | 287.8     | 287.1            | 287.3             | 288.1           |
| HCOF             | $\mathbf{C}$ | 288.2 | 288.7 | 288.5 | 288.2 | 288.5   | 288.1     | 287.4            | 287.6             | 288.6           |
| $CO_2$           | $\mathbf{C}$ | 290.8 | 290.6 | 290.4 | 289.9 | 290.2   | 289.7     | 291.9            | 289.2             | 293.4           |
| $CF_2O$          | $\mathbf{C}$ | 290.9 | 291.1 | 291.0 | 290.6 | 290.9   | 290.5     | 289.7            | 289.9             | 290.8           |
| $C_2N_2$         | Ν            | 398.9 | 399.6 | 399.3 | 399.0 | 400.8   | 399.0     | 398.3            | 398.5             | 399.5           |
| HCN              | Ν            | 399.7 | 400.4 | 400.1 | 399.8 | 399.8   | 399.6     | 398.9            | 399.1             | 400.0           |
| $NH_3$           | Ν            | 400.8 | 401.7 | 401.6 | 401.0 | 401.4   | 401.0     | 400.4            | 400.6             | 401.7           |
| $N_2$            | Ν            | 400.9 | 401.5 | 401.2 | 400.9 | 401.1   | 400.8     | 400.2            | 400.3             | 401.3           |
| Glycine          | Ν            | 401.2 | 402.1 | 403.1 | 401.5 | 402.0   | 402.5     | 401.9            | 402.1             | 402.4           |
| Pyrrole          | Ν            | 402.3 | 403.2 | 402.9 | 402.3 | 403.2   | 402.9     | 402.2            | 402.4             | 403.4           |
| Imidazole        | NH           | 402.3 | 403.2 | 403.0 | 402.4 | 403.5   | 403.1     | 402.5            | 402.7             | 403.6           |
| $N_2O$           | N (center)   | 404.6 | 405.2 | 404.9 | 404.4 | 404.7   | 404.4     | 403.8            | 404.0             | 404.9           |
| HCHO             | Ο            | 530.8 | 531.9 | 531.5 | 531.2 | 531.2   | 531.2     | 530.5            | 530.6             | 531.6           |
| acetone          | О            | 531.4 | 532.3 | 531.8 | 531.5 | 531.4   | 531.4     | 530.7            | 530.9             | 531.8           |
| HCOF             | О            | 532.1 | 533.1 | 532.6 | 532.2 | 532.2   | 532.2     | 531.6            | 531.7             | 532.7           |
| $CF_2O$          | О            | 532.7 | 534.1 | 533.6 | 533.2 | 533.1   | 533.1     | 532.4            | 532.6             | 533.5           |
| $H_2O$           | О            | 534.0 | 535.3 | 535.0 | 534.4 | 534.7   | 534.5     | 533.7            | 533.9             | 535.0           |
| MeOH             | О            | 534.1 | 535.5 | 535.2 | 534.5 | 534.8   | 534.6     | 533.8            | 534.0             | 535.0           |
| CO               | О            | 534.2 | 535.2 | 534.7 | 534.3 | 534.3   | 534.3     | 533.7            | 533.8             | 534.7           |
| $N_2O$           | Ο            | 534.6 | 536.1 | 535.5 | 535.1 | 535.0   | 535.0     | 534.4            | 534.6             | 535.5           |
| Furan            | Ο            | 535.2 | 536.3 | 536.0 | 535.4 | 535.5   | 535.3     | 534.7            | 534.9             | 535.9           |
| HCOOH            | OH           | 535.4 | 536.6 | 536.2 | 535.7 | 535.8   | 535.7     | 534.9            | 535.1             | 536.0           |
| $CO_2$           | Ο            | 535.4 | 536.5 | 536.9 | 535.3 | 537.0   | 536.2     | 535.4            | 535.6             | 536.6           |
| $F_2$            | F            | 682.2 | 683.8 | 683.0 | 682.7 | 682.9   | 682.7     | 682.2            | 682.1             | 683.1           |
| $_{\mathrm{HF}}$ | F            | 687.4 | 689.2 | 688.8 | 688.1 | 688.3   | 688.2     | 687.3            | 687.4             | 688.5           |
| HCOF             | F            | 687.7 | 689.3 | 688.8 | 688.3 | 688.4   | 688.4     | 687.6            | 687.7             | 688.7           |
| $CF_2O$          | F            | 689.2 | 690.9 | 690.4 | 689.8 | 689.9   | 689.9     | 689.1            | 689.2             | 690.1           |

Table S6: Excitation energies (in eV) for 37 K-edge (1s  $\rightarrow$  LUMO) transitions computed using GSTM, including relativistic corrections.

| Molecule         | Atom         | Expt. | SCAN  | SCAN0 | B3LYP | BH&HLYP | CAM-B3LYP | $LRC-\omega PBE$ | $LRC-\omega PBEh$ | $\omega B97X-V$ |
|------------------|--------------|-------|-------|-------|-------|---------|-----------|------------------|-------------------|-----------------|
| $C_2H_4$         | С            | 284.7 | 288.0 | 288.6 | 283.4 | 291.1   | 288.9     | 289.3            | 289.1             | 290.5           |
| HCHO             | $\mathbf{C}$ | 285.6 | 289.3 | 290.2 | 288.9 | 290.7   | 290.5     | 290.8            | 290.6             | 292.1           |
| $C_2H_2$         | $\mathbf{C}$ | 285.9 | 289.1 | 288.1 | 288.5 | 292.6   | 289.9     | 290.4            | 290.2             | 291.5           |
| $C_2N_2$         | $\mathbf{C}$ | 286.3 | 289.4 | 287.3 | 283.9 | 291.9   | 290.5     | 290.8            | 290.6             | 292.0           |
| HCN              | $\mathbf{C}$ | 286.4 | 289.8 | 290.7 | 289.4 | 291.1   | 291.0     | 291.3            | 291.1             | 292.6           |
| acetone          | C(CO)        | 286.4 | 290.0 | 290.9 | 289.5 | 291.3   | 291.1     | 291.4            | 291.2             | 292.7           |
| $C_2H_6$         | $\mathbf{C}$ | 286.9 | 291.0 | 291.0 | 289.4 | 291.4   | 290.2     | 291.2            | 290.5             | 291.5           |
| CO               | $\mathbf{C}$ | 287.4 | 290.8 | 291.8 | 290.5 | 292.5   | 292.2     | 292.4            | 292.2             | 293.8           |
| $CH_4$           | $\mathbf{C}$ | 288.0 | 291.0 | 290.9 | 289.3 | 289.9   | 290.1     | 290.5            | 290.3             | 291.4           |
| MeOH             | $\mathbf{C}$ | 288.0 | 292.2 | 292.4 | 290.8 | 291.5   | 291.6     | 292.0            | 291.9             | 293.0           |
| HCOOH            | $\mathbf{C}$ | 288.1 | 291.6 | 292.5 | 291.1 | 293.0   | 292.7     | 293.0            | 292.8             | 294.4           |
| HCOF             | $\mathbf{C}$ | 288.2 | 291.8 | 292.8 | 291.4 | 293.4   | 293.1     | 293.3            | 293.1             | 294.7           |
| $CO_2$           | $\mathbf{C}$ | 290.8 | 294.0 | 295.2 | 293.6 | 295.8   | 295.3     | 295.4            | 295.3             | 296.9           |
| $CF_2O$          | $\mathbf{C}$ | 290.9 | 294.5 | 295.6 | 294.0 | 296.2   | 295.7     | 295.8            | 295.7             | 297.3           |
| $C_2N_2$         | Ν            | 398.9 | 402.2 | 402.8 | 401.6 | 404.2   | 403.1     | 403.5            | 403.2             | 400.4           |
| HCN              | Ν            | 399.7 | 403.4 | 404.1 | 402.8 | 404.3   | 404.3     | 404.8            | 404.5             | 406.0           |
| $NH_3$           | Ν            | 400.8 | 405.3 | 405.3 | 403.5 | 404.2   | 404.5     | 405.0            | 404.9             | 406.0           |
| $N_2$            | Ν            | 400.9 | 404.7 | 403.8 | 399.7 | 409.2   | 406.0     | 401.1            | 406.1             | 407.7           |
| Glycine          | Ν            | 401.2 | 404.5 | 405.0 | 403.7 | 404.6   | 404.8     | 405.4            | 405.2             | 406.2           |
| Pyrrole          | Ν            | 402.3 | 405.4 | 405.8 | 404.6 | 405.5   | 405.8     | 406.3            | 406.2             | 407.2           |
| Imidazole        | NH           | 402.3 | 405.5 | 405.9 | 404.7 | 405.9   | 406.1     | 406.6            | 406.4             | 407.5           |
| $N_2O$           | N (center)   | 404.6 | 408.3 | 409.2 | 407.6 | 409.6   | 409.4     | 409.7            | 409.5             | 411.0           |
| HCHO             | Ο            | 530.8 | 535.0 | 535.4 | 534.0 | 535.3   | 535.6     | 536.1            | 535.7             | 537.2           |
| acetone          | Ο            | 531.4 | 535.2 | 537.1 | 535.7 | 535.4   | 537.3     | 537.7            | 537.3             | 538.8           |
| HCOF             | Ο            | 532.1 | 536.0 | 536.4 | 534.9 | 536.3   | 536.6     | 537.1            | 536.7             | 538.2           |
| $CF_2O$          | Ο            | 532.7 | 537.0 | 537.4 | 535.9 | 537.4   | 537.6     | 538.0            | 537.6             | 539.2           |
| $H_2O$           | Ο            | 534.0 | 539.3 | 539.2 | 537.2 | 537.9   | 538.3     | 538.9            | 538.6             | 539.8           |
| MeOH             | Ο            | 534.1 | 539.0 | 538.9 | 537.0 | 537.7   | 538.1     | 538.6            | 538.4             | 539.5           |
| CO               | Ο            | 534.2 | 538.3 | 538.8 | 537.3 | 538.7   | 539.0     | 539.5            | 539.1             | 540.6           |
| $N_2O$           | Ο            | 534.6 | 538.5 | 538.8 | 537.3 | 538.6   | 538.9     | 539.4            | 539.0             | 540.5           |
| Furan            | Ο            | 535.2 | 538.7 | 538.9 | 537.5 | 538.5   | 539.0     | 539.5            | 539.2             | 540.5           |
| HCOOH            | OH           | 535.4 | 538.7 | 539.1 | 537.5 | 539.0   | 539.2     | 539.6            | 539.3             | 540.8           |
| $CO_2$           | Ο            | 535.4 | 539.4 | 539.8 | 538.1 | 541.2   | 539.8     | 540.2            | 534.7             | 541.3           |
| $F_2$            | F            | 682.2 | 687.3 | 688.1 | 686.4 | 691.2   | 688.3     | 688.5            | 688.2             | 685.5           |
| $_{\mathrm{HF}}$ | F            | 687.4 | 693.6 | 693.4 | 691.1 | 691.9   | 692.5     | 693.0            | 692.6             | 693.9           |
| HCOF             | F            | 687.7 | 691.5 | 691.8 | 690.1 | 691.5   | 691.9     | 692.2            | 691.8             | 693.4           |
| $CF_2O$          | F            | 689.2 | 693.1 | 693.5 | 691.7 | 693.8   | 693.5     | 693.8            | 693.4             | 695.1           |

Table S7: Excitation energies (in eV) for 37 K-edge (1s  $\rightarrow$  LUMO) transitions computed using TPM, including relativistic corrections.

| Molecule  | Atom         | Expt. | SCAN  | SCAN0 | B3LYP | BH&HLYP | CAM-B3LYP | $LRC-\omega PBE$ | $LRC-\omega PBEh$ | $\omega B97X-V$ |
|-----------|--------------|-------|-------|-------|-------|---------|-----------|------------------|-------------------|-----------------|
| $C_2H_4$  | С            | 284.7 | 286.6 | 286.5 | 286.7 | 290.9   | 288.1     | 288.2            | 288.2             | 289.6           |
| HCHO      | $\mathbf{C}$ | 285.6 | 287.8 | 288.9 | 288.1 | 290.1   | 289.7     | 289.7            | 289.6             | 291.2           |
| $C_2H_2$  | $\mathbf{C}$ | 285.9 | 282.3 | 288.5 | 287.7 | 292.2   | 288.0     | 289.4            | 288.6             | 290.7           |
| $C_2N_2$  | $\mathbf{C}$ | 286.3 | 287.9 | 288.9 | 284.0 | 291.8   | 287.4     | 289.8            | 289.7             | 289.5           |
| HCN       | $\mathbf{C}$ | 286.4 | 288.4 | 289.4 | 288.6 | 290.3   | 290.0     | 290.1            | 290.0             | 291.4           |
| acetone   | C(CO)        | 286.4 | 288.5 | 289.6 | 288.7 | 289.9   | 290.2     | 290.3            | 290.3             | 291.6           |
| $C_2H_6$  | $\mathbf{C}$ | 286.9 | 289.5 | 288.1 | 288.6 | 291.3   | 289.6     | 289.6            | 287.7             | 289.1           |
| CO        | $\mathbf{C}$ | 287.4 | 289.2 | 290.6 | 289.7 | 291.9   | 291.4     | 291.3            | 291.3             | 292.9           |
| $CH_4$    | $\mathbf{C}$ | 288.0 | 289.6 | 289.8 | 288.6 | 289.4   | 289.3     | 289.5            | 289.5             | 290.6           |
| MeOH      | $\mathbf{C}$ | 288.0 | 290.7 | 291.1 | 289.9 | 291.0   | 290.8     | 291.0            | 291.0             | 292.1           |
| HCOOH     | $\mathbf{C}$ | 288.1 | 290.1 | 291.3 | 290.3 | 292.3   | 291.8     | 291.8            | 291.8             | 293.3           |
| HCOF      | $\mathbf{C}$ | 288.2 | 290.3 | 291.6 | 290.6 | 292.8   | 292.2     | 292.2            | 292.2             | 293.8           |
| CO2       | $\mathbf{C}$ | 290.8 | 292.5 | 293.7 | 292.5 | 294.8   | 294.1     | 293.9            | 294.0             | 295.5           |
| $CF_2O$   | $\mathbf{C}$ | 290.9 | 293.0 | 294.4 | 293.2 | 295.5   | 294.8     | 294.7            | 294.8             | 296.3           |
| $C_2N_2$  | Ν            | 398.9 | 400.6 | 401.5 | 400.7 | 403.5   | 402.2     | 402.3            | 402.2             | 400.6           |
| HCN       | Ν            | 399.7 | 401.8 | 402.8 | 401.9 | 403.5   | 403.3     | 403.4            | 403.4             | 404.8           |
| $NH_3$    | Ν            | 400.8 | 403.7 | 404.0 | 403.3 | 403.7   | 403.7     | 404.6            | 403.9             | 405.1           |
| $N_2$     | Ν            | 400.9 | 403.1 | 404.4 | 403.4 | 409.1   | 403.3     | 400.9            | 405.1             | 406.7           |
| Glycine   | Ν            | 401.2 | 403.0 | 403.8 | 402.9 | 403.9   | 403.9     | 404.1            | 404.1             | 405.5           |
| Pyrrole   | Ν            | 402.3 | 403.8 | 404.5 | 403.6 | 404.8   | 404.8     | 405.0            | 405.0             | 406.2           |
| Imidazole | NH           | 402.3 | 403.9 | 404.6 | 403.7 | 405.1   | 405.0     | 405.2            | 405.2             | 406.4           |
| $N_2O$    | N (center)   | 404.6 | 406.7 | 407.9 | 406.8 | 409.0   | 408.5     | 408.5            | 408.5             | 410.1           |
| HCHO      | Ο            | 530.8 | 533.2 | 534.0 | 533.1 | 534.7   | 534.7     | 534.9            | 534.7             | 536.3           |
| acetone   | Ο            | 531.4 | 533.4 | 534.1 | 533.2 | 534.7   | 534.8     | 534.9            | 534.7             | 536.2           |
| HCOF      | Ο            | 532.1 | 534.2 | 535.0 | 534.1 | 535.8   | 535.7     | 535.9            | 535.7             | 537.3           |
| $CF_2O$   | Ο            | 532.7 | 535.2 | 536.1 | 535.0 | 536.7   | 536.6     | 536.7            | 536.6             | 538.1           |
| $H_2O$    | Ο            | 534.0 | 537.5 | 537.8 | 536.3 | 537.4   | 537.4     | 537.7            | 537.6             | 538.8           |
| MeOH      | Ο            | 534.1 | 537.1 | 537.8 | 540.6 | 537.1   | 537.1     | 542.6            | 537.3             | 538.5           |
| CO        | Ο            | 534.2 | 536.5 | 537.4 | 536.4 | 538.1   | 538.1     | 538.3            | 538.1             | 539.6           |
| $N_2O$    | Ο            | 534.6 | 536.7 | 537.5 | 536.5 | 538.1   | 538.0     | 538.2            | 538.1             | 539.6           |
| Furan     | Ο            | 535.2 | 537.0 | 537.6 | 536.7 | 537.9   | 538.0     | 538.2            | 538.1             | 539.6           |
| HCOOH     | OH           | 535.4 | 536.9 | 537.8 | 536.7 | 538.4   | 538.2     | 538.3            | 538.2             | 539.7           |
| $CO_2$    | Ο            | 535.4 | 537.5 | 538.2 | 537.0 | 540.6   | 538.5     | 538.6            | 538.5             | 536.4           |
| $F_2$     | F            | 682.2 | 685.3 | 686.6 | 685.4 | 688.5   | 687.3     | 687.1            | 687.1             | 688.8           |
| HF        | F            | 687.4 | 691.6 | 691.9 | 690.2 | 691.4   | 691.5     | 691.8            | 691.6             | 692.9           |
| HCOF      | F            | 687.7 | 689.6 | 690.4 | 689.2 | 691.0   | 691.0     | 691.0            | 690.8             | 692.4           |
| $CF_2O$   | F            | 689.2 | 691.3 | 692.1 | 690.8 | 693.6   | 692.5     | 692.5            | 692.4             | 693.9           |

Table S8: Excitation energies (in eV) for 37 K-edge (1s  $\rightarrow$  LUMO) transitions computed using GTPM, including relativistic corrections.

| Molecule  | Atom         | Expt. | SCAN  | SCAN0 | B3LYP | BH&HLYP | CAM-B3LYP | $LRC-\omega PBE$ | $LRC-\omega PBEh$ | $\omega B97X-V$ |
|-----------|--------------|-------|-------|-------|-------|---------|-----------|------------------|-------------------|-----------------|
| $C_2H_4$  | С            | 284.7 | 285.3 | 281.9 | 288.9 | 286.7   | 288.4     | 289.5            | 286.4             | 289.1           |
| HCHO      | $\mathbf{C}$ | 285.6 | 286.5 | 283.4 | 290.2 | 284.9   | 289.9     | 290.8            | 287.7             | 290.6           |
| $C_2H_2$  | $\mathbf{C}$ | 285.9 | 286.3 | 292.3 | 290.1 | 288.1   | 289.6     | 290.7            | 283.9             | 290.3           |
| $C_2N_2$  | $\mathbf{C}$ | 286.3 | 287.4 | 283.1 | 289.9 | 287.8   | 290.7     | 291.7            | 288.6             | 291.4           |
| HCN       | $\mathbf{C}$ | 286.4 | 287.4 | 284.1 | 291.2 | 285.7   | 290.8     | 291.8            | 288.7             | 291.6           |
| acetone   | C(CO)        | 286.4 | 287.2 | 283.9 | 290.8 | 288.2   | 290.4     | 291.4            | 288.3             | 291.1           |
| $C_2H_6$  | $\mathbf{C}$ | 286.9 | 290.2 | 286.4 | 292.7 | 289.2   | 291.6     | 292.8            | 289.8             | 292.2           |
| CO        | $\mathbf{C}$ | 287.4 | 289.5 | 286.4 | 292.5 | 287.4   | 292.4     | 293.1            | 289.9             | 293.4           |
| $CH_4$    | $\mathbf{C}$ | 288.0 | 290.5 | 286.6 | 292.9 | 286.6   | 291.8     | 293.0            | 290.0             | 292.4           |
| MeOH      | $\mathbf{C}$ | 288.0 | 290.8 | 287.4 | 293.9 | 287.9   | 293.0     | 294.2            | 291.2             | 293.7           |
| HCOOH     | $\mathbf{C}$ | 288.1 | 288.8 | 285.7 | 292.5 | 287.2   | 292.1     | 293.0            | 290.0             | 292.8           |
| HCOF      | $\mathbf{C}$ | 288.2 | 289.0 | 286.0 | 292.7 | 287.6   | 292.4     | 293.3            | 290.2             | 293.2           |
| $CO_2$    | $\mathbf{C}$ | 290.8 | 291.5 | 288.7 | 295.1 | 290.3   | 294.9     | 295.7            | 292.7             | 295.6           |
| $CF_2O$   | $\mathbf{C}$ | 290.9 | 291.5 | 288.6 | 295.1 | 290.1   | 294.9     | 295.6            | 292.7             | 295.5           |
| $C_2N_2$  | Ν            | 398.9 | 398.9 | 395.4 | 403.6 | 403.2   | 403.2     | 405.3            | 401.2             | 404.4           |
| HCN       | Ν            | 399.7 | 401.0 | 396.6 | 404.8 | 397.5   | 404.4     | 406.7            | 402.4             | 405.6           |
| $NH_3$    | Ν            | 400.8 | 404.9 | 400.1 | 407.5 | 399.7   | 406.7     | 409.0            | 404.9             | 407.7           |
| $N_2$     | Ν            | 400.9 | 402.5 | 398.3 | 406.4 | 404.1   | 406.1     | 408.2            | 404.0             | 407.4           |
| Glycine   | Ν            | 401.2 | 404.5 | 400.0 | 407.6 | 399.9   | 406.8     | 409.1            | 405.1             | 407.7           |
| Pyrrole   | Ν            | 402.3 | 403.8 | 399.2 | 407.4 | 399.8   | 406.8     | 409.0            | 404.9             | 407.7           |
| Imidazole | NH           | 402.3 | 403.8 | 399.3 | 407.5 | 400.0   | 406.9     | 409.1            | 405.0             | 407.8           |
| $N_2O$    | N (center)   | 404.6 | 405.7 | 401.8 | 409.5 | 403.0   | 409.3     | 411.4            | 407.3             | 410.3           |
| HCHO      | Ο            | 530.8 | 533.3 | 527.8 | 537.1 | 528.1   | 536.8     | 540.1            | 534.7             | 538.1           |
| acetone   | Ο            | 531.4 | 533.8 | 528.1 | 537.4 | 534.6   | 537.1     | 540.3            | 535.0             | 538.2           |
| HCOF      | Ο            | 532.1 | 534.5 | 529.0 | 538.2 | 529.3   | 537.9     | 541.2            | 535.9             | 539.2           |
| $CF_2O$   | Ο            | 532.7 | 535.7 | 530.2 | 539.2 | 530.4   | 539.0     | 542.2            | 537.0             | 540.3           |
| $H_2O$    | Ο            | 534.0 | 539.6 | 533.8 | 542.3 | 533.0   | 541.7     | 545.1            | 539.9             | 542.9           |
| MeOH      | Ο            | 534.1 | 538.8 | 533.0 | 541.7 | 532.4   | 541.1     | 544.5            | 539.3             | 542.3           |
| CO        | Ο            | 534.2 | 536.9 | 531.5 | 540.6 | 531.7   | 540.4     | 543.8            | 538.4             | 541.7           |
| $N_2O$    | Ο            | 534.6 | 537.1 | 531.5 | 540.7 | 531.8   | 540.4     | 543.6            | 538.4             | 541.7           |
| Furan     | Ο            | 535.2 | 537.9 | 532.2 | 541.5 | 532.2   | 541.0     | 544.3            | 539.1             | 542.1           |
| HCOOH     | OH           | 535.4 | 538.2 | 532.8 | 541.9 | 533.2   | 541.7     | 544.9            | 539.6             | 542.9           |
| $CO_2$    | Ο            | 535.4 | 538.0 | 532.5 | 541.5 | 537.9   | 541.2     | 544.5            | 539.2             | 542.5           |
| $F_2$     | F            | 682.2 | 685.5 | 679.2 | 689.5 | 685.9   | 689.4     | 693.6            | 687.2             | 690.8           |
| HF        | F            | 687.4 | 695.4 | 688.5 | 698.0 | 687.2   | 697.6     | 702.0            | 695.7             | 699.0           |
| HCOF      | F            | 687.7 | 692.7 | 686.2 | 696.4 | 686.0   | 696.3     | 700.5            | 694.1             | 697.6           |
| $CF_2O$   | F            | 689.2 | 694.4 | 687.9 | 698.1 | 691.1   | 698.0     | 702.2            | 695.8             | 699.3           |

Table S9: Excitation energies (in eV) for 37 K-edge (1s  $\rightarrow$  LUMO) transitions computed using FCHM, including relativistic corrections.

| Molecule    | Atom         | Expt. | SCAN  | SCAN0 | B3LYP | BH&HLYP | CAM-B3LYP | $LRC-\omega PBE$ | $LRC-\omega PBEh$ | $\omega B97X-V$ |
|-------------|--------------|-------|-------|-------|-------|---------|-----------|------------------|-------------------|-----------------|
| $C_2H_4$    | С            | 284.7 | 283.3 | 277.6 | 285.7 | 279.8   | 281.9     | 281.3            | 278.9             | 280.5           |
| HCHO        | $\mathbf{C}$ | 285.6 | 283.8 | 277.7 | 285.8 | 276.5   | 281.9     | 281.6            | 279.0             | 280.5           |
| $C_2H_2$    | $\mathbf{C}$ | 285.9 | 283.9 | 278.3 | 286.3 | 280.9   | 282.6     | 282.0            | 279.6             | 281.2           |
| $C_2N_2$    | $\mathbf{C}$ | 286.3 | 285.1 | 279.3 | 287.3 | 282.2   | 283.7     | 283.3            | 280.7             | 282.2           |
| HCN         | $\mathbf{C}$ | 286.4 | 284.7 | 278.7 | 286.7 | 277.6   | 282.9     | 282.5            | 280.0             | 281.5           |
| acetone     | C(CO)        | 286.4 | 284.3 | 278.4 | 286.3 | 285.7   | 282.5     | 282.3            | 279.7             | 281.1           |
| $C_2H_6$    | $\mathbf{C}$ | 286.9 | 287.7 | 282.8 | 290.2 | 285.5   | 287.3     | 287.2            | 284.3             | 286.7           |
| CO          | $\mathbf{C}$ | 287.4 | 285.6 | 279.4 | 286.9 | 277.6   | 283.2     | 282.9            | 280.2             | 281.9           |
| $CH_4$      | $\mathbf{C}$ | 288.0 | 287.8 | 282.9 | 290.3 | 282.6   | 287.4     | 287.2            | 284.4             | 286.7           |
| MeOH        | $\mathbf{C}$ | 288.0 | 288.7 | 283.9 | 291.2 | 283.8   | 288.3     | 287.7            | 285.1             | 287.4           |
| HCOOH       | $\mathbf{C}$ | 288.1 | 286.0 | 280.0 | 287.8 | 278.7   | 284.0     | 283.7            | 281.1             | 282.6           |
| HCOF        | $\mathbf{C}$ | 288.2 | 286.1 | 280.0 | 287.8 | 278.7   | 284.0     | 283.7            | 281.1             | 282.6           |
| $CO_2$      | $\mathbf{C}$ | 290.8 | 288.2 | 282.4 | 289.9 | 281.1   | 286.3     | 285.9            | 283.4             | 284.9           |
| $CF_2O$     | $\mathbf{C}$ | 290.9 | 288.2 | 282.2 | 289.8 | 280.7   | 286.0     | 285.6            | 283.1             | 284.6           |
| $C_2N_2$    | Ν            | 398.9 | 398.0 | 391.0 | 400.2 | 389.7   | 396.7     | 397.3            | 393.7             | 395.6           |
| HCN         | Ν            | 399.7 | 398.3 | 391.3 | 400.5 | 389.8   | 396.8     | 397.5            | 393.8             | 395.8           |
| $NH_3$      | Ν            | 400.8 | 401.9 | 395.7 | 404.4 | 395.0   | 401.5     | 402.1            | 398.3             | 400.9           |
| $N_2$       | Ν            | 400.9 | 399.4 | 392.0 | 401.3 | 394.4   | 397.5     | 398.4            | 394.6             | 396.4           |
| Glycine     | Ν            | 401.2 | 402.4 | 396.4 | 405.0 | 395.7   | 402.1     | 404.7            | 401.1             | 401.3           |
| Pyrrole     | Ν            | 402.3 | 402.5 | 396.1 | 405.0 | 396.8   | 403.2     | 403.7            | 400.1             | 402.3           |
| Imidazole   | NH           | 402.3 | 402.6 | 396.1 | 405.0 | 397.0   | 403.5     | 404.0            | 400.4             | 402.6           |
| $N_2O$      | N (center)   | 404.6 | 402.9 | 395.7 | 404.8 | 394.0   | 401.1     | 402.0            | 398.3             | 400.0           |
| HCHO        | Ο            | 530.8 | 531.2 | 523.0 | 533.5 | 521.1   | 529.9     | 531.5            | 526.8             | 528.9           |
| acetone     | Ο            | 531.4 | 531.8 | 523.8 | 534.2 | 521.9   | 530.6     | 532.3            | 527.5             | 529.7           |
| HCOF        | Ο            | 532.1 | 532.7 | 524.4 | 534.8 | 522.4   | 531.2     | 532.9            | 528.1             | 530.2           |
| $CF_2O$     | Ο            | 532.7 | 533.8 | 525.6 | 535.9 | 523.4   | 532.2     | 534.0            | 529.2             | 531.3           |
| $H_2O$      | Ο            | 534.0 | 536.2 | 528.8 | 538.7 | 527.4   | 535.7     | 537.2            | 532.4             | 535.0           |
| MeOH        | Ο            | 534.1 | 536.4 | 529.0 | 538.9 | 527.6   | 535.9     | 537.4            | 532.7             | 535.2           |
| CO          | Ο            | 534.2 | 534.6 | 526.3 | 536.7 | 524.1   | 533.0     | 534.8            | 530.0             | 532.0           |
| $N_2O$      | Ο            | 534.6 | 536.2 | 527.9 | 538.3 | 525.7   | 534.6     | 536.4            | 531.6             | 533.7           |
| Furan       | Ο            | 535.2 | 536.7 | 529.1 | 539.1 | 527.4   | 535.7     | 537.4            | 536.9             | 534.9           |
| HCOOH       | OH           | 535.4 | 537.9 | 530.0 | 540.1 | 529.1   | 537.4     | 538.8            | 534.2             | 536.6           |
| $CO_2$      | Ο            | 535.4 | 536.4 | 529.9 | 538.4 | 530.6   | 536.9     | 538.5            | 533.8             | 536.2           |
| $F_2$       | F            | 682.2 | 683.3 | 672.7 | 684.8 | 674.3   | 681.0     | 684.6            | 678.0             | 680.1           |
| $_{\rm HF}$ | F            | 687.4 | 691.8 | 683.0 | 694.3 | 680.9   | 691.0     | 693.5            | 687.7             | 690.1           |
| HCOF        | F            | 687.7 | 692.6 | 683.5 | 694.8 | 681.0   | 691.3     | 694.0            | 688.2             | 690.4           |
| $CF_2O$     | F            | 689.2 | 694.3 | 685.1 | 696.4 | 685.5   | 693.2     | 695.8            | 690.0             | 692.6           |

Table S10: Excitation energies (in eV) for 37 K-edge (1s  $\rightarrow$  LUMO) transitions computed using XCHM, including relativistic corrections.

| Molecule   | Atom         | Expt. | SCAN  | SCAN0 | B3LYP | BH&HLYP | CAM-B3LYP | $LRC-\omega PBE$ | $LRC-\omega PBEh$ | $\omega B97X-V$ |
|------------|--------------|-------|-------|-------|-------|---------|-----------|------------------|-------------------|-----------------|
| $C_2H_4$   | С            | 284.7 | 285.7 | 285.2 | 286.4 | 288.3   | 287.8     | 287.8            | 287.8             | 289.3           |
| HCHO       | $\mathbf{C}$ | 285.6 | 286.9 | 288.2 | 287.8 | 290.0   | 289.4     | 289.2            | 289.2             | 290.9           |
| $C_2H_2$   | $\mathbf{C}$ | 285.9 | 286.8 | 286.4 | 287.5 | 289.5   | 288.9     | 288.8            | 288.9             | 290.3           |
| $C_2N_2$   | $\mathbf{C}$ | 286.3 | 287.1 | 285.9 | 282.9 | 289.2   | 289.4     | 289.2            | 289.3             | 290.9           |
| HCN        | $\mathbf{C}$ | 286.4 | 287.5 | 288.9 | 288.4 | 290.5   | 289.9     | 289.8            | 289.8             | 291.4           |
| acetone    | C(CO)        | 286.4 | 287.6 | 288.9 | 288.4 | 290.5   | 289.9     | 289.7            | 289.8             | 291.5           |
| $C_2H_6$   | $\mathbf{C}$ | 286.9 | 288.7 | 289.2 | 288.3 | 289.0   | 289.1     | 289.6            | 289.2             | 290.3           |
| CO         | $\mathbf{C}$ | 287.4 | 288.5 | 290.1 | 289.5 | 291.9   | 291.2     | 290.8            | 290.9             | 292.7           |
| $CH_4$     | $\mathbf{C}$ | 288.0 | 288.8 | 289.2 | 288.3 | 289.4   | 289.0     | 288.9            | 289.1             | 290.2           |
| MeOH       | $\mathbf{C}$ | 288.0 | 289.9 | 290.6 | 289.7 | 290.9   | 290.5     | 290.5            | 290.6             | 291.8           |
| HCOOH      | $\mathbf{C}$ | 288.1 | 289.2 | 290.6 | 290.0 | 292.3   | 291.6     | 291.4            | 291.4             | 293.2           |
| HCOF       | $\mathbf{C}$ | 288.2 | 289.4 | 290.9 | 290.3 | 292.7   | 291.9     | 291.7            | 291.7             | 293.6           |
| $CO_2$     | $\mathbf{C}$ | 290.8 | 291.7 | 293.4 | 292.5 | 295.2   | 294.2     | 293.8            | 294.0             | 295.8           |
| CF2O       | $\mathbf{C}$ | 290.9 | 292.1 | 293.7 | 292.9 | 295.5   | 294.6     | 294.2            | 294.3             | 296.2           |
| $C_2N_2$   | Ν            | 398.9 | 399.7 | 400.8 | 400.3 | 402.3   | 401.8     | 401.7            | 401.7             | 403.4           |
| HCN        | Ν            | 399.7 | 400.9 | 402.2 | 401.6 | 403.6   | 403.1     | 403.0            | 403.1             | 404.7           |
| $NH_3$     | Ν            | 400.8 | 402.8 | 403.4 | 402.4 | 403.6   | 403.3     | 403.3            | 403.5             | 404.7           |
| $N_2$      | Ν            | 400.9 | 402.2 | 402.0 | 403.0 | 405.8   | 404.8     | 404.5            | 404.6             | 406.4           |
| Glycine    | Ν            | 401.2 | 402.0 | 403.1 | 402.5 | 403.9   | 403.6     | 403.6            | 403.8             | 405.0           |
| Pyrrole    | Ν            | 402.3 | 402.8 | 403.9 | 403.4 | 404.9   | 404.6     | 404.6            | 404.7             | 405.9           |
| Imidazole  | NH           | 402.3 | 402.9 | 404.0 | 403.5 | 405.2   | 404.8     | 404.9            | 404.9             | 406.2           |
| $N_2O$     | N (center)   | 404.6 | 405.7 | 407.1 | 406.4 | 408.9   | 408.1     | 407.9            | 408.0             | 409.7           |
| HCHO       | О            | 530.8 | 532.1 | 533.3 | 532.7 | 534.6   | 534.3     | 534.2            | 534.2             | 535.8           |
| acetone    | О            | 531.4 | 532.3 | 533.3 | 532.8 | 534.7   | 534.4     | 534.2            | 534.2             | 535.9           |
| HCOF       | О            | 532.1 | 533.1 | 534.3 | 533.6 | 535.6   | 535.3     | 535.2            | 535.1             | 536.9           |
| $CF_2O$    | О            | 532.7 | 534.1 | 535.3 | 534.5 | 536.7   | 536.2     | 536.1            | 536.1             | 537.9           |
| $H_2O$     | О            | 534.0 | 536.5 | 537.1 | 535.9 | 537.3   | 537.1     | 537.0            | 537.1             | 538.4           |
| MeOH       | О            | 534.1 | 536.1 | 536.8 | 535.7 | 537.0   | 536.8     | 536.8            | 536.9             | 538.1           |
| CO         | О            | 534.2 | 535.4 | 536.7 | 536.0 | 538.0   | 537.7     | 537.6            | 537.6             | 539.2           |
| $N_2O$     | О            | 534.6 | 535.6 | 536.7 | 536.0 | 537.9   | 537.6     | 537.5            | 537.5             | 539.1           |
| Furan      | О            | 535.2 | 535.8 | 536.8 | 536.2 | 537.8   | 537.6     | 537.6            | 537.7             | 539.1           |
| HCOOH      | OH           | 535.4 | 535.8 | 537.0 | 536.3 | 538.4   | 537.9     | 537.7            | 537.8             | 539.5           |
| $CO_2$     | Ο            | 535.4 | 536.5 | 537.7 | 536.8 | 539.0   | 538.5     | 538.4            | 538.3             | 539.9           |
| $F_2$      | F            | 682.2 | 684.1 | 685.7 | 684.9 | 688.6   | 686.8     | 686.4            | 686.5             | 688.3           |
| $_{ m HF}$ | F            | 687.4 | 690.5 | 691.1 | 689.8 | 691.3   | 691.1     | 691.1            | 691.1             | 692.5           |
| HCOF       | $\mathbf{F}$ | 687.7 | 688.3 | 689.5 | 688.7 | 690.8   | 690.5     | 690.2            | 690.2             | 691.9           |
| $CF_2O$    | F            | 689.2 | 690.0 | 691.2 | 690.3 | 692.0   | 692.1     | 691.8            | 691.8             | 693.7           |

Table S11: Excitation energies (in eV) for 37 K-edge (1s  $\rightarrow$  LUMO) transitions computed using IP-TPM@1/2, including relativistic corrections.

| Molecule   | Atom         | Expt. | SCAN  | SCAN0 | B3LYP | BH&HLYP | CAM-B3LYP | $LRC-\omega PBE$ | $LRC-\omega PBEh$ | $\omega B97X-V$ |
|------------|--------------|-------|-------|-------|-------|---------|-----------|------------------|-------------------|-----------------|
| $C_2H_4$   | С            | 284.7 | 284.2 | 283.6 | 284.9 | 286.8   | 286.3     | 286.3            | 286.3             | 287.8           |
| HCHO       | С            | 285.6 | 285.2 | 286.6 | 285.9 | 288.2   | 287.5     | 287.3            | 287.4             | 289.1           |
| $C_2H_2$   | С            | 285.9 | 285.1 | 284.9 | 285.9 | 287.9   | 287.2     | 287.2            | 287.2             | 288.8           |
| $C_2N_2$   | С            | 286.3 | 285.5 | 284.2 | 281.5 | 287.8   | 288.2     | 287.7            | 287.7             | 289.7           |
| HCN        | С            | 286.4 | 285.6 | 287.0 | 286.5 | 288.7   | 288.1     | 287.9            | 288.0             | 289.6           |
| acetone    | C(CO)        | 286.4 | 286.0 | 287.3 | 286.8 | 288.9   | 288.3     | 288.1            | 288.2             | 289.8           |
| C2H6       | $\mathbf{C}$ | 286.9 | 287.7 | 288.4 | 287.4 | 288.1   | 288.2     | 288.1            | 288.4             | 289.5           |
| CO         | $\mathbf{C}$ | 287.4 | 286.3 | 287.8 | 287.2 | 289.7   | 288.9     | 288.6            | 288.7             | 290.5           |
| $CH_4$     | $\mathbf{C}$ | 288.0 | 287.7 | 288.2 | 287.2 | 288.4   | 288.0     | 287.9            | 288.1             | 289.3           |
| MeOH       | $\mathbf{C}$ | 288.0 | 288.7 | 289.5 | 288.6 | 290.0   | 289.6     | 289.5            | 289.6             | 290.9           |
| HCOOH      | $\mathbf{C}$ | 288.1 | 287.4 | 288.8 | 288.2 | 290.5   | 289.8     | 289.5            | 289.6             | 291.3           |
| HCOF       | $\mathbf{C}$ | 288.2 | 287.5 | 289.0 | 288.4 | 290.8   | 290.0     | 289.7            | 289.8             | 291.6           |
| $CO_2$     | $\mathbf{C}$ | 290.8 | 289.7 | 291.3 | 290.4 | 293.1   | 292.2     | 291.8            | 291.9             | 293.7           |
| $CF_2O$    | $\mathbf{C}$ | 290.9 | 290.1 | 291.7 | 290.9 | 293.5   | 292.6     | 292.2            | 292.3             | 294.2           |
| $C_2N_2$   | Ν            | 398.9 | 398.2 | 399.3 | 398.8 | 400.8   | 400.3     | 400.2            | 400.2             | 401.9           |
| HCN        | Ν            | 399.7 | 399.0 | 400.3 | 399.7 | 401.8   | 401.3     | 401.2            | 401.3             | 402.9           |
| $NH_3$     | Ν            | 400.8 | 401.6 | 402.2 | 401.1 | 402.5   | 402.1     | 402.2            | 402.3             | 403.5           |
| $N_2$      | Ν            | 400.9 | 400.0 | 399.8 | 400.9 | 403.6   | 402.5     | 402.3            | 402.4             | 404.2           |
| Glycine    | Ν            | 401.2 | 401.1 | 402.2 | 401.6 | 403.0   | 402.6     | 402.7            | 402.8             | 404.1           |
| Pyrrole    | Ν            | 402.3 | 401.7 | 402.7 | 402.2 | 403.8   | 403.5     | 403.5            | 403.6             | 405.0           |
| Imidazole  | NH           | 402.3 | 401.7 | 402.7 | 402.2 | 402.5   | 403.6     | 403.6            | 403.7             | 405.1           |
| $N_2O$     | N (center)   | 404.6 | 403.7 | 405.1 | 404.5 | 404.5   | 406.2     | 405.9            | 406.1             | 407.8           |
| HCHO       | О            | 530.8 | 530.3 | 531.5 | 530.9 | 532.9   | 532.6     | 532.5            | 532.4             | 534.1           |
| acetone    | О            | 531.4 | 530.8 | 531.9 | 531.3 | 533.2   | 532.9     | 532.8            | 532.8             | 534.4           |
| HCOF       | О            | 532.1 | 531.4 | 532.5 | 531.9 | 533.9   | 533.6     | 533.4            | 533.4             | 535.2           |
| $CF_2O$    | О            | 532.7 | 532.4 | 533.5 | 532.8 | 534.9   | 534.5     | 534.4            | 534.4             | 536.2           |
| $H_2O$     | О            | 534.0 | 535.0 | 535.7 | 534.5 | 536.0   | 535.7     | 535.7            | 535.8             | 537.1           |
| MeOH       | О            | 534.1 | 534.8 | 535.6 | 534.5 | 535.9   | 535.6     | 535.7            | 535.7             | 537.0           |
| CO         | О            | 534.2 | 533.4 | 534.7 | 534.0 | 536.1   | 535.8     | 535.7            | 535.6             | 537.3           |
| $N_2O$     | О            | 534.6 | 533.9 | 535.0 | 534.4 | 536.3   | 535.9     | 535.8            | 535.9             | 537.5           |
| Furan      | О            | 535.2 | 534.6 | 535.6 | 535.0 | 536.6   | 536.4     | 536.4            | 536.4             | 537.9           |
| HCOOH      | OH           | 535.4 | 534.4 | 535.6 | 534.9 | 534.7   | 536.5     | 536.4            | 536.4             | 538.1           |
| $CO_2$     | О            | 535.4 | 534.7 | 535.9 | 535.1 | 537.8   | 536.7     | 536.6            | 536.6             | 538.2           |
| $F_2$      | F            | 682.2 | 681.6 | 683.2 | 682.5 | 686.1   | 684.4     | 683.9            | 684.0             | 685.9           |
| $_{ m HF}$ | F            | 687.4 | 688.8 | 689.5 | 688.1 | 689.7   | 689.5     | 689.5            | 689.5             | 690.9           |
| HCOF       | F            | 687.7 | 686.9 | 688.0 | 687.3 | 689.4   | 689.0     | 688.8            | 688.8             | 690.5           |
| $CF_2O$    | F            | 689.2 | 688.5 | 689.7 | 688.8 | 690.5   | 690.6     | 690.4            | 690.3             | 692.2           |

Table S12: Excitation energies (in eV) for 37 K-edge (1s  $\rightarrow$  LUMO) transitions computed using IP-TPM@1/3, including relativistic corrections.

| Molecule    | Atom         | Expt. | SCAN  | SCAN0 | B3LYP | BH&HLYP | CAM-B3LYP | $LRC-\omega PBE$ | $LRC-\omega PBEh$ | $\omega$ B97X-V |
|-------------|--------------|-------|-------|-------|-------|---------|-----------|------------------|-------------------|-----------------|
| $C_2H_4$    | С            | 284.7 | 284.6 | 285.3 | 285.3 | 284.2   | 285.1     | 284.6            | 284.8             | 285.4           |
| HCHO        | $\mathbf{C}$ | 285.6 | 285.7 | 286.4 | 286.2 | 285.7   | 286.1     | 285.5            | 285.7             | 286.4           |
| $C_2H_2$    | $\mathbf{C}$ | 285.9 | 285.6 | 286.3 | 286.2 | 285.6   | 286.1     | 285.5            | 285.7             | 286.3           |
| $C_2N_2$    | $\mathbf{C}$ | 286.3 | 286.1 | 286.7 | 286.8 | 286.7   | 286.6     | 286.1            | 286.5             | 286.7           |
| HCN         | $\mathbf{C}$ | 286.4 | 286.3 | 286.9 | 286.8 | 286.6   | 286.6     | 286.1            | 286.2             | 286.7           |
| acetone     | C(CO)        | 286.4 | 286.3 | 287.1 | 286.8 | 287.1   | 286.7     | 286.2            | 286.4             | 286.9           |
| $C_2H_6$    | $\mathbf{C}$ | 286.9 | 286.8 | 283.6 | 287.6 | 287.5   | 287.5     | 287.2            | 287.1             | 287.6           |
| CO          | $\mathbf{C}$ | 287.4 | 286.7 | 287.5 | 287.3 | 286.8   | 287.2     | 286.6            | 286.8             | 287.4           |
| $CH_4$      | $\mathbf{C}$ | 288.0 | 286.6 | 287.2 | 287.4 | 288.3   | 287.1     | 286.9            | 286.8             | 287.0           |
| MeOH        | $\mathbf{C}$ | 288.0 | 288.2 | 288.8 | 288.9 | 289.9   | 288.7     | 288.4            | 288.3             | 288.6           |
| HCOOH       | $\mathbf{C}$ | 288.1 | 287.9 | 288.6 | 288.3 | 287.9   | 288.2     | 287.6            | 287.8             | 288.3           |
| HCOF        | $\mathbf{C}$ | 288.2 | 288.0 | 288.8 | 288.5 | 287.9   | 288.5     | 287.8            | 288.1             | 288.7           |
| $CO_2$      | $\mathbf{C}$ | 290.8 | 290.0 | 290.7 | 290.5 | 290.6   | 290.3     | 292.7            | 292.9             | 292.8           |
| $CF_2O$     | $\mathbf{C}$ | 290.9 | 290.5 | 291.3 | 290.9 | 291.6   | 290.8     | 290.1            | 290.4             | 291.0           |
| $C_2N_2$    | Ν            | 398.9 | 398.7 | 399.4 | 399.3 | 400.1   | 399.2     | 398.6            | 398.7             | 399.1           |
| HCN         | Ν            | 399.7 | 399.5 | 400.3 | 400.1 | 399.6   | 399.9     | 399.3            | 399.5             | 399.8           |
| $NH_3$      | Ν            | 400.8 | 400.5 | 401.2 | 401.2 | 401.9   | 401.0     | 400.7            | 400.6             | 400.8           |
| $N_2$       | Ν            | 400.9 | 400.7 | 401.5 | 401.2 | 399.8   | 401.1     | 400.5            | 400.6             | 401.2           |
| Glycine     | Ν            | 401.2 | 401.9 | 402.5 | 402.8 | 402.8   | 402.3     | 402.0            | 402.0             | 401.5           |
| Pyrrole     | Ν            | 402.3 | 402.1 | 402.5 | 403.0 | 403.7   | 402.8     | 402.4            | 402.4             | 402.4           |
| Imidazole   | NH           | 402.3 | 402.1 | 402.6 | 402.7 | 403.9   | 403.0     | 402.7            | 402.6             | 402.7           |
| N2O         | N (center)   | 404.6 | 404.4 | 405.2 | 404.7 | 403.7   | 404.6     | 404.1            | 404.2             | 404.8           |
| HCHO        | О            | 530.8 | 530.8 | 531.4 | 531.3 | 530.4   | 531.1     | 530.5            | 530.7             | 530.9           |
| acetone     | О            | 531.4 | 531.1 | 531.6 | 531.6 | 530.9   | 531.3     | 530.8            | 530.9             | 531.0           |
| HCOF        | О            | 532.1 | 531.9 | 532.4 | 532.4 | 532.9   | 532.1     | 531.6            | 531.7             | 531.9           |
| $CF_2O$     | О            | 532.7 | 532.8 | 533.4 | 533.3 | 532.5   | 533.0     | 532.5            | 532.6             | 532.7           |
| $H_2O$      | О            | 534.0 | 533.9 | 534.5 | 534.6 | 535.1   | 534.3     | 533.8            | 533.8             | 533.7           |
| MeOH        | О            | 534.1 | 534.0 | 534.6 | 534.7 | 535.4   | 534.4     | 534.0            | 533.9             | 533.8           |
| CO          | О            | 534.2 | 534.0 | 534.6 | 534.5 | 533.6   | 534.3     | 533.8            | 533.9             | 534.0           |
| $N_2O$      | О            | 534.6 | 534.8 | 535.2 | 535.2 | 534.3   | 534.8     | 534.4            | 534.5             | 534.0           |
| Furan       | О            | 535.2 | 534.9 | 535.5 | 535.5 | 535.4   | 535.1     | 534.7            | 534.8             | 534.8           |
| HCOOH       | OH           | 535.4 | 535.1 | 535.6 | 535.7 | 535.9   | 535.3     | 534.8            | 534.8             | 534.6           |
| $CO_2$      | О            | 535.4 | 535.3 | 536.7 | 535.6 | 538.5   | 536.2     | 535.7            | 536.4             | 536.5           |
| $F_2$       | F            | 682.2 | 682.5 | 683.2 | 682.9 | 680.9   | 682.7     | 682.2            | 682.5             | 682.4           |
| $_{\rm HF}$ | F            | 687.4 | 687.4 | 687.9 | 688.0 | 688.6   | 687.7     | 687.1            | 687.1             | 686.7           |
| HCOF        | F            | 687.7 | 687.5 | 687.9 | 688.2 | 688.3   | 687.8     | 687.2            | 687.2             | 686.9           |
| $CF_2O$     | F            | 689.2 | 689.1 | 689.5 | 689.7 | 690.0   | 689.1     | 688.6            | 688.6             | 688.0           |

Table S13: Excitation energies (in eV) for 37 K-edge (1s  $\rightarrow$  LUMO) transitions computed using the empirically-shifted XTPM approach, including relativistic corrections.

Table S14: Excitation energies (in eV) for 20 higher-lying transitions computed using XCHM, including relativistic corrections.

| Molecules           | Orbitals     | Transitions                 | Expt.               | SCAN   | SCAN0  | B3LYP  | BH&HLYP | CAM-B3LYP | $LRC-\omega PBE$ | $LRC-\omega PBEh$ | $\omega B97X-V$ |
|---------------------|--------------|-----------------------------|---------------------|--------|--------|--------|---------|-----------|------------------|-------------------|-----------------|
| NH <sub>3</sub>     | Ν            | $1s \rightarrow 3p(E)$      | $402.33^{7}$        | 403.92 | 398.99 | 407.27 | 399.30  | 406.40    | 408.49           | 404.40            | 407.22          |
| NH <sub>3</sub>     | Ν            | $1s \rightarrow 3p(A_1)$    | $402.86^{7}$        | 403.92 | 398.99 | 407.27 | 399.30  | 406.40    | 408.49           | 404.40            | 407.22          |
| NH <sub>3</sub>     | Ν            | $1s \rightarrow 4s(A_1)$    | $403.57^{7}$        | 405.67 | 400.42 | 408.70 | 400.47  | 407.59    | 409.63           | 405.59            | 408.29          |
| HCHO (formaldehyde) | С            | $1s \rightarrow 3s$         | 290.18 <sup>3</sup> | 288.67 | 284.58 | 291.28 | 284.59  | 290.01    | 290.97           | 288.04            | 290.25          |
| HCHO (formaldehyde) | С            | $1s \rightarrow 3p(B_2)$    | 291.25 <sup>3</sup> | 290.00 | 285.84 | 292.48 | 285.76  | 291.16    | 292.10           | 289.19            | 291.40          |
| HCHO (formaldehyde) | С            | $1s \rightarrow 3p(B_1)$    | 291.73 <sup>3</sup> | 290.20 | 285.98 | 292.80 | 285.95  | 291.38    | 292.22           | 289.31            | 291.53          |
| HCHO (formaldehyde) | 0            | $1s \rightarrow 3s$         | 535.43 <sup>3</sup> | 536.34 | 529.82 | 538.94 | 528.73  | 537.70    | 540.71           | 535.61            | 538.30          |
| HCHO (formaldehyde) | 0            | $1s \rightarrow 3p$         | 536.34 <sup>3</sup> | 537.25 | 530.75 | 539.91 | 529.69  | 538.63    | 541.60           | 536.51            | 539.22          |
| CO                  | С            | $1s \rightarrow 3s\sigma$   | 292.37 <sup>6</sup> | 291.56 | 287.15 | 293.37 | 286.58  | 292.02    | 292.70           | 289.78            | 295.19          |
| CO                  | С            | $1s \rightarrow 3p\pi$      | 293.33 <sup>6</sup> | 292.50 | 288.09 | 294.39 | 287.58  | 292.99    | 293.64           | 290.74            | 295.62          |
| CO                  | $\mathbf{C}$ | $1s \rightarrow 3p\sigma$   | $293.49^{6}$        | 292.80 | 288.35 | 294.49 | 287.70  | 293.14    | 293.84           | 290.92            | 295.98          |
| CO                  | 0            | $1s \rightarrow 3s$         | $538.91^{16}$       | 539.58 | 532.90 | 541.91 | 531.57  | 540.59    | 543.58           | 538.44            | 543.85          |
| CO                  | 0            | $1s \rightarrow 3p\pi$      | $539.91^{16}$       | 540.62 | 533.92 | 542.99 | 532.62  | 541.64    | 544.61           | 539.49            | 545.00          |
| $N_2$               | Ν            | $1s \rightarrow 3s\sigma_q$ | $406.1^{17}$        | 405.86 | 400.46 | 408.15 | 399.73  | 407.03    | 409.25           | 405.14            | 407.75          |
| $N_2$               | Ν            | $1s \rightarrow 3p\pi_u$    | 407 <sup>17</sup>   | 406.48 | 400.91 | 408.64 | 400.07  | 407.32    | 409.32           | 405.25            | 407.83          |
| $N_2O$              | NC           | $1s \rightarrow 3p\sigma$   | $407.6^{17}$        | 407.17 | 402.30 | 410.11 | 402.43  | 409.16    | 411.28           | 407.26            | 412.23          |
| $C_2H_4$ (ethylene) | С            | $1s \rightarrow 3s$         | $287.24^{18}$       | 286.41 | 282.26 | 289.05 | 282.88  | 288.11    | 289.27           | 286.11            | 288.96          |
| $C_2H_4$ (ethylene) | $\mathbf{C}$ | $1s \rightarrow 3p\pi$      | $287.88^{18}$       | 287.17 | 282.93 | 289.76 | 285.39  | 290.77    | 291.76           | 288.77            | 289.74          |
| $H_2O$              | 0            | $1s \rightarrow 2b_1/3p$    | 535.9 <sup>7</sup>  | 538.09 | 532.06 | 541.49 | 531.78  | 540.65    | 543.71           | 538.57            | 541.45          |
| $H_2O$              | 0            | $1s \rightarrow 3p$ (B2)    | 537 <mark>7</mark>  | 540.26 | 533.74 | 543.05 | 533.02  | 541.88    | 544.85           | 539.76            | 542.51          |

Table S15: Excitation energies (in eV) for 20 higher-lying transitions computed using XTPM, including relativistic corrections.

| Molecules           | Orbitals     | Expt.  | SCAN   | SCAN0  | B3LYP  | BH&HLYP | CAM-B3LYP | $LRC-\omega PBE$ | $LRC-\omega PBEh$ | $\omega B97X-V$ |
|---------------------|--------------|--------|--------|--------|--------|---------|-----------|------------------|-------------------|-----------------|
| NH <sub>3</sub>     | Ν            | 402.33 | 405.23 | 405.30 | 404.19 | 405.01  | 405.28    | 405.64           | 405.49            | 406.66          |
| $NH_3$              | Ν            | 402.86 | 405.23 | 405.30 | 404.19 | 405.01  | 405.28    | 405.64           | 405.49            | 406.66          |
| $NH_3$              | Ν            | 403.57 | 406.54 | 406.35 | 405.26 | 405.90  | 406.18    | 406.45           | 406.34            | 407.45          |
| HCHO (formaldehyde) | $\mathbf{C}$ | 290.18 | 291.75 | 291.76 | 290.34 | 291.04  | 291.10    | 291.23           | 291.20            | 292.22          |
| HCHO (formaldehyde) | $\mathbf{C}$ | 291.25 | 293.15 | 293.07 | 291.57 | 292.24  | 292.28    | 292.37           | 292.37            | 293.38          |
| HCHO (formaldehyde) | $\mathbf{C}$ | 291.73 | 293.16 | 293.10 | 291.70 | 292.33  | 292.36    | 292.39           | 292.39            | 293.41          |
| HCHO (formaldehyde) | О            | 535.43 | 537.77 | 537.26 | 535.67 | 535.89  | 536.47    | 536.68           | 536.49            | 532.61          |
| HCHO (formaldehyde) | Ο            | 536.34 | 538.89 | 538.40 | 536.81 | 537.03  | 537.56    | 537.70           | 537.52            | 532.61          |
| CO                  | С            | 292.37 | 293.20 | 293.17 | 291.71 | 292.39  | 292.35    | 292.19           | 292.27            | 293.24          |
| CO                  | С            | 293.33 | 294.16 | 294.13 | 292.73 | 293.41  | 293.34    | 293.15           | 293.24            | 294.23          |
| CO                  | С            | 293.49 | 294.40 | 294.31 | 292.81 | 293.50  | 293.45    | 293.33           | 293.40            | 294.38          |
| CO                  | Ο            | 538.91 | 540.94 | 540.37 | 538.68 | 538.88  | 539.38    | 539.46           | 539.30            | 540.29          |
| CO                  | Ο            | 539.91 | 541.91 | 541.35 | 539.74 | 539.94  | 540.42    | 540.48           | 540.32            | 541.31          |
| $N_2$               | Ν            | 406.10 | 408.27 | 406.13 | 406.34 | 410.03  | 407.26    | 402.33           | 407.46            | 408.51          |
| $N_2$               | Ν            | 407.00 | 408.77 | 406.51 | 406.81 | 410.35  | 407.53    | 402.33           | 407.54            | 408.55          |
| $N_2O$              | NC           | 407.60 | 409.85 | 410.17 | 408.33 | 409.62  | 409.44    | 409.64           | 409.59            | 410.70          |
| $C_2H_4$ (ethylene) | С            | 287.24 | 289.23 | 287.15 | 287.85 | 290.62  | 288.55    | 288.82           | 288.75            | 289.73          |
| $C_2H_4$ (ethylene) | С            | 287.88 | 289.78 | 287.63 | 288.38 | 291.06  | 289.02    | 289.21           | 289.16            | 290.13          |
| H <sub>2</sub> O    | 0            | 535.90 | 538.85 | 538.77 | 537.34 | 538.00  | 538.41    | 538.61           | 538.41            | 539.55          |
| H <sub>2</sub> O    | Ο            | 537.00 | 540.42 | 539.96 | 538.47 | 538.90  | 539.30    | 539.42           | 539.26            | 540.32          |

Table S16: Excitation energies (in eV) for 20 higher-lying transitions computed using XGTPM, including relativistic corrections.

| Molecules           | Orbitals     | Expt.  | SCAN   | SCAN0  | B3LYP  | BH&HLYP | CAM-B3LYP | $LRC-\omega PBE$ | $LRC-\omega PBEh$ | $\omega B97X-V$ |
|---------------------|--------------|--------|--------|--------|--------|---------|-----------|------------------|-------------------|-----------------|
| NH <sub>3</sub>     | Ν            | 402.33 | 403.83 | 404.20 | 403.38 | 404.44  | 404.39    | 404.49           | 404.51            | 405.70          |
| $NH_3$              | Ν            | 402.86 | 403.84 | 404.20 | 403.38 | 404.44  | 404.40    | 404.49           | 404.51            | 405.70          |
| $NH_3$              | Ν            | 403.57 | 405.13 | 405.26 | 404.46 | 405.34  | 405.31    | 405.35           | 405.40            | 406.52          |
| HCHO (formaldehyde) | $\mathbf{C}$ | 290.18 | 290.33 | 290.56 | 289.52 | 290.39  | 290.24    | 290.17           | 290.26            | 291.30          |
| HCHO (formaldehyde) | $\mathbf{C}$ | 291.25 | 291.65 | 291.82 | 290.74 | 291.58  | 291.41    | 291.30           | 291.41            | 292.45          |
| HCHO (formaldehyde) | $\mathbf{C}$ | 291.73 | 291.75 | 291.89 | 290.89 | 291.67  | 291.51    | 291.34           | 291.46            | 292.50          |
| HCHO (formaldehyde) | Ο            | 535.43 | 536.06 | 535.94 | 534.82 | 535.35  | 535.56    | 535.51           | 535.51            | 536.54          |
| HCHO (formaldehyde) | 0            | 536.34 | 537.14 | 537.04 | 535.94 | 536.46  | 536.64    | 536.51           | 536.53            | 537.58          |
| CO                  | С            | 292.37 | 291.80 | 291.98 | 290.89 | 291.74  | 291.48    | 291.13           | 291.32            | 293.07          |
| CO                  | С            | 293.33 | 292.74 | 292.93 | 291.92 | 292.76  | 292.48    | 292.10           | 292.31            | 294.03          |
| CO                  | С            | 293.49 | 293.10 | 293.21 | 291.99 | 292.84  | 292.59    | 292.27           | 292.46            | 294.18          |
| CO                  | 0            | 538.91 | 539.21 | 539.01 | 537.77 | 538.26  | 538.43    | 538.25           | 538.27            | 540.03          |
| CO                  | 0            | 539.91 | 540.18 | 539.98 | 538.84 | 539.32  | 539.47    | 539.27           | 539.30            | 541.02          |
| $N_2$               | Ν            | 406.10 | 406.65 | 405.91 | 407.16 | 409.82  | 404.44    | 402.11           | 405.09            | 406.32          |
| $N_2$               | Ν            | 407.00 | 407.20 | 406.30 | 407.98 | 410.14  | 404.71    | 402.14           | 405.17            | 406.36          |
| N2O                 | NC           | 407.60 | 408.21 | 407.07 | 407.48 | 408.77  | 408.54    | 408.51           | 408.61            | 410.39          |
| $C_2H_4$ (ethylene) | С            | 287.24 | 287.85 | 287.02 | 287.08 | 290.47  | 287.74    | 284.55           | 287.88            | 289.17          |
| $C_2H_4$ (ethylene) | $\mathbf{C}$ | 287.88 | 288.45 | 287.50 | 287.63 | 290.86  | 288.20    | 284.83           | 288.27            | 289.60          |
| H <sub>2</sub> O    | 0            | 535.90 | 537.11 | 537.38 | 536.45 | 537.37  | 537.42    | 537.31           | 537.32            | 538.48          |
| $H_2O$              | 0            | 537.00 | 538.66 | 538.60 | 537.56 | 538.28  | 538.33    | 538.17           | 538.20            | 539.28          |

| Molecules           | Orbitals     | Expt.  | SCAN   | SCAN0  | B3LYP  | BH&HLYP | CAM-B3LYP | $LRC-\omega PBE$ | $LRC-\omega PBEh$ | $\omega B97X-V$ |
|---------------------|--------------|--------|--------|--------|--------|---------|-----------|------------------|-------------------|-----------------|
| NH <sub>3</sub>     | Ν            | 400.66 | 404.98 | 405.55 | 404.42 | 405.66  | 405.35    | 405.28           | 405.45            | 406.66          |
| $NH_3$              | Ν            | 402.33 | 404.98 | 405.55 | 404.42 | 405.66  | 405.35    | 405.28           | 405.45            | 406.66          |
| NH <sub>3</sub>     | Ν            | 402.86 | 406.39 | 406.63 | 405.61 | 406.59  | 406.32    | 406.16           | 406.37            | 407.49          |
| HCHO (formaldehyde) | $\mathbf{C}$ | 285.59 | 292.13 | 292.73 | 291.88 | 293.14  | 292.73    | 292.50           | 292.69            | 293.92          |
| HCHO (formaldehyde) | $\mathbf{C}$ | 290.18 | 293.65 | 294.15 | 293.17 | 294.42  | 293.99    | 293.73           | 293.95            | 295.17          |
| HCHO (formaldehyde) | $\mathbf{C}$ | 291.25 | 293.66 | 294.17 | 293.36 | 294.57  | 294.15    | 293.88           | 294.09            | 295.31          |
| HCHO (formaldehyde) | О            | 530.82 | 537.62 | 537.90 | 536.86 | 537.74  | 537.71    | 537.53           | 537.67            | 538.78          |
| HCHO (formaldehyde) | 0            | 535.43 | 538.61 | 538.98 | 537.97 | 538.95  | 538.87    | 538.70           | 538.85            | 539.98          |
| CO                  | С            | 287.40 | 295.05 | 295.51 | 294.56 | 295.74  | 295.24    | 294.68           | 295.00            | 296.22          |
| CO                  | $\mathbf{C}$ | 292.37 | 296.17 | 296.59 | 295.75 | 296.87  | 296.32    | 295.67           | 296.02            | 297.24          |
| CO                  | $\mathbf{C}$ | 293.33 | 296.76 | 297.08 | 295.86 | 296.98  | 296.47    | 295.86           | 296.19            | 297.41          |
| CO                  | 0            | 534.21 | 541.48 | 541.61 | 540.57 | 541.38  | 541.30    | 540.97           | 541.14            | 542.22          |
| CO                  | 0            | 538.91 | 542.62 | 542.70 | 541.81 | 542.56  | 542.43    | 541.98           | 542.19            | 543.26          |
| $N_2$               | Ν            | 401.00 | 409.38 | 408.04 | 408.49 | 410.09  | 409.36    | 401.60           | 409.39            | 410.56          |
| $N_2$               | Ν            | 406.10 | 410.50 | 409.00 | 409.49 | 410.94  | 410.16    | 402.12           | 409.99            | 411.12          |
| $N_2O$              | NC           | 404.70 | 409.47 | 410.72 | 409.63 | 411.47  | 410.95    | 410.73           | 410.97            | 412.38          |
| $C_2H_4$ (ethylene) | С            | 284.67 | 289.08 | 287.92 | 288.73 | 289.89  | 289.44    | 289.32           | 289.50            | 290.58          |
| $C_2H_4$ (ethylene) | С            | 287.24 | 289.94 | 288.67 | 289.42 | 290.53  | 290.08    | 289.86           | 290.08            | 291.16          |
| $H_2O$              | О            | 534.00 | 538.45 | 538.93 | 537.85 | 539.04  | 538.81    | 538.52           | 538.69            | 539.90          |
| $H_2O$              | 0            | 535.90 | 539.84 | 540.00 | 539.16 | 540.00  | 539.80    | 539.37           | 539.58            | 540.72          |

Table S17: Excitation energies (in eV) for 20 higher-lying transitions computed using IP-TPM@1/2, including relativistic corrections.

Table S18: Excitation energies (in eV) for 20 higher-lying transitions computed using IP-TPM@1/3, including relativistic corrections.

| Molecules           | Orbitals     | Expt.  | SCAN   | SCAN0  | B3LYP  | BH&HLYP | CAM-B3LYP | $LRC-\omega PBE$ | $LRC-\omega PBEh$ | $\omega B97X-V$ |
|---------------------|--------------|--------|--------|--------|--------|---------|-----------|------------------|-------------------|-----------------|
| NH <sub>3</sub>     | Ν            | 400.66 | 403.66 | 404.34 | 403.16 | 404.51  | 404.18    | 404.13           | 404.29            | 405.53          |
| $NH_3$              | Ν            | 402.33 | 403.66 | 404.34 | 403.16 | 404.51  | 404.18    | 404.13           | 404.29            | 405.53          |
| $NH_3$              | Ν            | 402.86 | 405.42 | 405.67 | 404.62 | 405.62  | 405.34    | 405.18           | 405.39            | 406.52          |
| HCHO (formaldehyde) | $\mathbf{C}$ | 285.59 | 290.99 | 291.73 | 290.76 | 292.13  | 291.71    | 291.52           | 291.70            | 292.96          |
| HCHO (formaldehyde) | $\mathbf{C}$ | 290.18 | 292.47 | 293.15 | 292.02 | 293.40  | 292.96    | 292.76           | 292.96            | 294.22          |
| HCHO (formaldehyde) | $\mathbf{C}$ | 291.25 | 292.67 | 293.22 | 292.36 | 293.63  | 293.21    | 293.01           | 293.20            | 294.44          |
| HCHO (formaldehyde) | 0            | 530.82 | 536.66 | 537.00 | 535.91 | 536.85  | 536.82    | 536.68           | 536.80            | 537.94          |
| HCHO (formaldehyde) | 0            | 535.43 | 537.52 | 537.96 | 536.92 | 537.97  | 537.89    | 537.80           | 537.91            | 539.08          |
| CO                  | $\mathbf{C}$ | 287.40 | 294.11 | 294.60 | 293.59 | 294.81  | 294.32    | 293.83           | 294.13            | 295.36          |
| CO                  | $\mathbf{C}$ | 292.37 | 295.35 | 295.77 | 294.88 | 296.01  | 295.47    | 294.85           | 295.20            | 296.42          |
| CO                  | $\mathbf{C}$ | 293.33 | 295.96 | 296.29 | 295.02 | 296.16  | 295.65    | 295.06           | 295.39            | 296.61          |
| CO                  | 0            | 534.21 | 540.54 | 540.71 | 539.63 | 540.48  | 540.41    | 540.12           | 540.28            | 541.37          |
| CO                  | 0            | 538.91 | 541.82 | 541.90 | 540.96 | 541.74  | 541.60    | 541.17           | 541.37            | 542.45          |
| $N_2$               | Ν            | 401.00 | 408.34 | 407.02 | 407.44 | 409.04  | 408.31    | 400.56           | 408.35            | 409.53          |
| $N_2$               | Ν            | 406.10 | 409.68 | 408.18 | 408.62 | 410.09  | 409.30    | 401.28           | 409.15            | 410.28          |
| $N_2O$              | NC           | 404.70 | 407.97 | 409.43 | 408.33 | 410.25  | 409.78    | 409.56           | 409.79            | 411.29          |
| $C_2H_4$ (ethylene) | $\mathbf{C}$ | 284.67 | 288.12 | 287.05 | 287.78 | 289.03  | 288.56    | 288.49           | 288.64            | 289.74          |
| $C_2H_4$ (ethylene) | $\mathbf{C}$ | 287.24 | 289.03 | 287.85 | 288.61 | 289.73  | 289.30    | 289.10           | 289.32            | 290.41          |
| $H_2O$              | Ο            | 534.00 | 537.05 | 537.69 | 536.48 | 537.84  | 537.60    | 537.40           | 537.53            | 538.81          |
| H <sub>2</sub> O    | О            | 535.90 | 538.95 | 539.11 | 538.22 | 539.08  | 538.89    | 538.48           | 538.69            | 539.83          |

| Molecules           | Orbitals | Expt.  | SCAN   | SCAN0  | B3LYP  | BH&HLYP | CAM-B3LYP | $LRC-\omega PBE$ | $LRC-\omega PBEh$ | $\omega B97X-V$ |
|---------------------|----------|--------|--------|--------|--------|---------|-----------|------------------|-------------------|-----------------|
| NH <sub>3</sub>     | Ν        | 402.33 | 402.62 | 403.55 | 403.47 | 405.03  | 404.03    | 404.36           | 404.11            | 404.18          |
| $NH_3$              | Ν        | 402.86 | 402.63 | 403.55 | 403.47 | 405.03  | 404.03    | 404.36           | 404.11            | 404.18          |
| $NH_3$              | Ν        | 403.57 | 403.87 | 404.54 | 404.53 | 405.97  | 404.91    | 405.17           | 404.95            | 404.95          |
| HCHO (formaldehyde) | С        | 290.18 | 289.53 | 290.28 | 289.76 | 290.86  | 290.16    | 290.24           | 290.15            | 290.37          |
| HCHO (formaldehyde) | С        | 291.25 | 290.89 | 291.56 | 290.99 | 292.06  | 291.34    | 291.38           | 291.31            | 291.53          |
| HCHO (formaldehyde) | С        | 291.73 | 290.93 | 291.61 | 291.12 | 292.17  | 291.41    | 291.40           | 291.33            | 291.55          |
| HCHO (formaldehyde) | О        | 535.43 | 534.76 | 535.33 | 534.90 | 535.51  | 535.12    | 535.25           | 535.01            | 536.10          |
| HCHO (formaldehyde) | О        | 536.34 | 535.89 | 536.48 | 536.04 | 536.63  | 536.22    | 536.27           | 536.05            | 537.52          |
| CO                  | С        | 292.37 | 290.90 | 291.58 | 291.11 | 292.37  | 291.35    | 291.18           | 291.16            | 291.96          |
| CO                  | С        | 293.33 | 291.86 | 292.53 | 292.13 | 293.36  | 292.35    | 292.14           | 292.15            | 292.93          |
| CO                  | С        | 293.49 | 292.16 | 292.79 | 292.21 | 293.48  | 292.46    | 292.32           | 292.30            | 293.07          |
| CO                  | О        | 538.91 | 537.89 | 538.38 | 537.89 | 538.58  | 538.01    | 538.01           | 537.79            | 538.20          |
| CO                  | О        | 539.91 | 538.86 | 539.35 | 538.96 | 539.62  | 539.05    | 539.03           | 538.81            | 539.20          |
| $N_2$               | Ν        | 406.10 | 405.66 | 404.88 | 405.67 | 410.62  | 406.13    | 401.51           | 406.21            | 406.26          |
| $N_2$               | Ν        | 407.00 | 406.17 | 405.26 | 406.14 | 410.95  | 406.39    | 401.52           | 406.28            | 406.30          |
| $N_2O$              | NC       | 407.60 | 407.23 | 408.47 | 407.66 | 409.33  | 408.31    | 408.43           | 408.33            | 409.02          |
| $C_2H_4$ (ethylene) | С        | 287.24 | 286.99 | 286.11 | 287.27 | 291.03  | 287.62    | 287.86           | 287.72            | 288.17          |
| $C_2H_4$ (ethylene) | С        | 287.88 | 287.55 | 286.60 | 287.80 | 291.53  | 288.07    | 288.22           | 288.10            | 288.57          |
| $H_2O$              | 0        | 535.90 | 535.75 | 536.60 | 536.51 | 538.08  | 536.90    | 537.05           | 536.73            | 536.50          |
| H <sub>2</sub> O    | О        | 537.00 | 537.19 | 537.68 | 537.61 | 539.06  | 537.77    | 537.86           | 537.55            | 537.25          |

Table S19: Excitation energies (in eV) for 20 higher-lying transitions computed using the empirically-shifted XTPM approach, including relativistic corrections.

Table S20: Excitation energies (in eV) for 20 higher-lying transitions computed using  $\Delta$ SCF, including relativistic corrections.

| Molecule            | Atom         | Expt.  | SCAN   | SCAN0  | B3LYP  | BH&HLYP | CAM-B3LYP | $LRC-\omega PBE$ | $LRC-\omega PBEh$ | $\omega B97X-V$ |
|---------------------|--------------|--------|--------|--------|--------|---------|-----------|------------------|-------------------|-----------------|
| NH <sub>3</sub>     | Ν            | 402.33 | 402.33 | 402.56 | 402.30 | 403.06  | 402.48    | 401.62           | 401.89            | 403.06          |
| $NH_3$              | Ν            | 402.86 | 402.40 | 402.60 | 402.35 | 403.08  | 402.50    | 401.64           | 401.91            | 403.07          |
| $NH_3$              | Ν            | 403.57 | 403.80 | 403.94 | 403.71 | 404.36  | 403.87    | 402.99           | 403.23            | 404.41          |
| HCHO (formaldehyde) | $\mathbf{C}$ | 290.18 | 290.07 | 290.31 | 290.22 | 290.97  | 290.30    | 289.35           | 289.65            | 290.78          |
| HCHO (formaldehyde) | $\mathbf{C}$ | 291.25 | 291.73 | 291.93 | 291.82 | 292.05  | 291.93    | 291.04           | 291.30            | 292.47          |
| HCHO (formaldehyde) | С            | 291.73 | 291.10 | 291.37 | 291.22 | 292.57  | 291.38    | 290.49           | 290.77            | 291.94          |
| HCHO (formaldehyde) | 0            | 535.43 | 535.72 | 535.70 | 535.51 | 535.93  | 535.65    | 534.84           | 535.04            | 536.07          |
| HCHO (formaldehyde) | 0            | 536.34 | 536.58 | 536.63 | 536.34 | 537.13  | 536.54    | 535.74           | 535.94            | 537.03          |
| CO                  | $\mathbf{C}$ | 292.37 | 292.73 | 293.05 | 292.86 | 293.70  | 292.98    | 291.90           | 292.24            | 294.67          |
| CO                  | $\mathbf{C}$ | 293.33 | 293.73 | 294.11 | 293.90 | 295.02  | 294.10    | 292.97           | 293.32            | 296.04          |
| CO                  | $\mathbf{C}$ | 293.49 | 293.95 | 294.33 | 294.11 | 294.80  | 294.34    | 293.24           | 293.57            | 295.63          |
| CO                  | 0            | 538.91 | 539.17 | 539.17 | 538.92 | 539.39  | 539.09    | 538.21           | 538.41            | 540.65          |
| CO                  | 0            | 539.91 | 540.19 | 540.25 | 539.98 | 540.71  | 540.23    | 539.31           | 539.51            | 542.21          |
| $N_2$               | Ν            | 406.10 | 406.82 | 407.01 | 406.76 | 407.48  | 406.92    | 406.97           | 406.23            | 407.36          |
| $N_2$               | Ν            | 407.00 | 407.74 | 407.99 | 407.72 | 408.51  | 407.98    | 408.60           | 407.26            | 408.41          |
| $N_2O$              | NC           | 407.60 | 407.96 | 408.62 | 407.99 | 410.06  | 408.29    | 407.23           | 407.68            | 409.53          |
| $C_2H_4$ (ethylene) | $\mathbf{C}$ | 287.24 | 287.23 | 287.42 | 287.32 | 288.30  | 287.71    | 286.93           | 287.18            | 288.28          |
| $C_2H_4$ (ethylene) | $\mathbf{C}$ | 287.88 | 288.02 | 288.20 | 288.09 | 288.70  | 288.20    | 287.46           | 287.69            | 289.26          |
| H <sub>2</sub> O    | Ο            | 535.90 | 535.66 | 535.82 | 535.49 | 536.24  | 535.75    | 534.81           | 535.05            | 536.24          |
| H <sub>2</sub> O    | Ο            | 537.00 | 537.52 | 537.59 | 537.14 | 537.92  | 537.54    | 536.58           | 536.80            | 537.96          |

Table S21: Excitation energies (in eV) for 29 transitions from Ref. 1, comparing BSE@ $G_0W_0$  results from that work to shifted-XTPM (B3LYP) and TDDFT +  $\Delta$ SCF (B3LYP) from the present work, including relativistic corrections

| Molecule            | Atom         | Transition                  | Expt.  | shifted- | TDDFT         | $BSE@G_0W_0$ |
|---------------------|--------------|-----------------------------|--------|----------|---------------|--------------|
|                     | 1100111      | 11011011011                 | Linpti | XTPM     | $+\Delta SCF$ | 20200000     |
| $ m NH_3$           | Ν            | $1s \rightarrow 3s$         | 400.66 | 401.13   | 400.69        | 400.02       |
| $\rm NH_3$          | Ν            | $1s \to 3p(E)$              | 402.33 | 403.47   | 402.34        | 401.67       |
| $\rm NH_3$          | Ν            | $1s \to 3p(A_1)$            | 402.86 | 403.47   | 402.34        | 401.67       |
| $\rm NH_3$          | Ν            | $1s \to 4s(A_1)$            | 403.57 | 404.53   | 405.25        | 402.83       |
| HCHO (formaldehyde) | $\mathbf{C}$ | $1s \to \pi^*$              | 285.59 | 286.24   | 285.56        | 284.96       |
| HCHO (formaldehyde) | $\mathbf{C}$ | $1s \rightarrow 3s$         | 290.18 | 289.76   | 289.39        | 289.92       |
| HCHO (formaldehyde) | $\mathbf{C}$ | $1s \to 3p(B_2)$            | 291.25 | 290.99   | 290.60        | 290.79       |
| HCHO (formaldehyde) | $\mathbf{C}$ | $1s \to 3p(B_1)$            | 291.73 | 291.12   | 290.90        | 291.42       |
| HCHO (formaldehyde) | Ο            | $1s \to \pi^*$              | 530.82 | 531.35   | 530.73        | 529.88       |
| HCHO (formaldehyde) | Ο            | $1s \rightarrow 3s$         | 535.43 | 534.90   | 534.80        | 534.93       |
| HCHO (formaldehyde) | Ο            | $1s \rightarrow 3p$         | 536.34 | 536.04   | 536.17        | 535.71       |
| CO                  | $\mathbf{C}$ | $1s \rightarrow 2p\pi^*$    | 287.40 | 287.29   | 286.59        | 285.46       |
| CO                  | $\mathbf{C}$ | $1s \rightarrow 3s\sigma$   | 292.37 | 291.11   | 291.72        | 292.08       |
| CO                  | $\mathbf{C}$ | $1s \rightarrow 3p\pi$      | 293.33 | 292.13   | 292.62        | 293.29       |
| CO                  | $\mathbf{C}$ | $1s \rightarrow 3p\sigma$   | 293.49 | 292.21   | 292.77        | 293.60       |
| CO                  | Ο            | $1s \to \pi^*$              | 534.21 | 534.48   | 533.84        | 532.77       |
| CO                  | Ο            | $1s \rightarrow 3s$         | 538.91 | 537.89   | 538.59        | 538.25       |
| CO                  | Ο            | $1s \rightarrow 3p\pi$      | 539.91 | 538.96   | 539.80        | 539.70       |
| $N_2$               | Ν            | $1s \rightarrow 2p\pi_g$    | 401.00 | 401.21   | 400.45        | 399.93       |
| $N_2$               | Ν            | $1s \rightarrow 3s\sigma_q$ | 406.10 | 405.67   | 406.83        | 406.05       |
| $N_2$               | Ν            | $1s \rightarrow 3p\pi_u$    | 407.00 | 406.14   | 407.50        | 407.08       |
| $N_2O$              | NC           | $1s \rightarrow 3p\pi^*$    | 404.70 | 404.72   | 404.02        | 403.91       |
| $N_2O$              | NC           | $1s \rightarrow 3p\sigma$   | 407.60 | 407.66   | 407.39        | 406.53       |
| $C_2H_4$ (ethylene) | $\mathbf{C}$ | $1s \to \pi^*$              | 284.67 | 285.32   | 284.72        | 284.04       |
| $C_2H_4$ (ethylene) | $\mathbf{C}$ | $1s \rightarrow 3s$         | 287.24 | 287.27   | 287.08        | 287.05       |
| $C_2H_4$ (ethylene) | $\mathbf{C}$ | $1s \rightarrow 3p\pi$      | 287.88 | 287.80   | 287.74        | 287.57       |
| H <sub>2</sub> O    | Ο            | $1s \rightarrow 4a_1/3s$    | 534.00 | 534.48   | 533.99        | 532.66       |
| $H_2O$              | Ο            | $1s \rightarrow 2b_1/3p$    | 535.90 | 536.51   | 535.63        | 534.32       |
| $H_2O$              | Ο            | $1s \rightarrow 3p(b2)$     | 537.00 | 537.61   | 540.01        | 536.25       |