Supporting Information for: "Using Atomic Confining Potentials for Geometry Optimization and Vibrational Frequency Calculations in Quantum-Chemical Models of Enzyme Active Sites"

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| | k = 30 N/m | | | | | k = 450 N/m | | | | | | k = 990 N/m | | | | | | |
|------|-------------|-------------------|--------------|--------------|--------------|--------------|-------------------|--------------|--------------|----------------|----------|-------------------|--------------|--------------|--------------|--|--|--|
| mode | | freq. (cm^{-1}) |) | error | (cm^{-1}) | | freq. (cm^{-1}) |) | error | (cm^{-1}) | | freq. (cm^{-1}) |) | error | (cm^{-1}) | | | |
| | analytic | $IDRV=0^{a}$ | $IDRV=1^{b}$ | $IDRV=0^{a}$ | $IDRV=1^{b}$ | analytic | $IDRV=0^{a}$ | $IDRV=1^{b}$ | $IDRV=0^{a}$ | $IDRV = 1^{b}$ | analytic | $IDRV=0^{a}$ | $IDRV=1^{b}$ | $IDRV=0^{a}$ | $IDRV=1^{b}$ | | | |
| 1 | 70.12 | 70.12 | 70.08 | 0.00 | 0.04 | 90.49 | 90.48 | 90.52 | -0.04 | -0.03 | 84.23 | 84.12 | 84.34 | 0.11 | -0.11 | | | |
| 2 | 88.21 | 88.19 | 88.21 | 0.02 | 0.00 | 137.97 | 137.96 | 138.00 | 0.02 | -0.03 | 95.47 | 95.47 | 95.48 | 0.00 | -0.01 | | | |
| 3 | 141.08 | 141.07 | 141.10 | 0.01 | -0.02 | 182.44 | 182.40 | 182.49 | 0.03 | -0.05 | 167.33 | 167.31 | 167.35 | 0.02 | -0.02 | | | |
| 4 | 264.43 | 264.42 | 264.46 | 0.01 | -0.03 | 264.31 | 264.32 | 264.30 | 0.04 | 0.01 | 267.91 | 267.91 | 267.92 | 0.00 | -0.01 | | | |
| 5 | 285.17 | 285.16 | 285.17 | 0.01 | 0.00 | 311.79 | 311.80 | 311.83 | 0.01 | -0.04 | 326.65 | 326.64 | 326.68 | 0.01 | -0.03 | | | |
| 6 | 291.15 | 291.11 | 291.15 | 0.04 | 0.00 | 332.59 | 332.59 | 332.61 | 0.04 | -0.02 | 351.48 | 351.48 | 351.51 | 0.00 | -0.03 | | | |
| 7 | 326.40 | 326.40 | 326.40 | 0.00 | 0.00 | 395.34 | 395.35 | 395.35 | 0.00 | -0.01 | 407.03 | 407.03 | 407.02 | 0.00 | 0.01 | | | |
| 8 | 349.19 | 349.18 | 349.18 | 0.01 | 0.01 | 434.71 | 434.71 | 434.73 | 0.00 | -0.02 | 492.38 | 492.37 | 492.38 | 0.01 | 0.00 | | | |
| 9 | 413.53 | 413.53 | 413.55 | 0.00 | -0.02 | 486.11 | 486.10 | 486.11 | 0.02 | 0.00 | 546.13 | 546.13 | 546.16 | 0.00 | -0.03 | | | |
| 10 | 473.06 | 473.05 | 473.08 | 0.01 | -0.02 | 559.27 | 559.27 | 559.29 | 0.03 | -0.02 | 617.96 | 617.96 | 617.99 | 0.00 | -0.03 | | | |
| 11 | 504.75 | 504.75 | 504.76 | 0.00 | -0.01 | 574.93 | 574.93 | 574.93 | 0.01 | 0.00 | 659.66 | 659.66 | 659.69 | 0.00 | -0.03 | | | |
| 12 | 658.69 | 658.68 | 658.73 | 0.01 | -0.04 | 658.18 | 658.18 | 658.20 | 0.05 | -0.02 | 680.86 | 680.86 | 680.86 | 0.00 | 0.00 | | | |
| 13 | 680.82 | 680.82 | 680.82 | 0.00 | 0.00 | 680.68 | 680.68 | 680.67 | 0.00 | 0.01 | 691.78 | 691.78 | 691.78 | 0.00 | 0.00 | | | |
| 14 | 753.20 | 753.20 | 753.24 | 0.00 | -0.04 | 754.44 | 754.44 | 754.44 | 0.04 | 0.00 | 762.07 | 762.07 | 762.06 | 0.00 | 0.01 | | | |
| 15 | 790.84 | 790.83 | 790.84 | 0.01 | 0.00 | 790.30 | 790.29 | 790.31 | 0.01 | -0.01 | 790.33 | 790.32 | 790.33 | 0.01 | 0.00 | | | |
| 16 | 833.35 | 833.35 | 833.33 | 0.00 | 0.02 | 826.02 | 826.01 | 826.04 | -0.02 | -0.02 | 816.47 | 816.46 | 816.51 | 0.01 | -0.04 | | | |
| 17 | 851.34 | 851.33 | 851.32 | 0.01 | 0.02 | 840.19 | 840.18 | 840.19 | -0.01 | 0.00 | 841.21 | 841.20 | 841.21 | 0.01 | 0.00 | | | |
| 18 | 887.46 | 887.46 | 887.50 | 0.00 | -0.04 | 892.17 | 892.17 | 892.20 | 0.04 | -0.03 | 897.35 | 897.34 | 897.39 | 0.01 | -0.04 | | | |
| 19 | 905.80 | 905.79 | 905.82 | 0.01 | -0.02 | 931.92 | 931.92 | 931.88 | 0.03 | 0.04 | 932.56 | 932.56 | 932.53 | 0.00 | 0.03 | | | |
| 20 | 931.93 | 931.93 | 931.92 | 0.00 | 0.01 | 960.35 | 960.35 | 960.37 | -0.01 | -0.02 | 984.67 | 984.67 | 984.68 | 0.00 | -0.01 | | | |
| 21 | 959.01 | 959.01 | 959.00 | 0.00 | 0.01 | 1021.35 | 1021.35 | 1021.31 | -0.01 | 0.04 | 1023.13 | 1023.13 | 1023.10 | 0.00 | 0.03 | | | |
| 22 | 1020.34 | 1020.34 | 1020.40 | 0.00 | -0.06 | 1045.70 | 1045.71 | 1045.70 | 0.06 | 0.00 | 1088.19 | 1088.19 | 1088.14 | 0.00 | 0.05 | | | |
| 23 | 1032.95 | 1032.95 | 1032.99 | 0.00 | -0.04 | 1074.23 | 1074.23 | 1074.23 | 0.04 | 0.00 | 1115.60 | 1115.60 | 1115.63 | 0.00 | -0.03 | | | |
| 24 | 1108.54 | 1108.54 | 1108.52 | 0.00 | 0.02 | 1121.64 | 1121.64 | 1121.67 | -0.02 | -0.03 | 1125.98 | 1125.98 | 1126.04 | 0.00 | -0.06 | | | |
| 25 | 1122.24 | 1122.24 | 1122.26 | 0.00 | -0.02 | 1143.15 | 1143.15 | 1143.11 | 0.02 | 0.04 | 1151.04 | 1151.04 | 1151.12 | 0.00 | -0.08 | | | |
| 26 | 1132.38 | 1132.38 | 1132.37 | 0.00 | 0.01 | 1152.16 | 1152.16 | 1152.22 | -0.01 | -0.06 | 1184.79 | 1184.78 | 1184.85 | 0.01 | -0.06 | | | |
| 27 | 1152.66 | 1152.66 | 1152.69 | 0.00 | -0.03 | 1160.19 | 1160.19 | 1160.22 | 0.03 | -0.03 | 1209.90 | 1209.90 | 1209.89 | 0.00 | 0.01 | | | |
| 28 | 1217.70 | 1217.70 | 1217.73 | 0.00 | -0.03 | 1258.43 | 1258.43 | 1258.42 | 0.03 | 0.01 | 1272.35 | 1272.34 | 1272.33 | 0.01 | 0.02 | | | |
| 29 | 1258.59 | 1258.60 | 1258.59 | -0.01 | 0.00 | 1270.24 | 1270.24 | 1270.27 | -0.01 | -0.03 | 1284.52 | 1284.52 | 1284.55 | 0.00 | -0.03 | | | |
| 30 | 1276.66 | 1276.66 | 1276.64 | 0.00 | 0.02 | 1282.67 | 1282.67 | 1282.69 | -0.02 | -0.02 | 1297.55 | 1297.55 | 1297.48 | 0.00 | 0.07 | | | |
| 31 | 1293.51 | 1293.51 | 1293.58 | 0.00 | -0.07 | 1304.88 | 1304.88 | 1304.83 | 0.07 | 0.05 | 1337.10 | 1337.09 | 1337.04 | 0.01 | 0.06 | | | |
| 32 | 1342.99 | 1342.98 | 1342.85 | 0.01 | 0.14 | 1343.33 | 1343.32 | 1343.23 | -0.13 | 0.10 | 1376.48 | 1376.48 | 1376.44 | 0.00 | 0.04 | | | |
| 33 | 1385.21 | 1385.21 | 1385.35 | 0.00 | -0.14 | 1391.94 | 1391.94 | 1391.98 | 0.14 | -0.04 | 1394.16 | 1394.16 | 1394.19 | 0.00 | -0.03 | | | |
| 34 | 1397.29 | 1397.28 | 1397.19 | 0.01 | 0.10 | 1409.73 | 1409.73 | 1409.75 | -0.09 | -0.02 | 1417.42 | 1417.42 | 1417.46 | 0.00 | -0.04 | | | |
| 35 | 1419.28 | 1419.28 | 1419.30 | 0.00 | -0.02 | 1424.09 | 1424.08 | 1424.13 | 0.02 | -0.04 | 1438.17 | 1438.16 | 1438.20 | 0.01 | -0.03 | | | |
| 36 | 1443.26 | 1443.26 | 1443.24 | 0.00 | 0.02 | 1445.70 | 1445.70 | 1445.72 | -0.02 | -0.02 | 1448.61 | 1448.61 | 1448.64 | 0.00 | -0.03 | | | |
| 37 | 1448.19 | 1448.19 | 1448.23 | 0.00 | -0.04 | 1503.31 | 1503.30 | 1503.30 | 0.04 | 0.01 | 1505.01 | 1505.00 | 1505.00 | 0.01 | 0.01 | | | |
| 38 | 1505.89 | 1505.89 | 1505.89 | 0.00 | 0.00 | 1525.03 | 1525.03 | 1525.06 | 0.00 | -0.03 | 1525.72 | 1525.72 | 1525.74 | 0.00 | -0.02 | | | |
| 39 | 1518.97 | 1518.98 | 1518.98 | -0.01 | -0.01 | 1532.25 | 1532.25 | 1532.24 | 0.00 | 0.01 | 1552.08 | 1552.07 | 1552.08 | 0.01 | 0.00 | | | |
| 40 | 1524.55 | 1524.54 | 1524.57 | 0.01 | -0.02 | 1548.60 | 1548.60 | 1548.62 | 0.03 | -0.02 | 1575.16 | 1575.16 | 1575.16 | 0.00 | 0.00 | | | |
| 41 | 1531.23 | 1531.22 | 1531.23 | 0.01 | 0.00 | 1552.34 | 1552.34 | 1552.34 | 0.01 | 0.00 | 1628.56 | 1628.56 | 1628.52 | 0.00 | 0.04 | | | |
| 42 | 1620.92 | 1620.92 | 1620.84 | 0.00 | 0.08 | 1627.09 | 1627.09 | 1627.08 | -0.08 | 0.01 | 1672.22 | 1672.21 | 1672.23 | 0.01 | -0.01 | | | |
| 43 | 1699.22 | 1699.21 | 1699.23 | 0.01 | -0.01 | 1698.92 | 1698.92 | 1698.95 | 0.02 | -0.03 | 1703.64 | 1703.63 | 1703.65 | 0.01 | -0.01 | | | |
| 44 | 3017.93 | 3017.93 | 3017.95 | 0.00 | -0.02 | 3023.10 | 3023.12 | 3023.12 | 0.02 | -0.02 | 3019.32 | 3019.32 | 3019.34 | 0.00 | -0.02 | | | |
| 45 | 3033.95 | 3033.96 | 3033.97 | -0.01 | -0.02 | 3028.49 | 3028.50 | 3028.53 | 0.01 | -0.04 | 3027.06 | 3027.05 | 3027.10 | 0.01 | -0.04 | | | |
| 46 | 3043.17 | 3043.18 | 3043.20 | -0.01 | -0.03 | 3035.23 | 3035.23 | 3035.24 | 0.02 | -0.01 | 3037.55 | 3037.55 | 3037.56 | 0.00 | -0.01 | | | |
| 47 | 3077.55 | 3077.55 | 3077.53 | 0.00 | 0.02 | 3076.83 | 3076.84 | 3076.83 | -0.02 | 0.00 | 3075.11 | 3075.11 | 3075.11 | 0.00 | 0.00 | | | |
| 48 | 3103.11 | 3103.12 | 3103.11 | -0.01 | 0.00 | 3083.44 | 3083.45 | 3083.41 | -0.01 | 0.03 | 3084.11 | 3084.11 | 3084.07 | 0.00 | 0.04 | | | |
| 49 | 3135.88 | 3135.89 | 3135.84 | -0.01 | 0.04 | 3112.71 | 3112.72 | 3112.69 | -0.05 | 0.02 | 3121.86 | 3121.87 | 3121.85 | -0.01 | 0.01 | | | |
| 50 | 3256.18 | 3256.18 | 3256.12 | 0.00 | 0.06 | 3251.43 | 3251.43 | 3251.44 | -0.06 | -0.01 | 3250.47 | 3250.47 | 3250.52 | 0.00 | -0.05 | | | |
| 51 | 3261.20 | 3261.21 | 3261.15 | -0.01 | 0.05 | 3269.27 | 3269.28 | 3269.23 | -0.06 | 0.04 | 3271.25 | 3271.26 | 3271.21 | -0.01 | 0.04 | | | |
| 52 | 3447.43 | 3447.44 | 3447.45 | -0.01 | -0.02 | 3470.88 | 3470.88 | 3470.89 | 0.01 | -0.01 | 3476.45 | 3476.46 | 3476.47 | -0.01 | -0.02 | | | |
| 53 | 3536.94 | 3536.94 | 3536.93 | 0.00 | 0.01 | 3574.04 | 3574.04 | 3574.02 | -0.01 | 0.02 | 3581.63 | 3581.63 | 3581.61 | 0.00 | 0.02 | | | |
| 54 | 3636.12 | 3636.14 | 3636.12 | -0.02 | 0.00 | 3640.85 | 3640.86 | 3640.84 | -0.02 | 0.01 | 3640.07 | 3640.08 | 3640.06 | -0.01 | 0.01 | | | |

Table S1: Comparison vibrational frequencies for Gly-Ala. with both terminal carbons confined with potential, computed using analytic and finite-difference second derivatives.

^aSecond-order finite difference of energies. ^bFirst-order finite difference of analytic gradients.

Table S2: Anchor atoms indices for all the model systems. The anchor atoms coordinates either kept fixed (coordinate lock formalism) or constrained with a harmonic confiner

| Model | | Anchor atom indices | | | | | | | | | | | | | | | |
|-------------------|----|---------------------|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|
| AMDase (Model I) | 3 | 9 | 17 | 20 | 23 | | | | | | | | | | | | |
| AMDase (Model II) | 3 | 14 | 18 | 19 | 22 | 33 | 37 | 44 | 50 | 51 | 55 | 62 | 69 | 70 | 71 | 74 | 84 |
| 4-OT | 17 | 18 | 22 | 27 | 28 | 34 | | | | | | | | | | | |



Figure S1: Optimized structures for model II of methyl(phenyl)malonate in the active site of AMDase, overlaying the structures obtained using harmonic and fixed-atom constraints.



Figure S2: Displacements of the constrained "anchor atoms" as compared to their initial, crystallographic positions \mathbf{r}_i^0 , for model I of methyl(phenyl)malonate in AMDase.



Figure S3: Displacements of the constrained "anchor atoms" as compared to their initial, crystallographic positions \mathbf{r}_i^0 , for model II of methyl(phenyl)malonate in AMDase.



Figure S4: Displacements of the constrained "anchor atoms" as compared to their initial, crystallographic positions \mathbf{r}_{i}^{0} , for the reaction catalyzed by 4-OT.



Figure S5: Differences in vibrational frequencies, $\Delta \nu = \nu$ (harmonic conf.) $-\nu$ (fixed atom), for each of the stationary points optimized for the 4-OT–catalyzed tautomerization of 2-oxo-4hexenedioate. (a) Plot of $\Delta \nu$ versus the normal mode index, with the modes ordered by increasing vibrational frequency, for each stationary point along the reaction pathway. (b) Plot of $\Delta \nu$ versus the frequency ν (fixed atom).