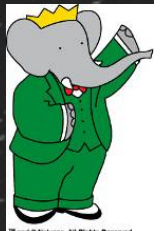


Beyond the Standard Model

Searches for New Physics at the B-Factories

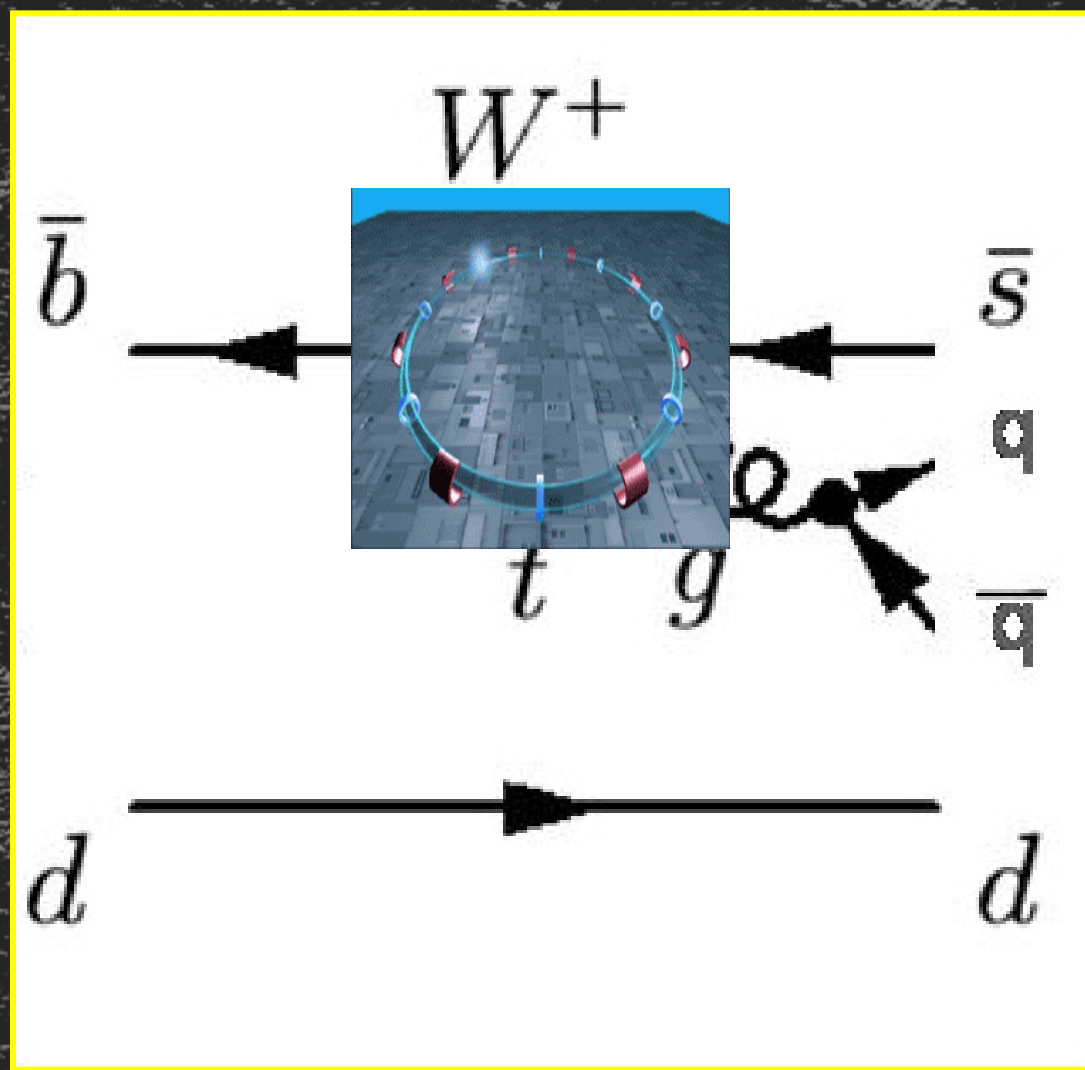


K. Honscheid
Ohio State University
Aspen 2006



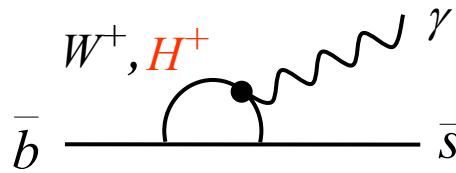
™ and © Hohens. All Rights Reserved

Where to look for New Physics?

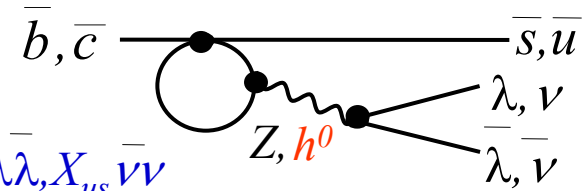


Experimental Strategies

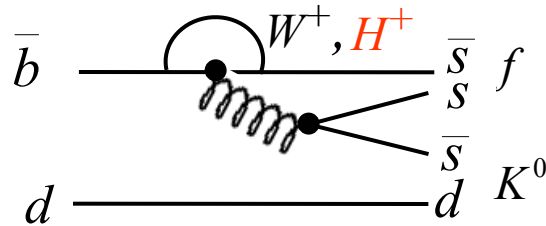
$b \rightarrow s \gamma$ penguins



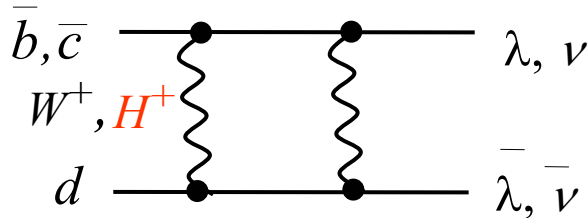
$B, D \rightarrow X_{us} \lambda \lambda, X_{us} \bar{\nu} \nu$



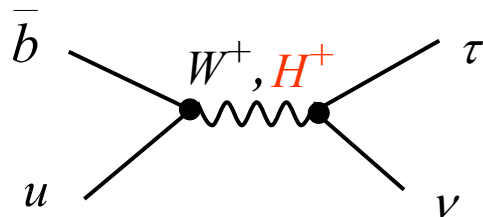
$b \rightarrow s g$ penguins



$B, D \rightarrow \lambda \lambda, \bar{\nu} \nu$

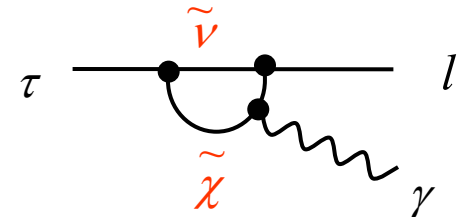


$B \rightarrow \tau \nu$



LFV

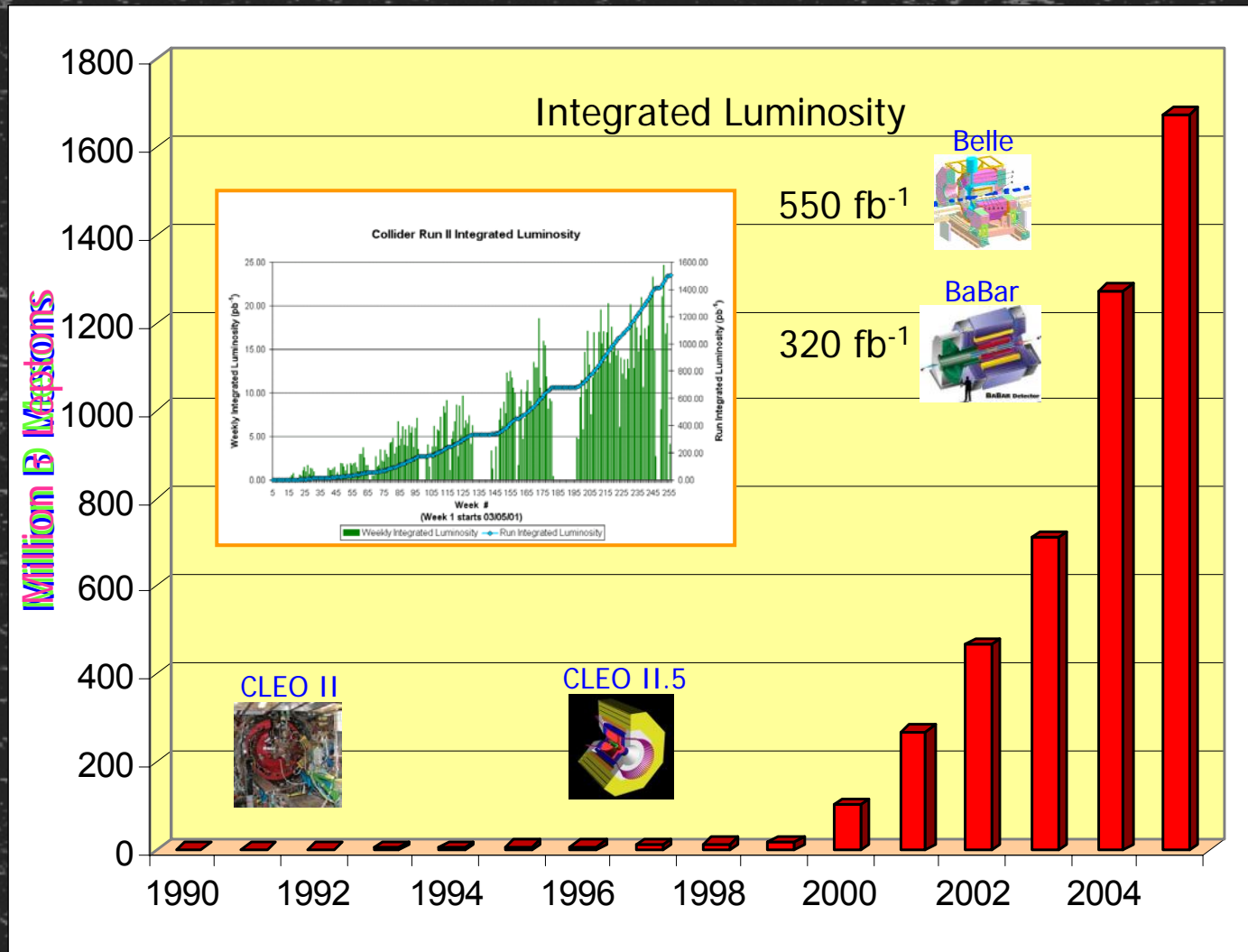
$\tau \rightarrow l \gamma$



Surprises

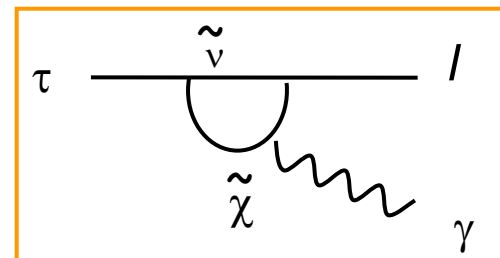
From Hitlin, LHC Labor Workshop

Experimental Landscape (ca 2006)



Search for Lepton Flavor Violation in τ Decays

- Lepton flavor is conserved in the Standard Model
 - not protected by an underlying conserved current symmetry
 - Neutrino Masses
- Many SM extensions include LF violation

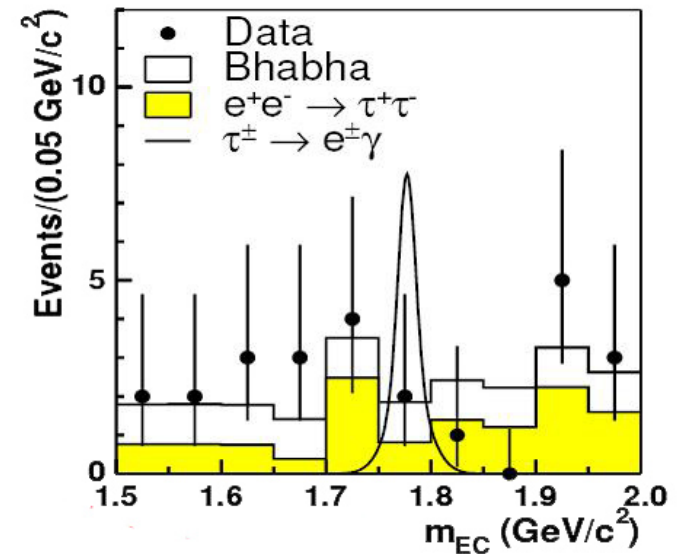
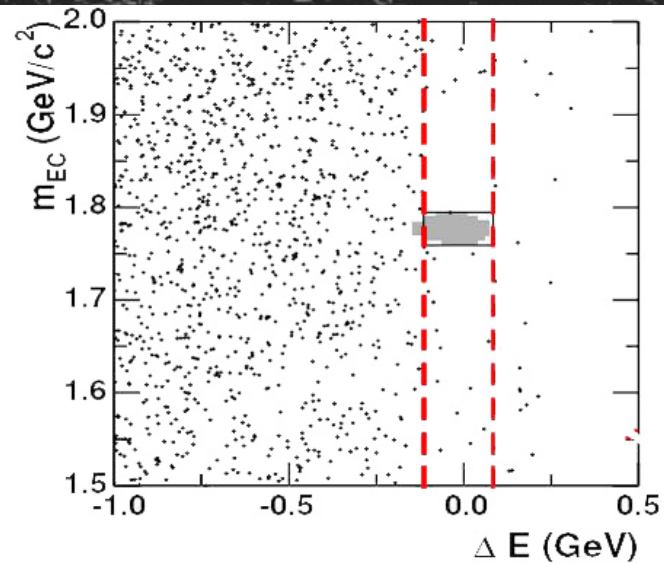
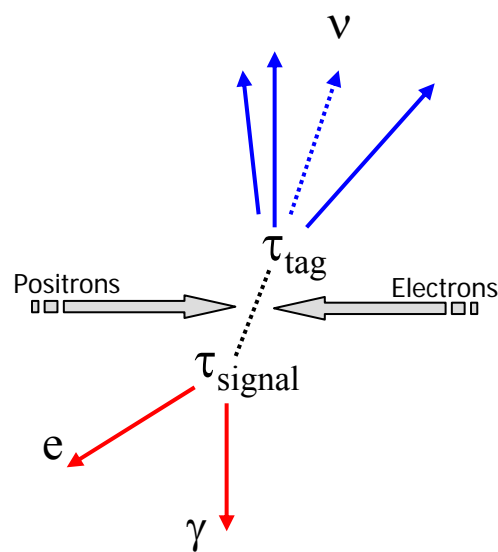


Model	$\tau \rightarrow \ell \gamma$	Reference
SM + lepton mixing	10^{-40}	hep-ph/9810484
SM + rh heavy Majorana neutrino	$<10^{-9}$	PRD66(2002)034008
mSUGRA + seesaw	$<10^{-7}$	hep-ph/0206110, hep-ph/9911459
SUSY $SU(5)$	$<10^{-4}$	hep-ph/0303071
SUSY $SO(10)$ + seesaw	$<10^{-5}$	hep-ph/0209303, hep-ph/0304190, hep-ph/0405017
SUSY anomalous $U(1)$	$<10^{-7}$	hep-ph/0308093
neutral SUSY Higgs	$<10^{-10}$	hep-ph/0304081)
MSSM+nonuniversal soft SUSY breaking	$<10^{-10}$	hep-ph/0305290
Non universal Z' (technicolor)	$<10^{-9}$	PLB547(2002)252
extra dimensions	$<10^{-11}$	hep-ph/0210021

- Observation of LF violation would be a clear signature for new physics

Search for $\tau^- \rightarrow e^- \gamma$

PRL 96, 041801 (2006)



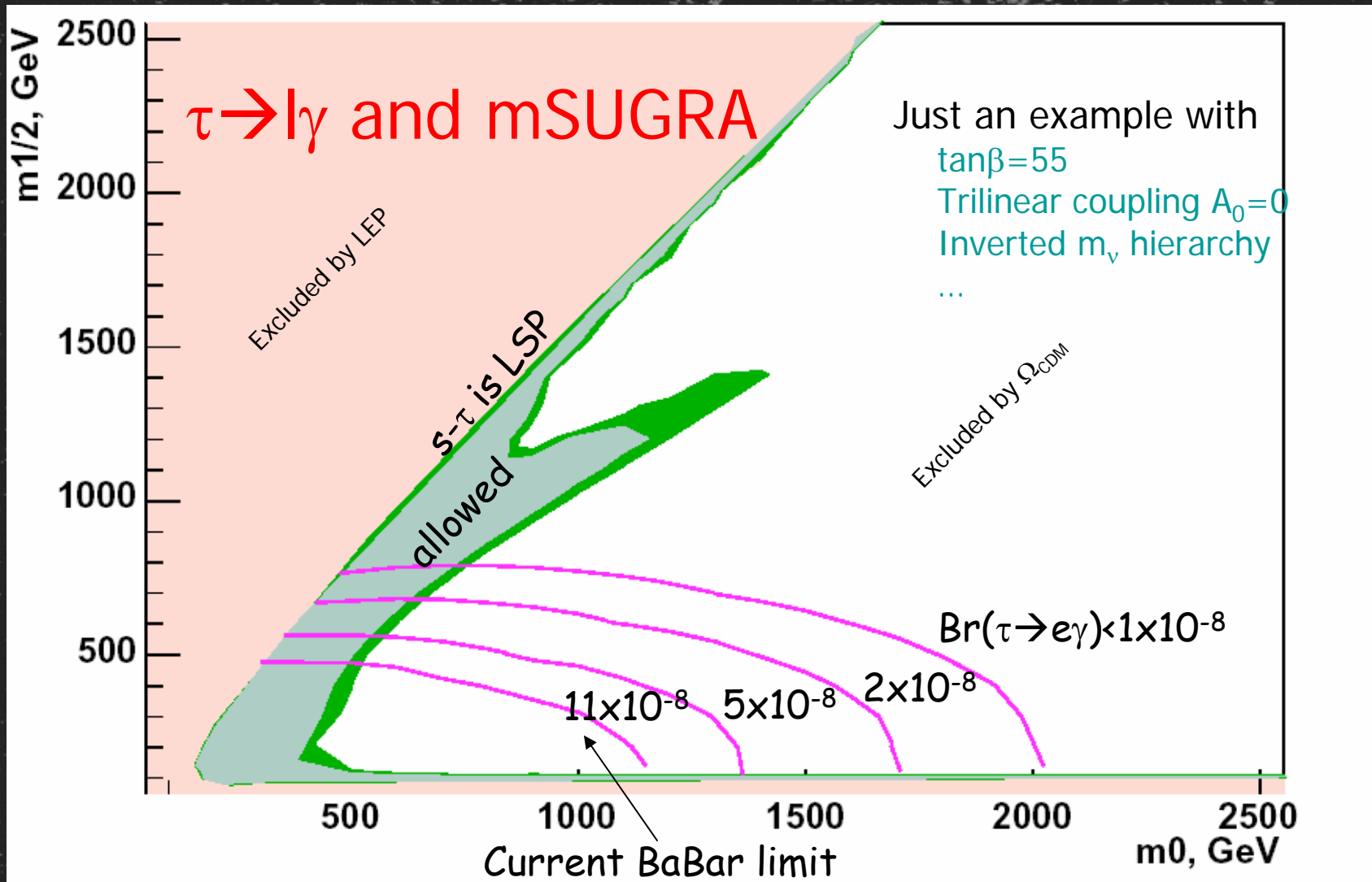
- 207×10^6 $e^+e^- \rightarrow \tau^+\tau^-$ events
- Observe 1 event in a $2\sigma \times 2\sigma$ signal box on 1.9 ± 0.4 expected background

$$\text{Br}(\tau^- \rightarrow e^- \gamma) < 1.1 \times 10^{-7} \text{ at } 90\% \text{ C.L.}$$

Previous limits (all @ 90% CL):

$\text{Br}(\tau^- \rightarrow \mu^- \gamma) < 0.68 \times 10^{-7}$	(BaBar, PRL 95 041802)
$\text{Br}(\tau^- \rightarrow \mu^- \gamma) < 3.1 \times 10^{-7}$	(Belle, PRL 92 171802)
$\text{Br}(\tau^- \rightarrow e^- \gamma) < 3.8 \times 10^{-7}$	(Belle, PLB 613 22)

Limits on New Physics – An Example



O. Igonkina, SUSY 2005

K. Honscheid, Ohio State University, Aspen 2006

Search for New Physics in the Charm Sector

- D⁰ Mixing**

Flavor eigenstates are not mass eigenstates

$$|D_{1,2}^0\rangle = p|D^0\rangle \pm q|\bar{D}^0\rangle \text{ with } M_{1,2} \text{ and } \Gamma_{1,2}$$

$$x \equiv \frac{\Delta m}{\Gamma}, \quad y \equiv \frac{\Delta\Gamma}{2\Gamma}$$

$$\text{mixing rate: } R_M = \frac{x^2 + y^2}{2}$$

- D⁰ Mixing is small in the SM**

box diagram: $x, y, < \text{few} \times 10^{-5}$

long distance: $x \sim 10^{-3}, y \sim 10^{-2}$

- Strong phase in hadronic decays**

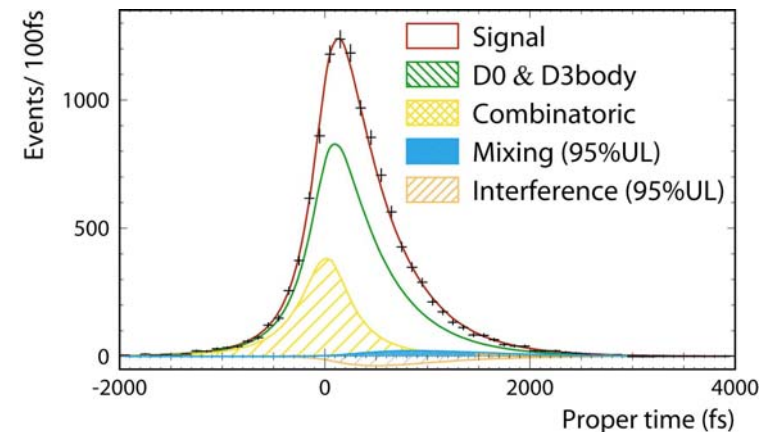
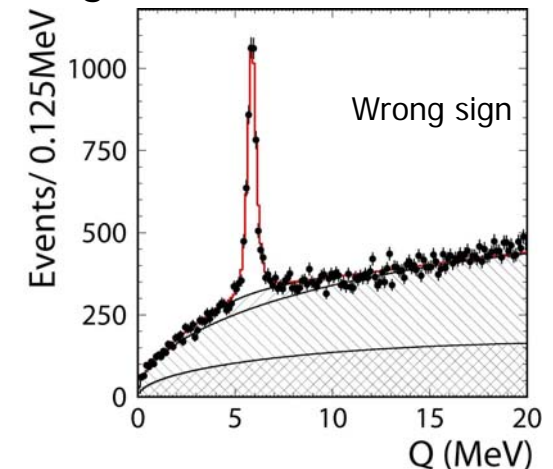
$$x' = x \cos\delta + y \sin\delta$$

$$y' = y \cos\delta - x \sin\delta$$

- Proper Time Fit**

$$\text{WS signal: } \left[R_D + \sqrt{R_D y'} t + \frac{x'^2 + y'^2}{4} t^2 \right] e^{-t}$$

Using D⁰ → K⁺π⁻, 400 fb⁻¹

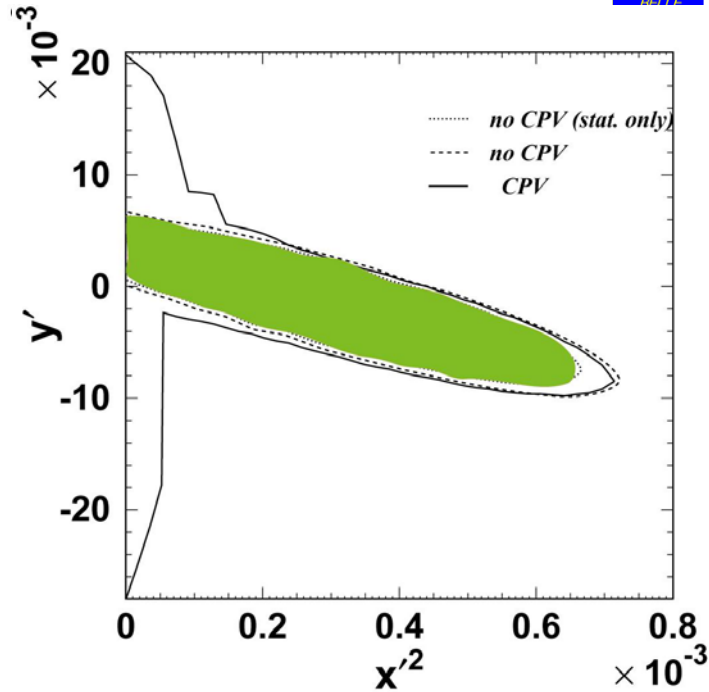


hep-ex/0601029



Experimental Limits on D^0 mixing

hep-ex/0601029

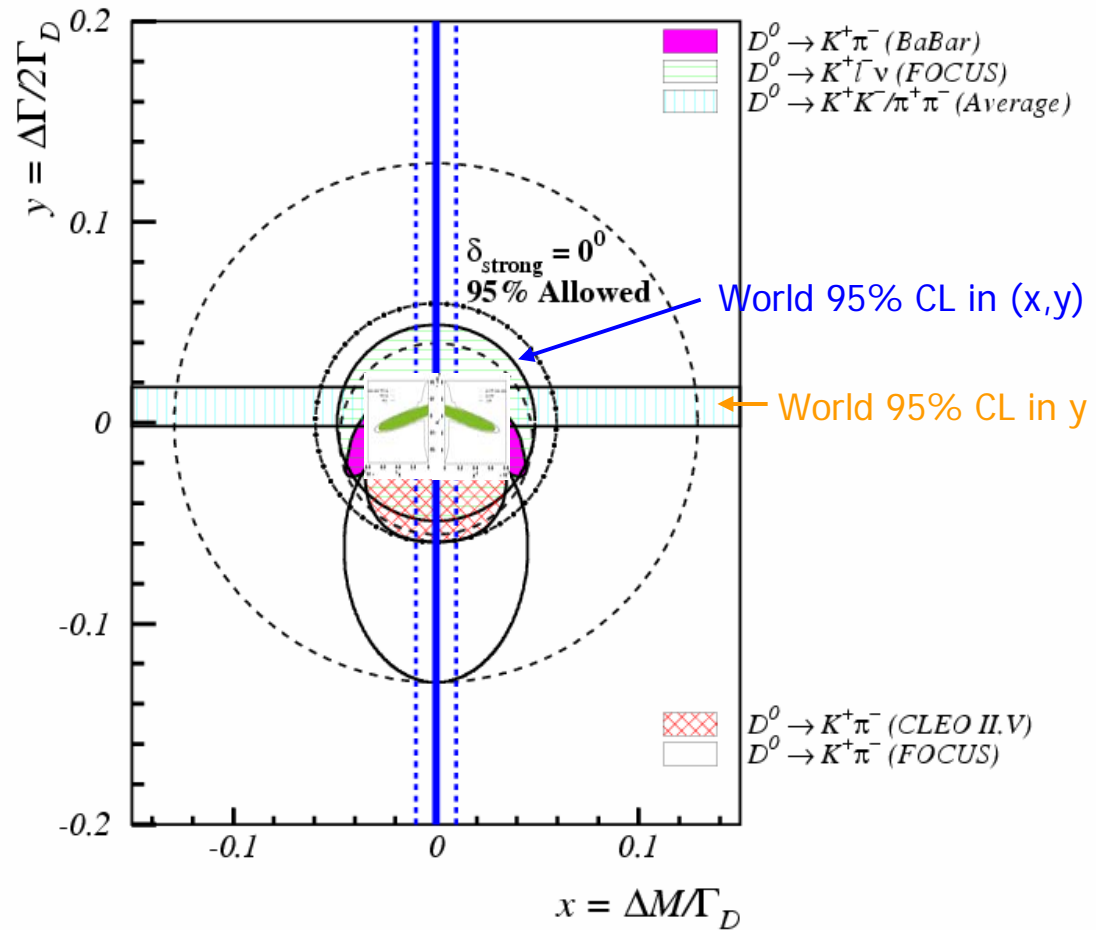


95% CL Limits (assuming CP)

$$x'^2 < 0.72 \times 10^{-3}$$

$$-9.9 \times 10^{-3} < y' < 6.8 \times 10^{-3}$$

Note: No-Mixing (0,0) has only 3.9% CL



G. Burdman and I. Shipsey, Ann. Rev. Nucl. Part. Sci. 53, 431 (2003)

[arXiv:hep-ph/030076]

(assuming $\delta = 0$, CPV = 0)

Rare Charm Decays and CP Violation

Experiment	Decay mode	A_{CP} (%)	Notes
BaBar	$D^+ \rightarrow K^- K^+ \pi^+$	$1.4 \pm 1.0 \pm 0.8$	
BaBar	$D^+ \rightarrow \phi^+ \pi^+$	$0.2 \pm 1.5 \pm 0.6$	Res. Substr. Of $D^+ \rightarrow K^- K^+ \pi^+$
BaBar	$D^+ \rightarrow K^{*0} K^+$	$0.9 \pm 1.7 \pm 0.7$	
CLEO II.V	$D^0 \rightarrow \pi^+ \pi^- \pi^0$	1 ± 8	Dalitz plot analysis
CDF	$D^0 \rightarrow K^+ K^-$	$2.0 \pm 1.2 \pm 0.6$	Direct CPV
CDF	$D^0 \rightarrow \pi^+ \pi^-$	$1.0 \pm 1.3 \pm 0.6$	Direct CPV
FOCUS	$D^0 \rightarrow K^+ K^- \pi^+ \pi^-$	$1.0 \pm 5.7 \pm 3.7$	T violation through triple product correlations
FOCUS	$D^+ \rightarrow K^0 K^+ \pi^+ \pi^-$	$2.3 \pm 6.2 \pm 2.2$	
FOCUS	$D_S \rightarrow K^0 K^+ \pi^+$	$-3.6 \pm 6.7 \pm 2.3$	

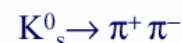
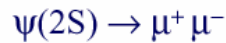
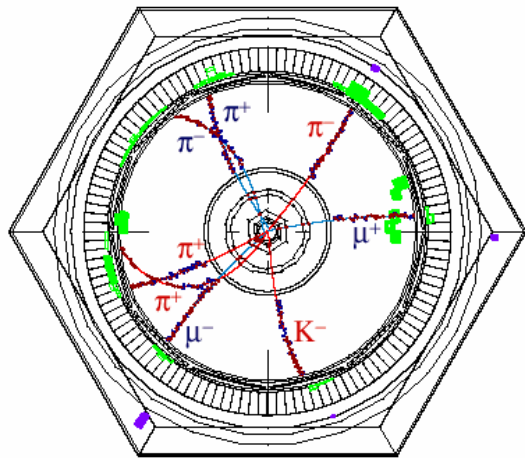
from S. Stone

Experimental Aside: Single B Meson Beams

Lots of interesting modes include one or more neutrinos.

“Beams” with a single, monochromatic B and without c, QED etc would be very useful for : $B \rightarrow \tau \nu$, $B \rightarrow \nu \nu$, $B \rightarrow K \nu \nu, \dots$

Fully reconstruct one of the Bs and study the remaining of the event \rightarrow closed kinematics, missing energy reconstruction

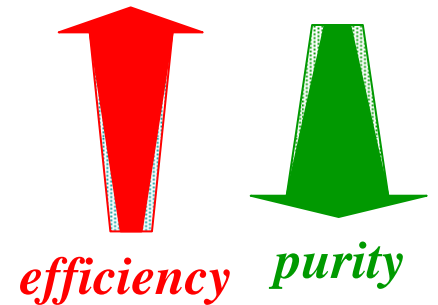


Tag types

Semileptonic $D^{(*)} l (\nu \pi)$
5K/fb⁻¹

Hadronic $D^{(*)} X$
3K/fb⁻¹

$$X = n\pi + m\pi^0 + pK + qK_s$$



Search for $B \rightarrow \tau \nu$

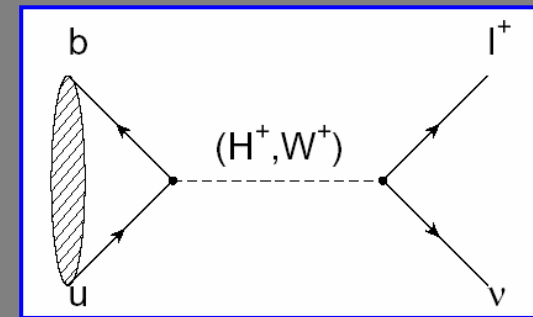
hep-ex/0507069



- SM decay proceeds via W-annihilation diagram

$$B^{SM}(B^+ \rightarrow \tau^+ \nu_\tau) = 9.3 \times 10^{-5} \left[\frac{f_{B^+}}{196 \text{ MeV}} \right]^2 \left[\frac{|V_{ub}|}{0.00367} \right]^2$$

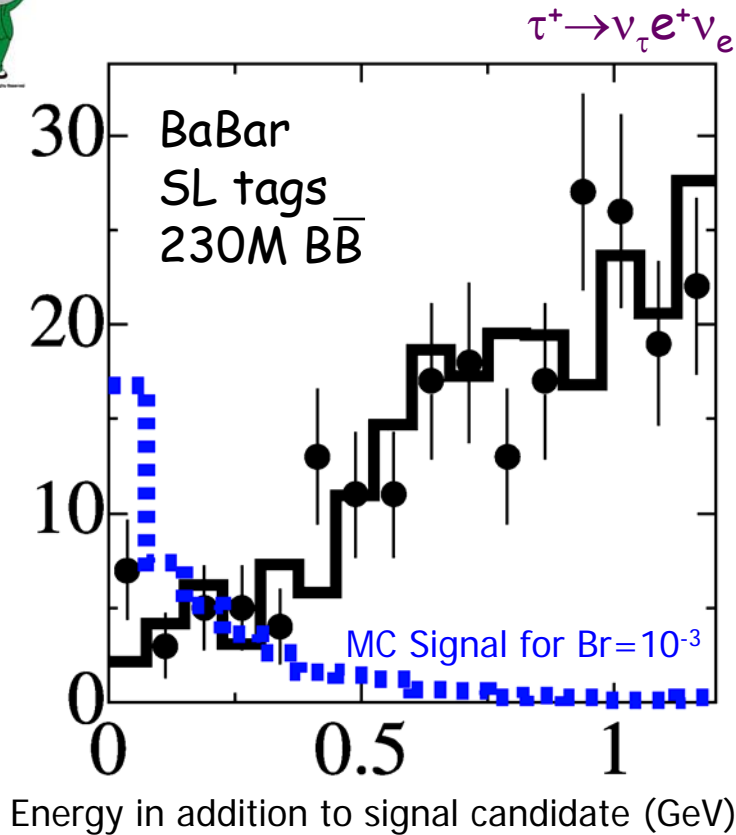
- Sensitive to new physics charged current



- Analysis:

- Undetected neutrinos result in large missing energy and few kinematic constraints – high background.
- Reduce the background by reconstructing the second B (“tag B”) in the event in the copious decay mode $B^- \rightarrow D^{*0} l^- \nu_l$
- Reconstruct $B^+ \rightarrow \tau^+ \nu_\tau$ with $\tau^+ \rightarrow l^+ \nu_{\text{bar}}$ or $\tau^+ \rightarrow h^+ \nu$, where $h = \pi, \rho, \text{ or } a_1$
- Require no additional charged tracks in the event

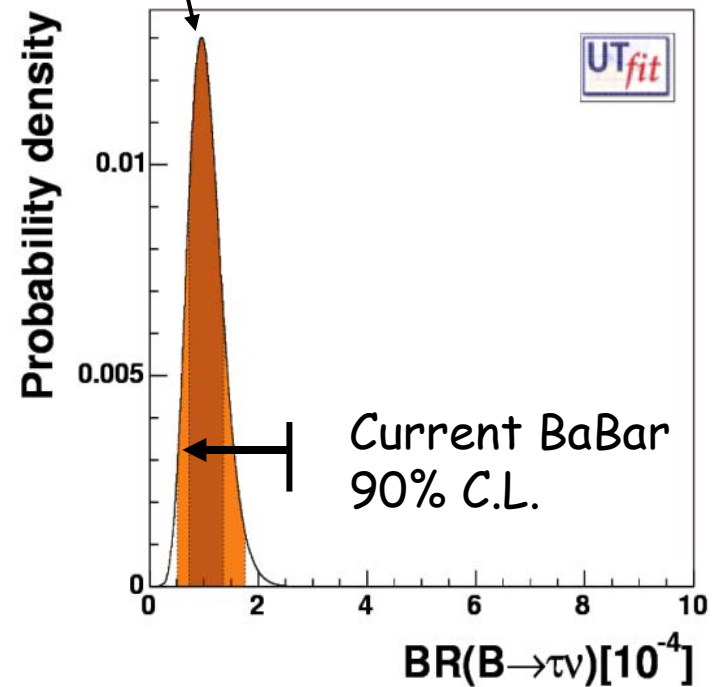
Results for $B \rightarrow \tau \nu$



No signal in 230 M $B\bar{B}$ events
90% CL Upper Limit
(Combined with hadronic tags)

$$Br(B^+ \rightarrow \tau^+ \nu_\tau) < 2.6 \times 10^{-4}$$

Expectations from U.T. fit



Close to the discovery of this mode or NP

...even closer

hep-ex/0507034

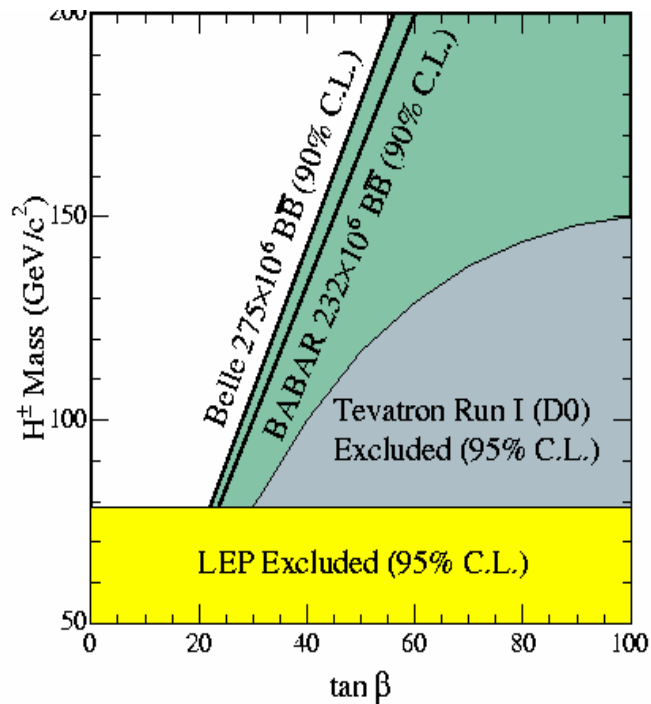
New Belle analysis using 250 fb^{-1}

$$BF(B \rightarrow \tau \nu) < 1.8 \times 10^{-4}$$



Higgs sensitivity

Limits on 2-Higgs Models from $B \rightarrow \tau \nu$

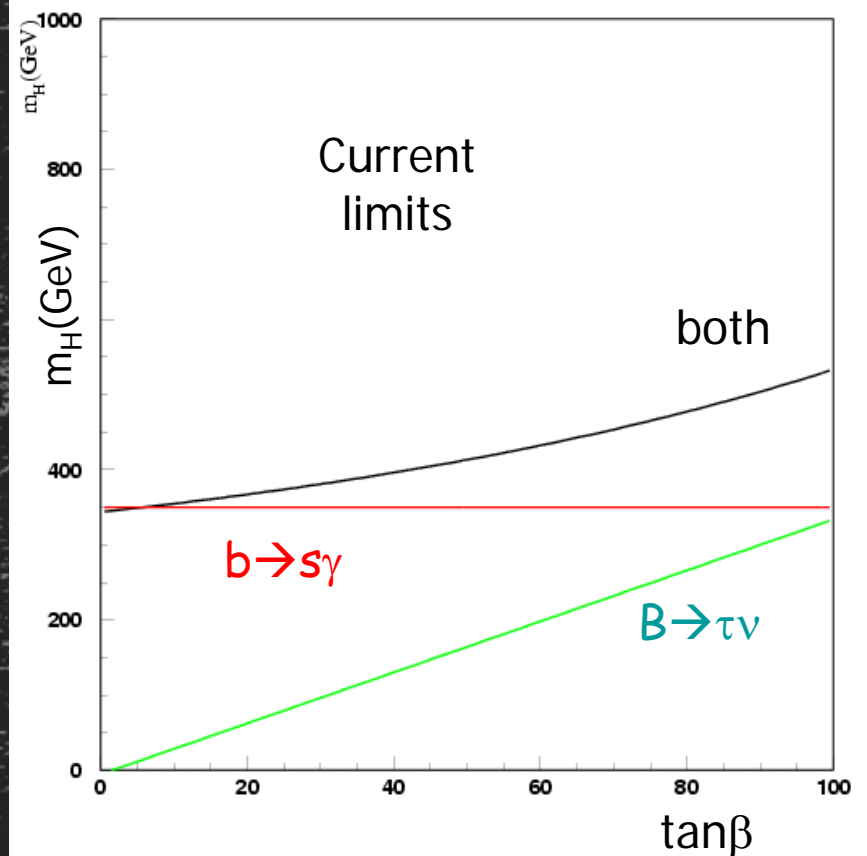


2HDM

Gambino, Misiak Nucl. Phys. B611 338

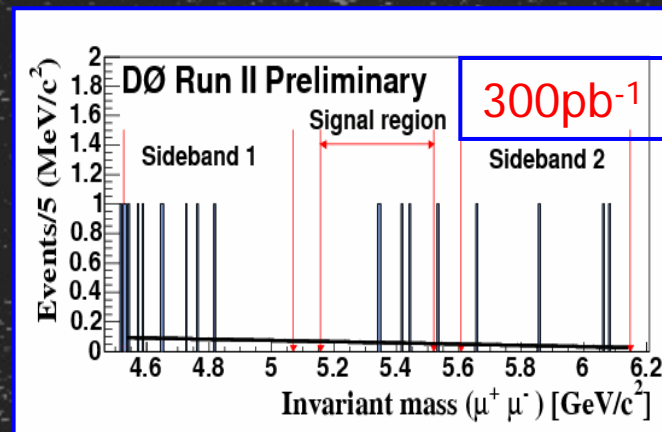
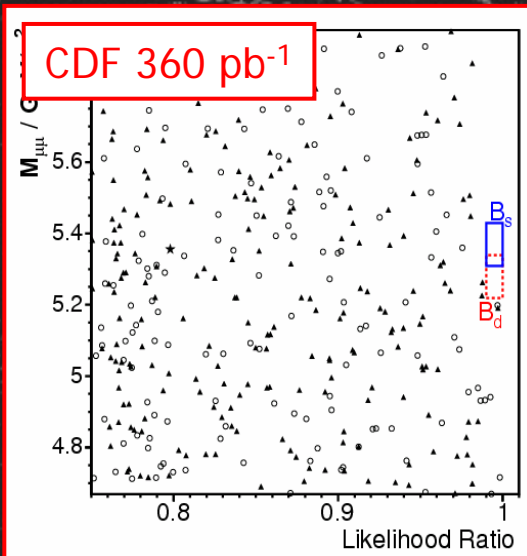
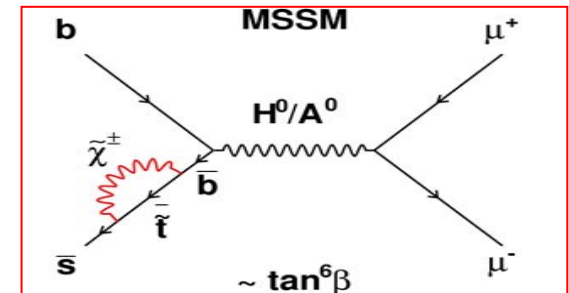
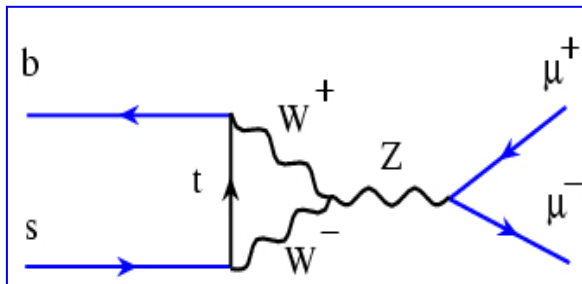
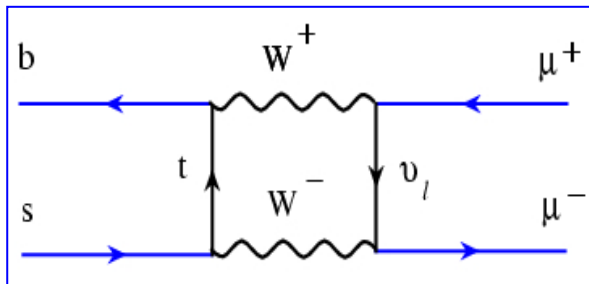
Hou Phys.Rev.D48:2342-2344,1993

18.10



Search for $B_s \rightarrow \mu^+ \mu^-$ at the Tevatron hep-ex/0508058

Standard model prediction: $\text{Br}(B_s \rightarrow \mu^+ \mu^-) = (3.5 \pm 0.9) \times 10^{-9}$



No Signal found

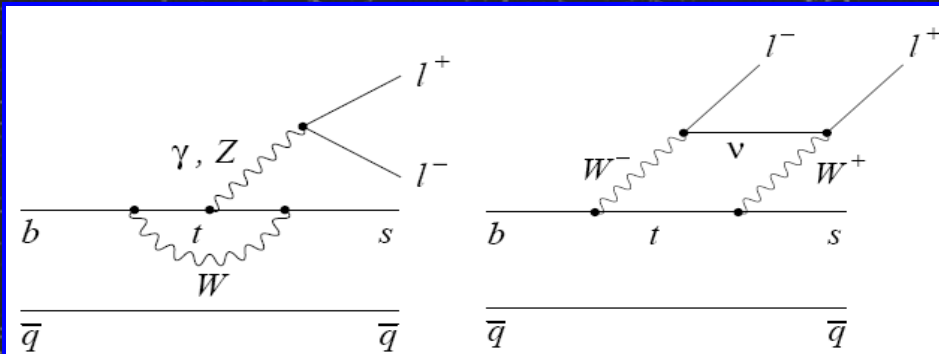
$$B_s \rightarrow \mu^+ \mu^- < 2.0 \times 10^{-7} \text{ CDF}$$

$$B_s \rightarrow \mu^+ \mu^- < 3.9 \times 10^{-7} \text{ D0}$$

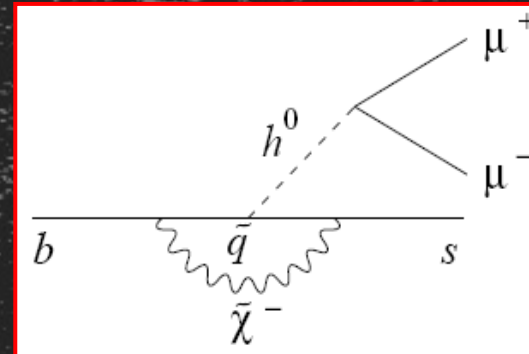
Combined (90% CL)

$$B_s \rightarrow \mu^+ \mu^- < 1.5 \times 10^{-7}$$

EW Penguins: $B \rightarrow K l^+ l^-$, $B \rightarrow K^* l^+ l^-$, and $B \rightarrow X_S l^+ l^-$



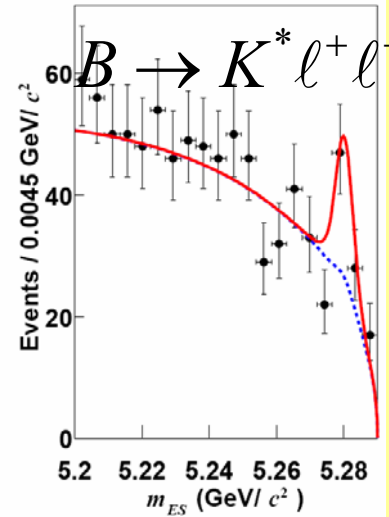
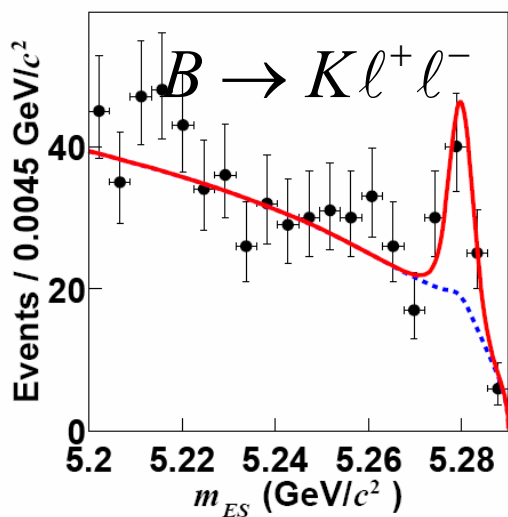
- With l^+l^- pair, can produce both pseudoscalar and vector mesons
- SM: $\text{Br}(B \rightarrow K l^+ l^-) \sim 4 \times 10^{-7}$ ($\pm 30\%$ theory)
 ~ 3 times that for K^*



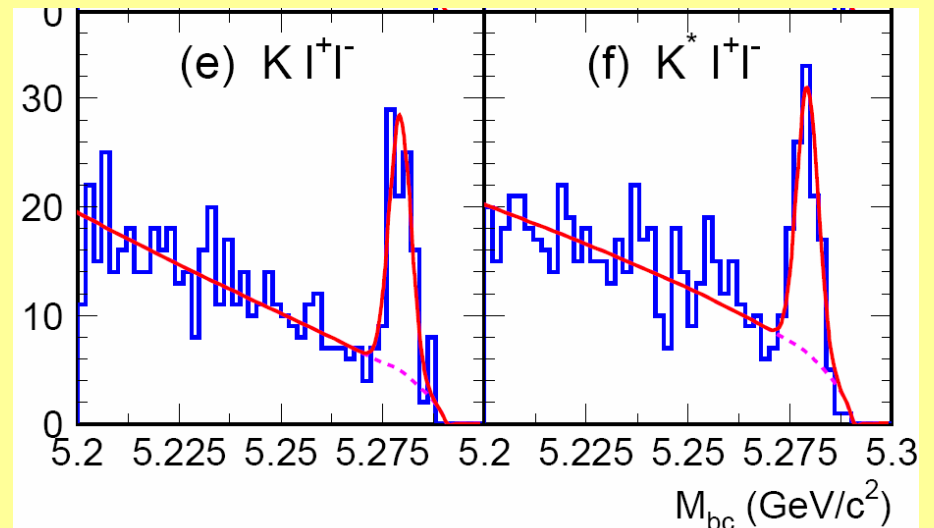
New Physics affects

- Rates
- Asymmetries (A_{FB} , CP)
- $\mu\mu/ee$ ratio

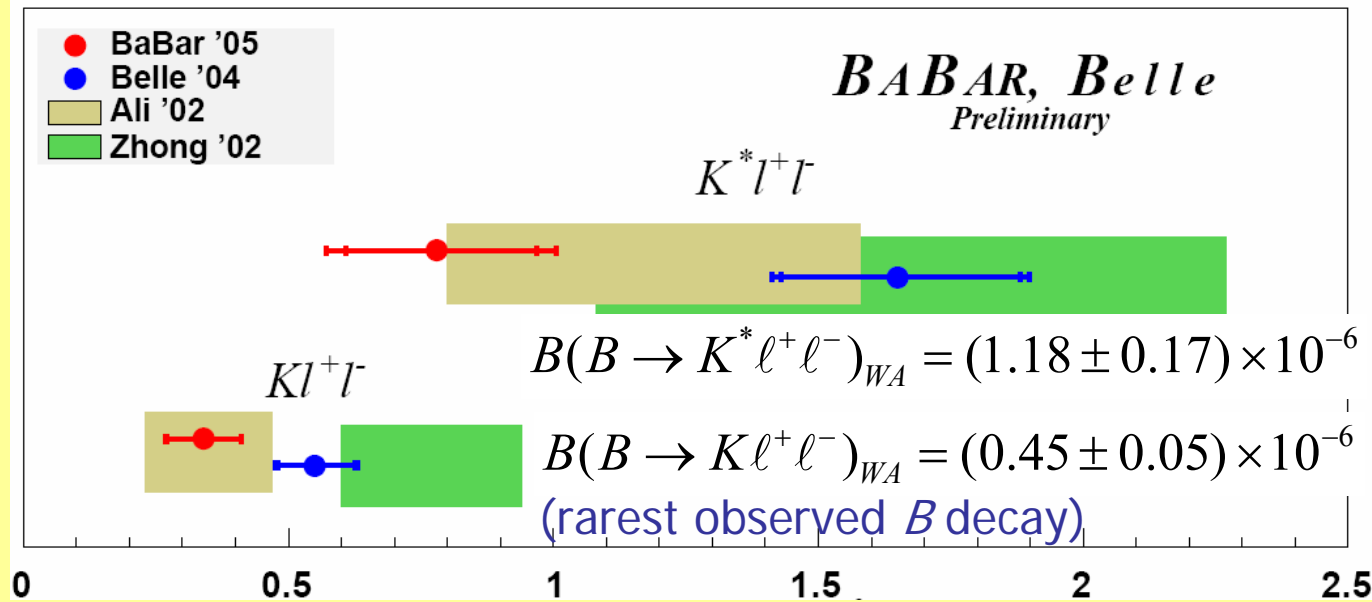
BABAR hep-ex/0507005 (229M BB)



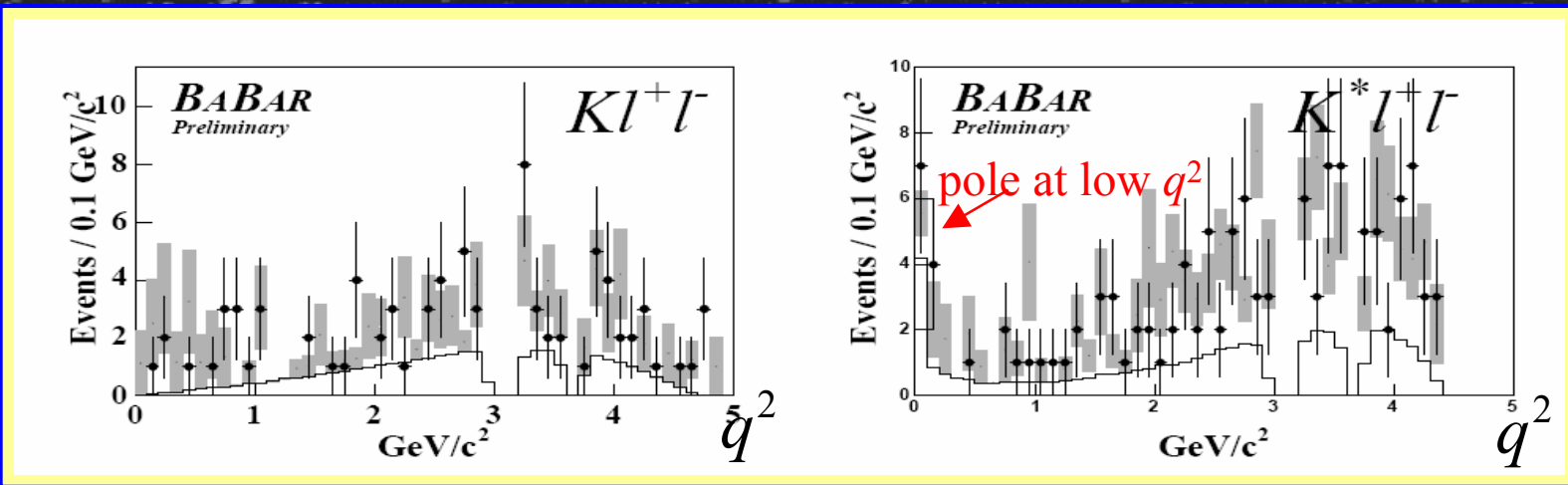
Belle prelim. hep-ex/0410006, 0508009



$B \rightarrow K l^+ l^-$ and $B \rightarrow K^* l^+ l^-$: branching fractions

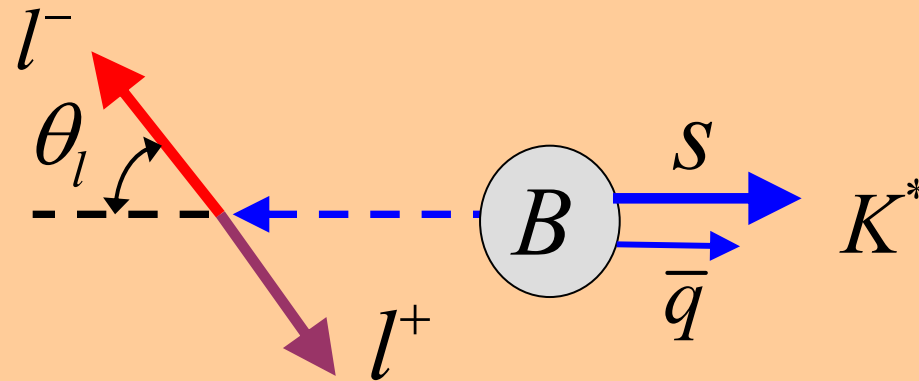


Theory errors mainly due to form factors.

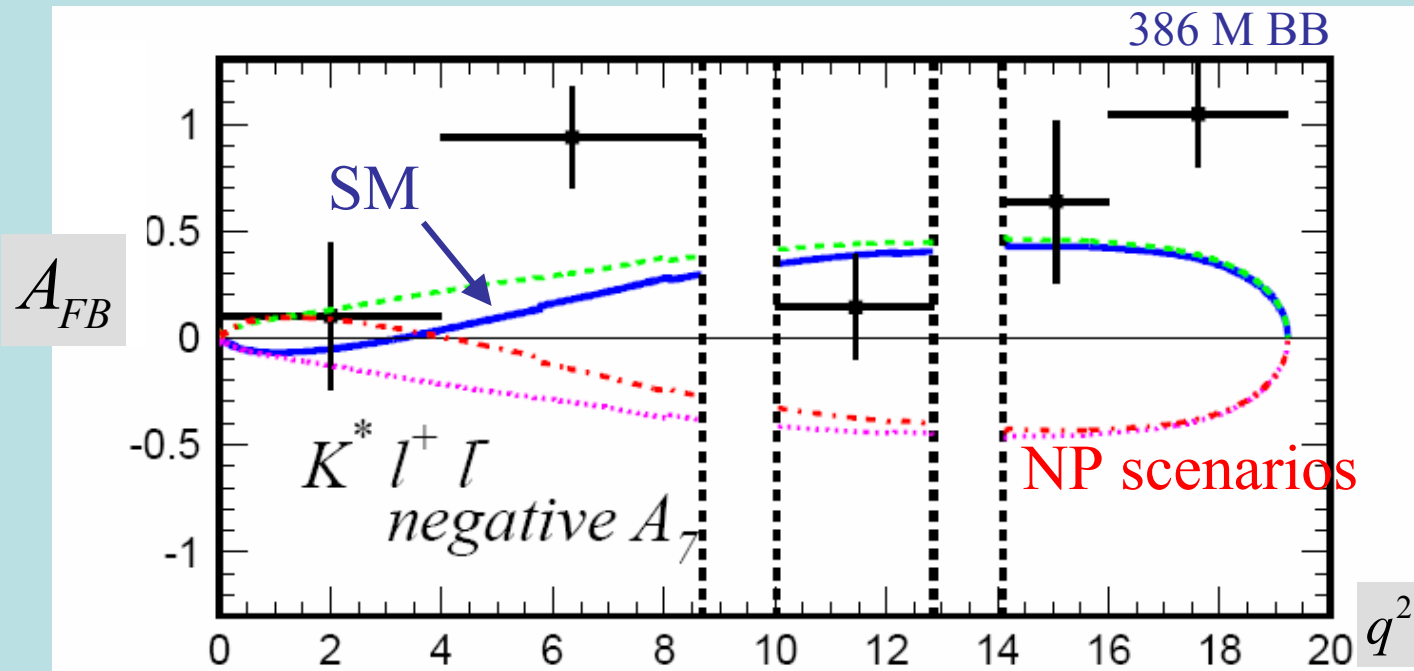


$B \rightarrow K^* l^+ l^-$: Lepton F-B Asymmetry

hep-ex/0508009



Lepton angular distribution in $l^+ l^-$ rest frame



→ constraints on Wilson coeffs describing short-distance physics

Getting Lost?

Little Higgs w
MFV UV fix

Extra dim w
SM on brane

Supersoft
SUSY breaking
Dirac gauginos

MSSM
MFV
small $\tan\beta$

Generic Little Higgs

Generic extra dim w SM in bulk

MSSM
MFV
large $\tan\beta$

SUSY GUTs

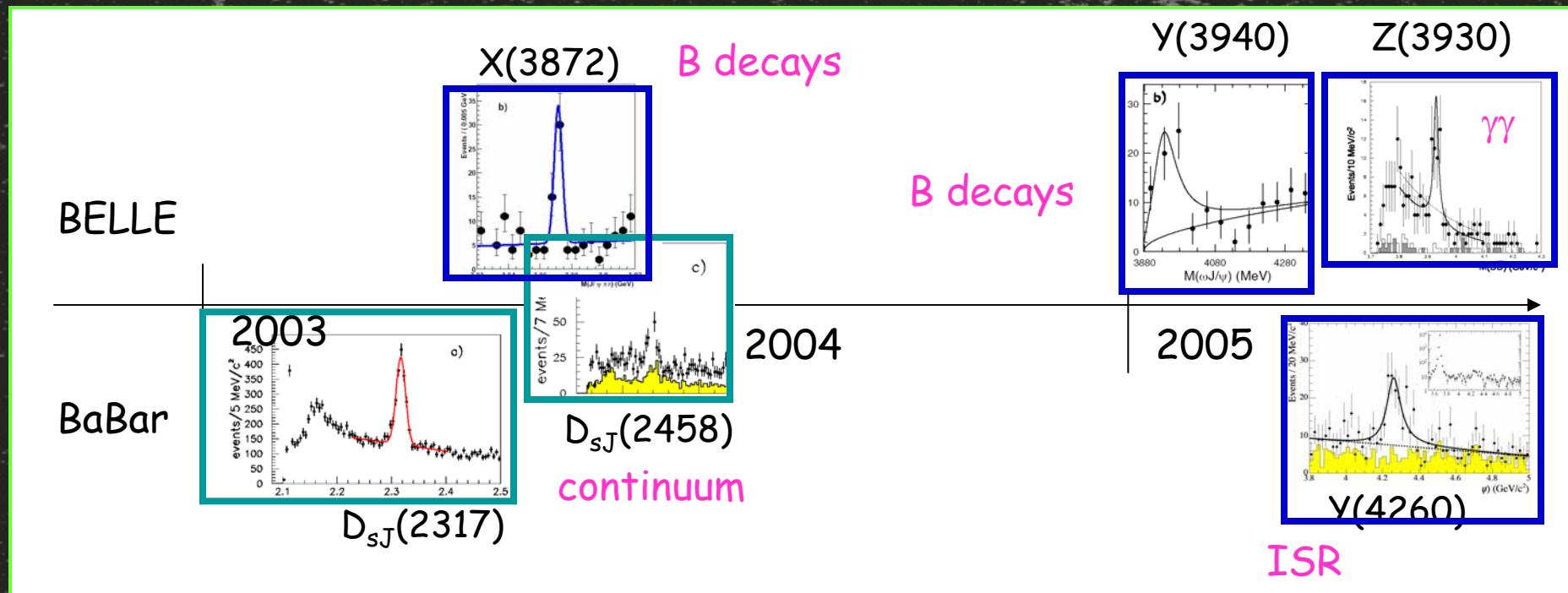
Effective SUSY

SM-like B physics

New Physics in B data

after G. Hiller

Be ready for surprises

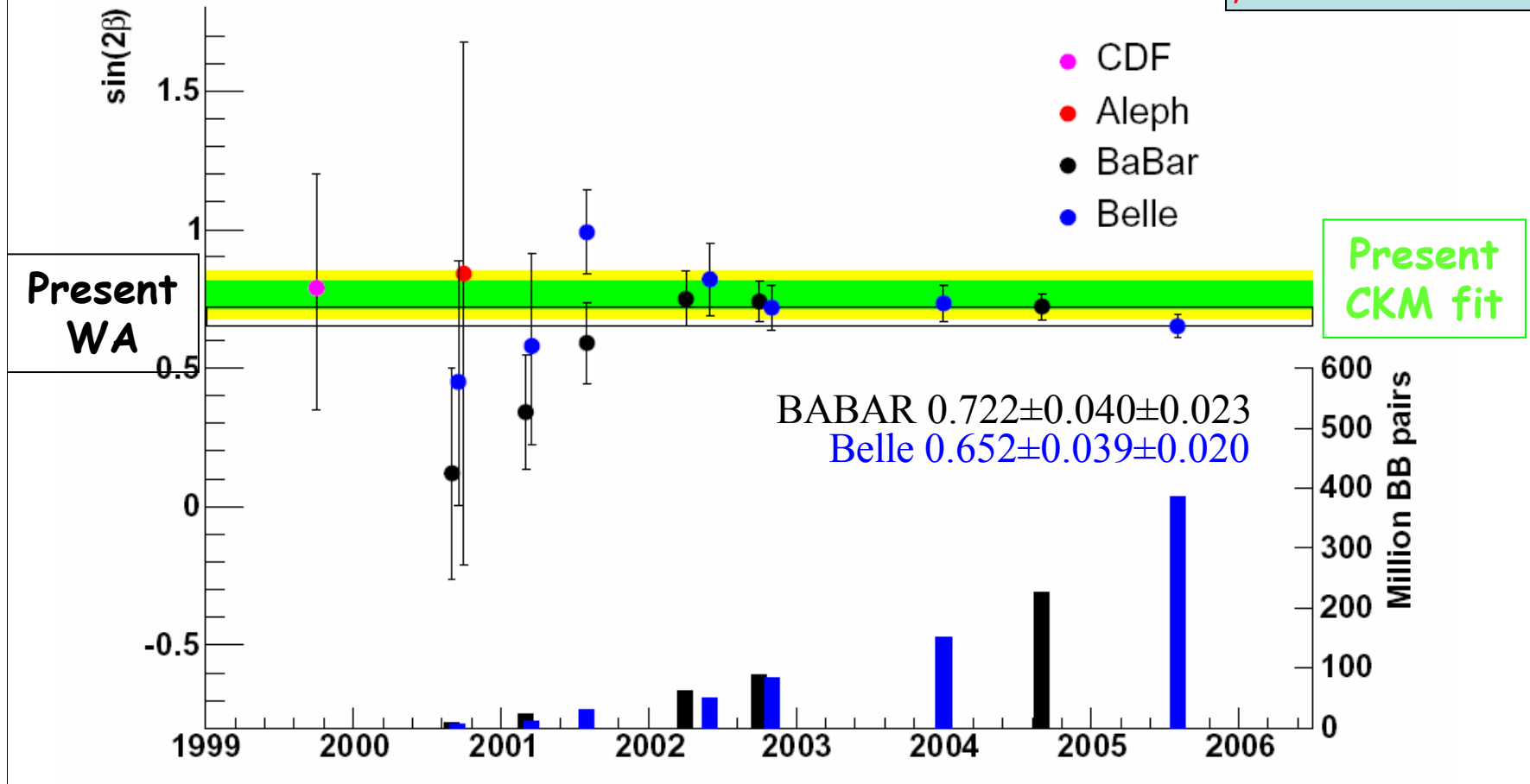
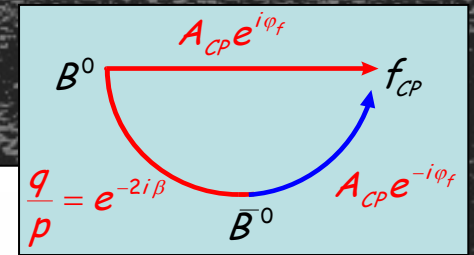


Several new particles have been observed by the B Factories

Different production mechanism \rightarrow Different J^{PC}

For a nice review by Swanson see hep-ph/0601110

CP Violation in the B System



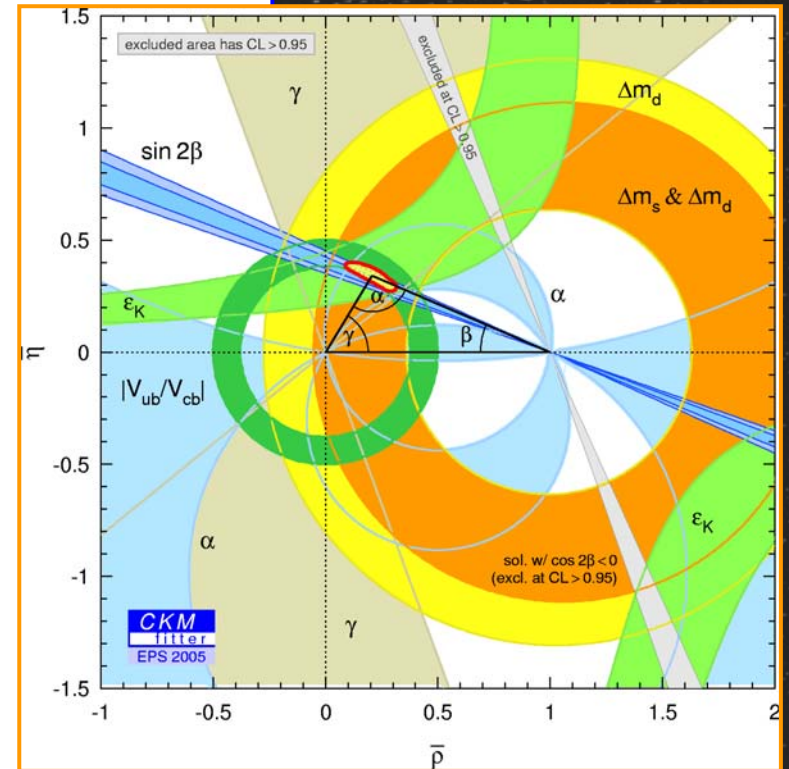
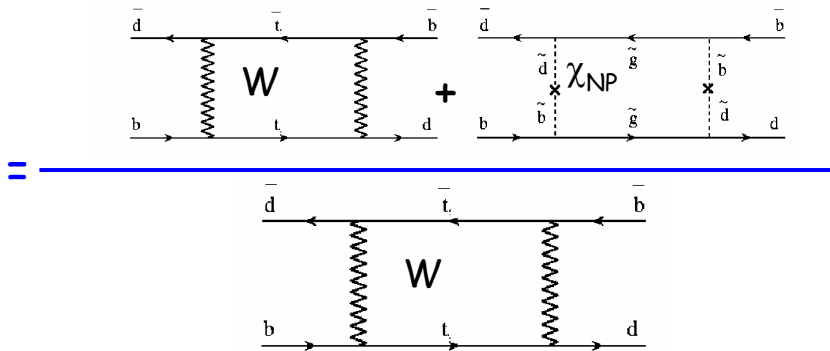
See talk by Aihara for more on CPV

Bounds on new physics from UT fits

CKM Model confirmed by many measurements
 Now look for New Physics as correction to CKM Model

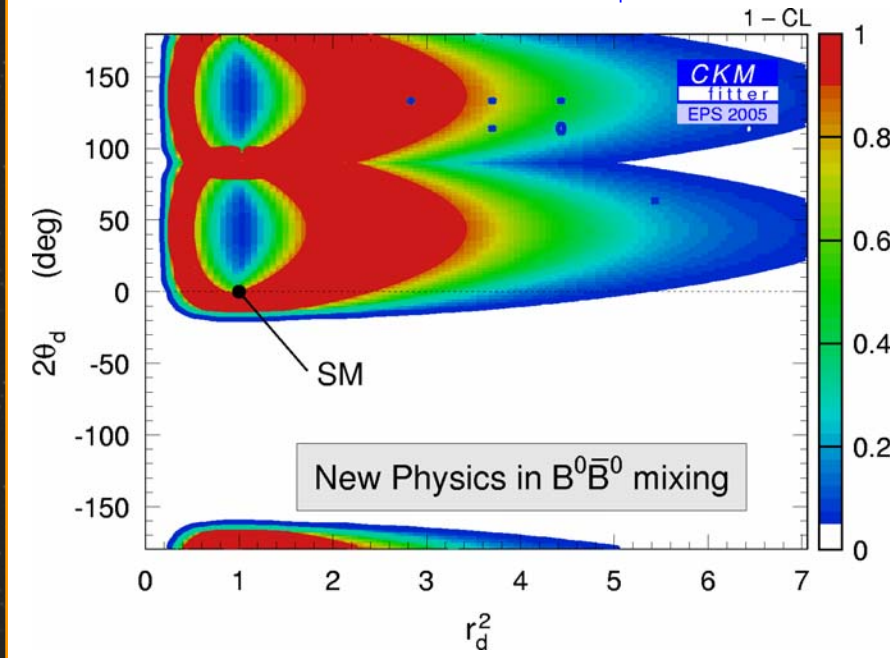
The fit to the unitarity triangle constraints:

$$C_{B_d} e^{2i\phi_{B_d}} = \frac{A_{SM} e^{2i\beta} + A_{NP} e^{2i(\beta + \phi_{NP})}}{A_{SM} e^{2i\beta}}$$

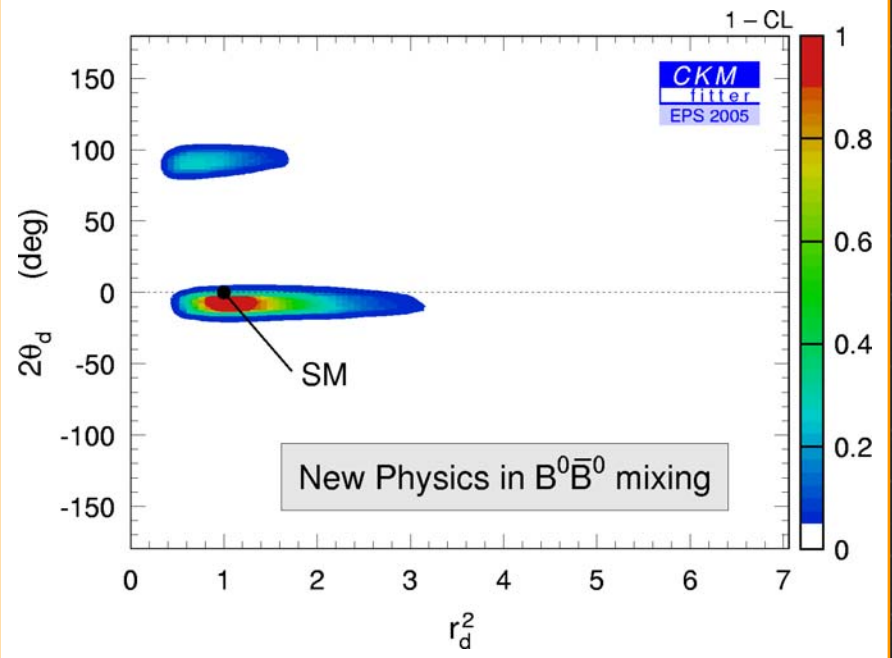


Bounds on new physics from UT fits

Constraints: $|V_{ub}|$, Δm_d , $S_{\psi K}$



add: α , γ



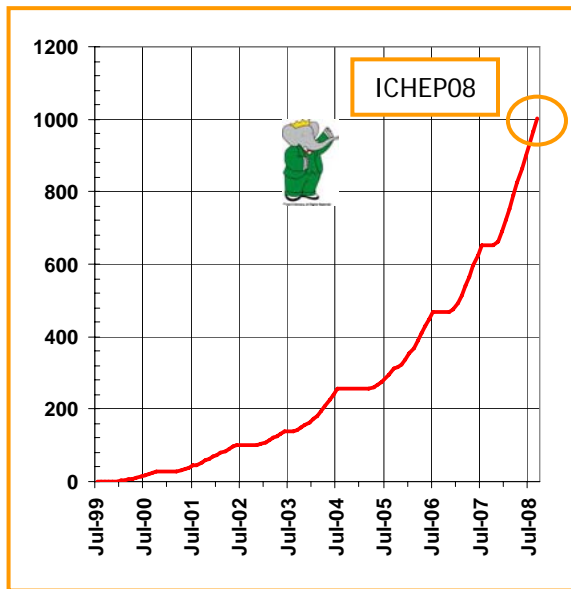
First constraints on Θ_d , C_{Bd}
 In terms of probed new physics mass
 scale ($\Lambda = m(\chi_{NP})$; $g_{NP} = \text{coupling}$)

$$\Lambda(\text{now}) \sim 5g_{NP} \text{ TeV}$$

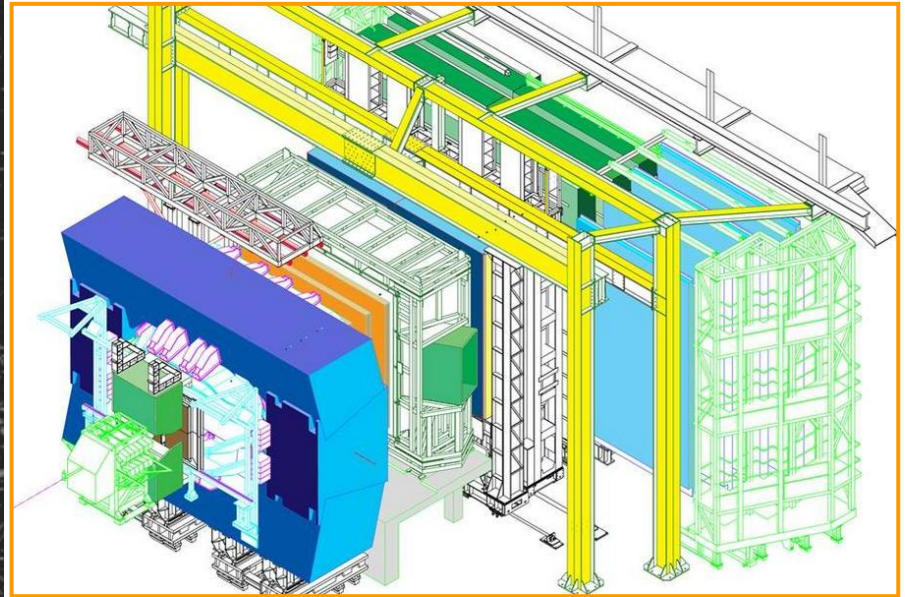
Ligeti,
 Silvestrini,
 Agashe et al

The next few years (2006 – 2008)

- Belle and BaBar
 - 1 ab^{-1} (2006)
 - 2 ab^{-1} (2008)
- Tevatron
 - 2 fb^{-1} (2006)
 - 8 fb^{-1} (2009)



- LHCb is nearing completion

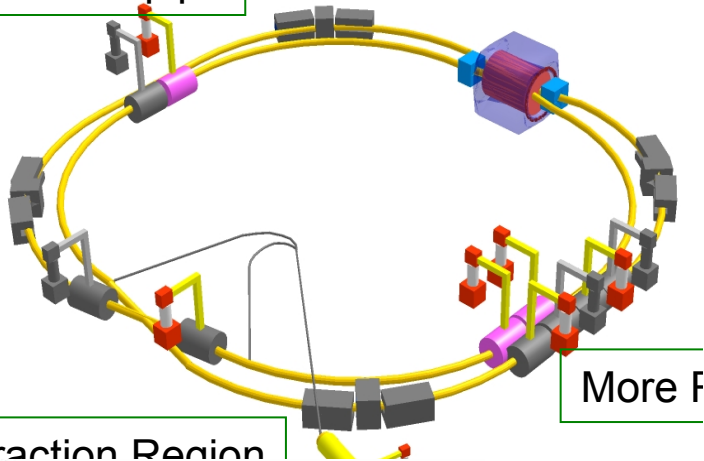


See talk by S. Stone on Thursday

Super B-Factory Plans at KEK and Frascati

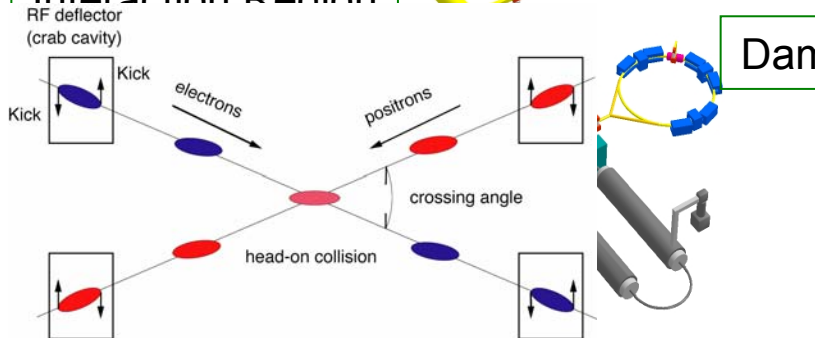
Design Luminosity $\sim 1 \times 10^{36}$ /cm²/sec
 Synergy with ILC
 Lots of R&D needed

New Beam pipe

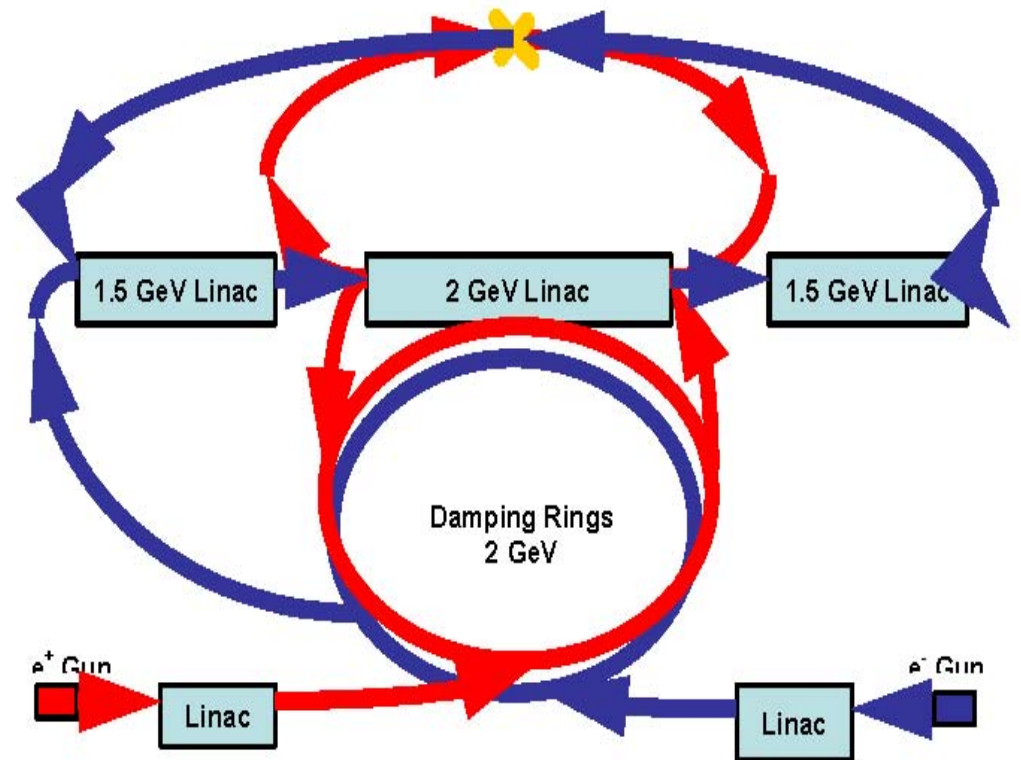


More F

Interaction Region



$$L = 4 \times 10^{35} / \text{cm}^2 / \text{sec}$$



KEK

Frascati

Next Super B Workshop in Frascati, March 16-18, 2006

Have Ideas – Need Statistics

Mode	BR_{SM}	Notes on New Physics
$b \rightarrow s\gamma$	$\sim 3 \cdot 10^{-4}$	BF, A_{CP} , and A_{FB} important
$b \rightarrow s\gamma$	$\sim 10^{-5}$ each	BF not critical. Need events to measure S_{CP}
$B \rightarrow XII$	$\sim 10^{-6}$ each	BF, A_{CP} , and A_{FB} important
$B \rightarrow X_{VV}$	$\sim 10^{-6}$ each	Up to 10^{-5} each
$D \rightarrow XII$	$\sim 10^{-6}$ each	Up to 10^{-5} each
$B \rightarrow \tau\nu$	$\sim 10^{-4}$	Experiments close to SM sensitivity
$\tau \rightarrow l\gamma$	$\sim 10^{-40}$	Up to 10^{-8}
$B \rightarrow II$	$< 10^{-11}$	Up to 10^{-5}
$D \rightarrow II$	$< 10^{-9}$	Up to 10^{-6}

Additional Transparencies

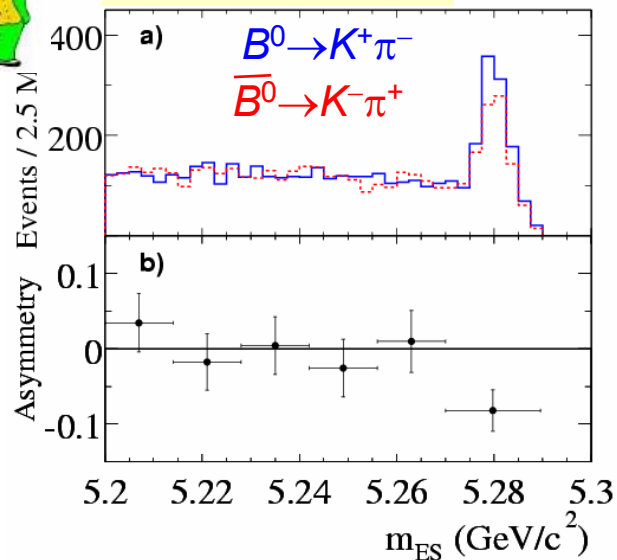
K. Honscheid
Ohio State University
Aspen 2006

Let's rule out at least one NP model

Observation of direct CP violation in $B^0 \rightarrow K^+ \pi^-$



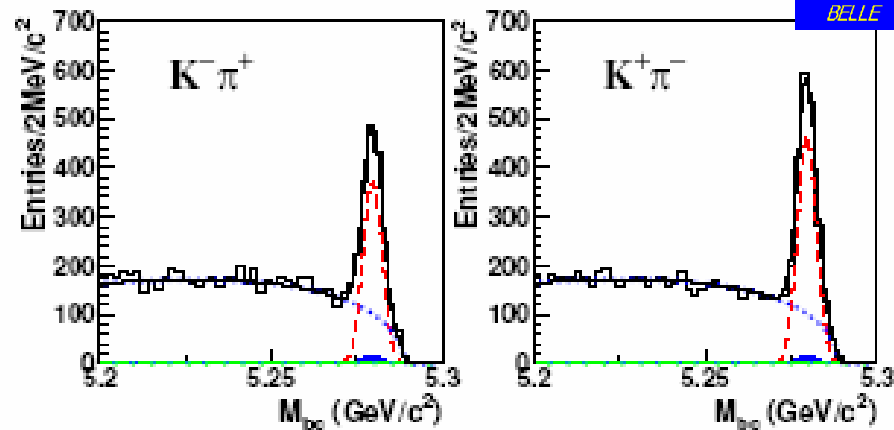
232x10⁶ $B\bar{B}$'s



BaBar 2004

$$A_{CP} = -0.133 \pm 0.030 \pm 0.009$$

Belle ($386 \times 10^6 B\bar{B}$)

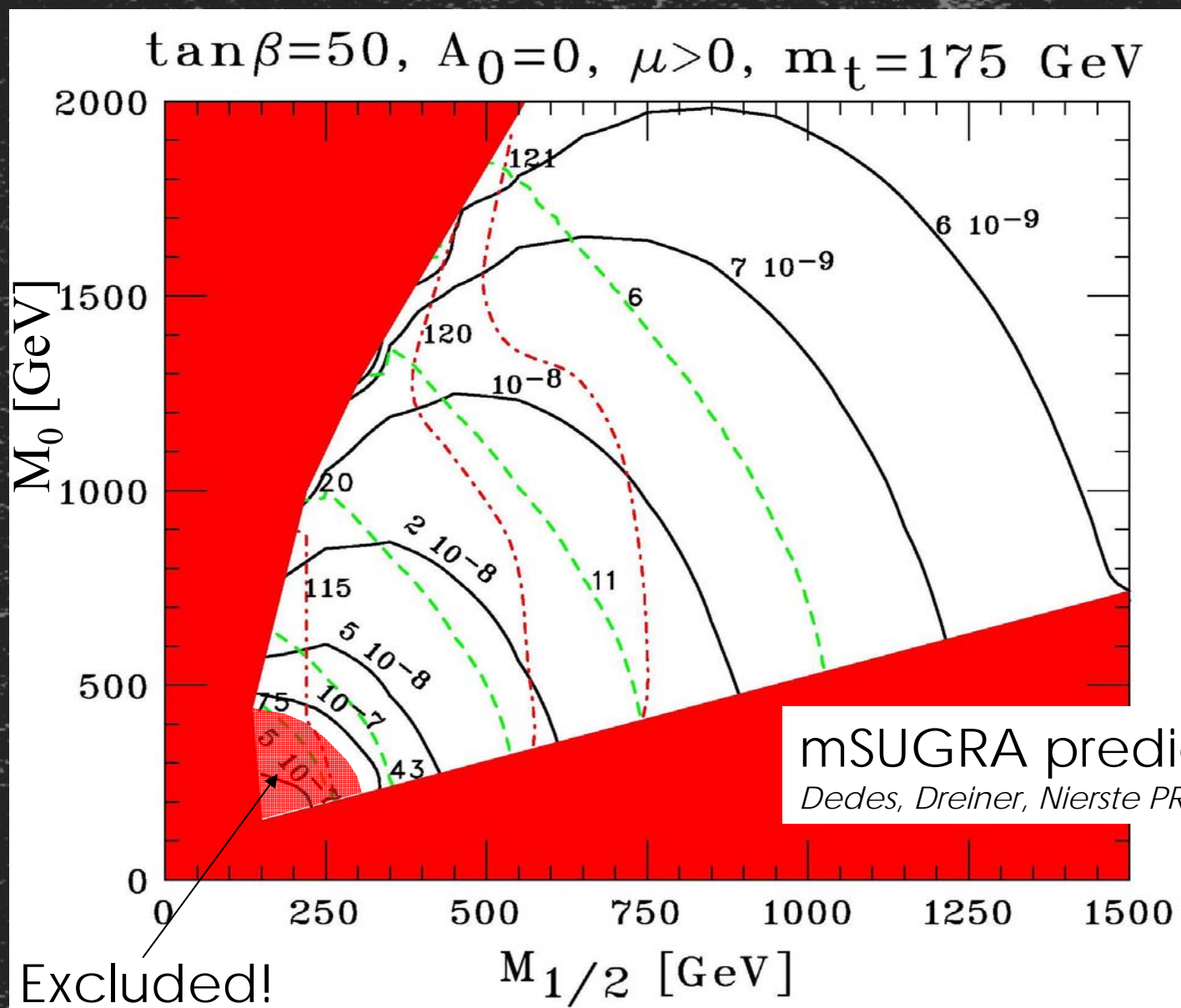


New Belle Result:

$$-0.113 \pm 0.022 \pm 0.008$$

➔ Superweak Model (Wolfenstein) is really out

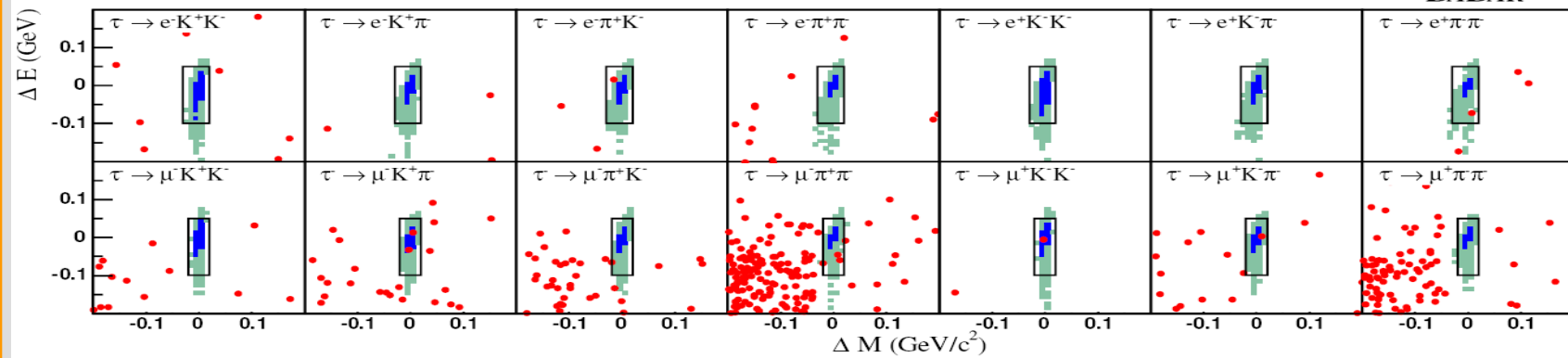
Implications of $B_s \rightarrow \mu^+ \mu^- < 1.5 \times 10^{-7}$



mSUGRA prediction:
Dedes, Dreiner, Nierste PRL87:251804,2001

Search for LFV in $\tau^- \rightarrow l^\pm hh'$

PRL 95, 191801 (2005)



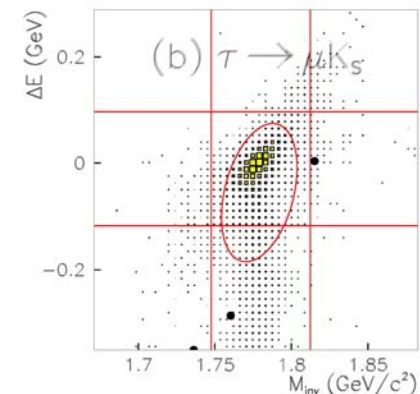
$\tau^- \rightarrow$	$e^-K^+K^-$	$e^-K^+\pi^-$	$e^-\pi^+K^-$	$e^-\pi^+\pi^-$	$e^+K^-K^-$	$e^+K^-\pi^-$	$e^+\pi^-\pi^-$
UL($\times 10^{-7}$)	1.4	1.7	3.2	1.2	1.5	1.8	2.7
$\tau^- \rightarrow$	$\mu^-K^+K^-$	$\mu^-K^+\pi^-$	$\mu^-\pi^+K^-$	$\mu^-\pi^+\pi^-$	$\mu^+K^-K^-$	$\mu^+K^-\pi^-$	$\mu^+\pi^-\pi^-$
UL($\times 10^{-7}$)	2.5	3.2	2.6	2.9	4.8	2.2	0.7

hep-ex/0509016



$\text{Br}(\tau^- \rightarrow e^-K_S) < 5.6 \times 10^{-8}$ at 90% C.L.

$\text{Br}(\tau^- \rightarrow \mu^-K_S) < 4.9 \times 10^{-8}$ at 90% C.L.



First Search for $B^0 \rightarrow \tau^+ \tau^-$

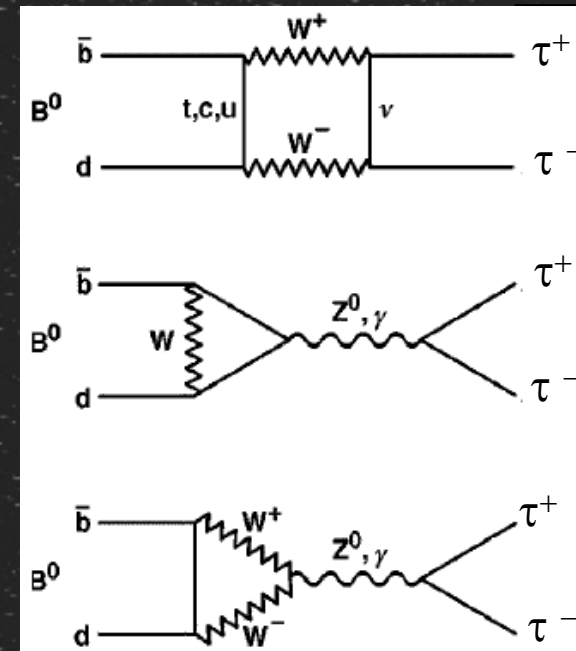
hep-ex/0501115



- SM expectation $\sim 10^{-7}$
(Compare: 10^{-11} for $\mu^+ \mu^-$, 10^{-15} for $e^+ e^-$)
- Helicity $(m_\tau/m_B)^2$ and Cabibbo $(V_{tb} V_{td}^*)$ suppressed
- Very clean theoretically
- Small SM \rightarrow Sensitive to new physics in the loops

● Analysis

- Reconstruct the tag B in decays to $D^{(*)}$ and up to 5 kaons and pions
- Reconstruct the signal decay $B^0 \rightarrow \tau^+ \tau^-$, with $\tau \rightarrow 1$ -prong decays
- Require no additional charged tracks in the event
- Require little remaining energy: $E_{\text{extra}} < 0.11$ GeV
- Use correlations between E_{extra} and the momenta of the reconstructed τ daughters in a neural net to further reduce the background



$B^0 \rightarrow \tau^+ \tau^-$ Results

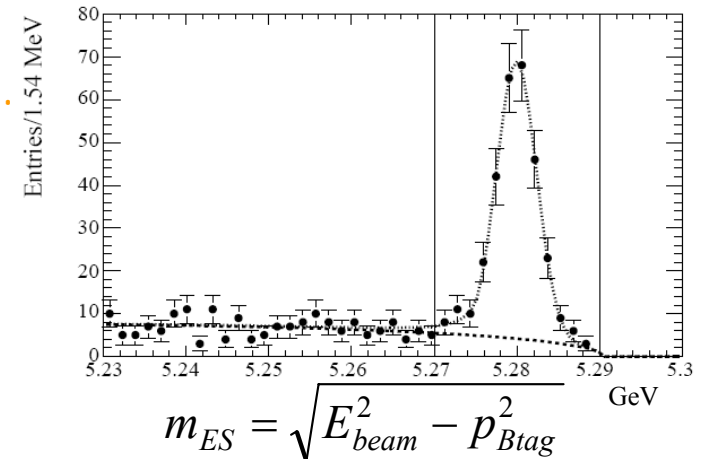
hep-ex/0501115



Using $232 \times 10^6 Y(4S) \rightarrow B\bar{B}$ events we observe 263 ± 19 events with 281 ± 40 expected background.

➔ First limit on this mode

$$\text{Br}(B^0 \rightarrow \tau^+ \tau^-) < 3.2 \times 10^{-3} \text{ at } 90\% \text{ C.L.}$$



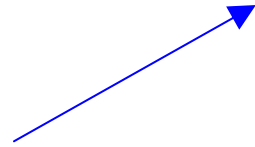
Yields a constraint on leptoquark parameter. For example

$$\lambda_R^{33} \lambda_R^{13} < 1.1 \times 10^{-2} \left[\frac{m_{S_{1/2}}}{100 \text{ GeV}} \right]^2$$

↙
↘

RH coupling to generations i,j
Leptoquark doublet mass

SM



Sign of C_7 flipped



Constraints on C_i from $B(B \rightarrow X_s l^+ l^-)$

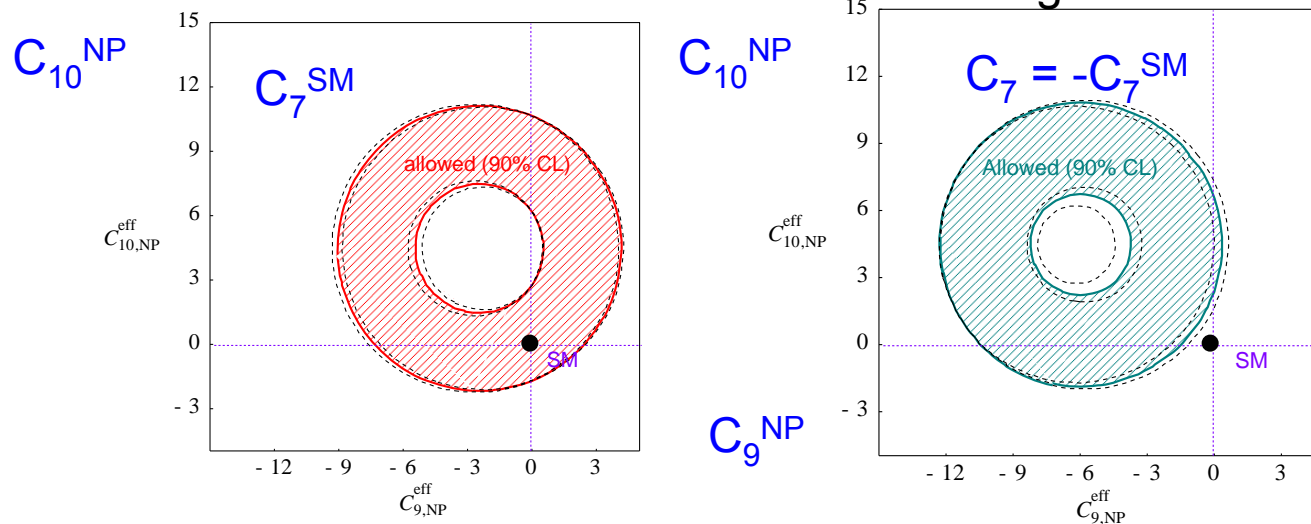


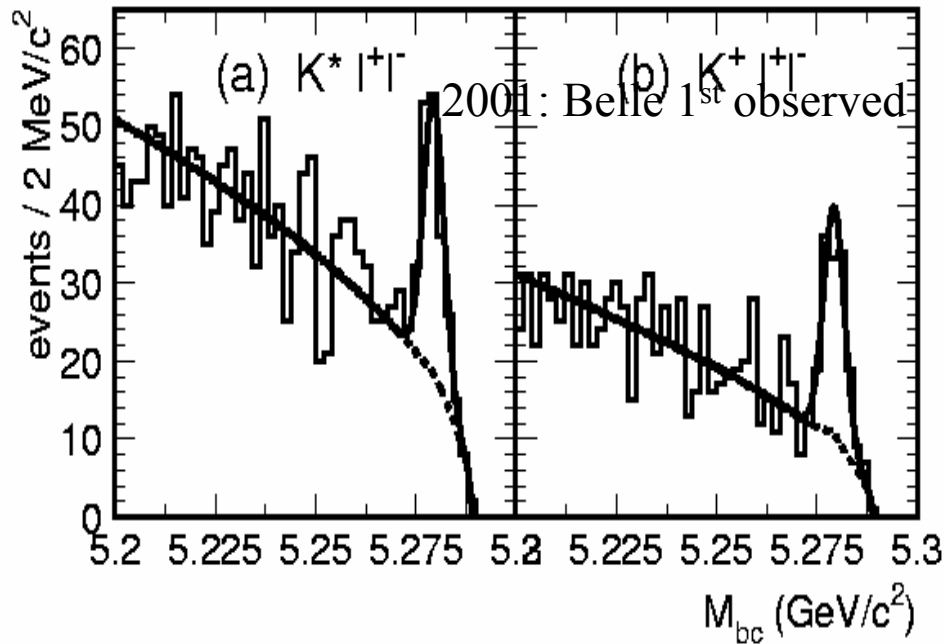
P.Gambino, U.Haisch and M.Misiak PRL 94 061803 (2005)

- Clean prediction for $B(B \rightarrow X_{sl})$ with $1 < q^2 < 6 \text{ GeV}^2$ is available.
 - Combine Belle and Babar results
 - Sign of C_7 flipped case with SM C_9 and C_{10} values is unlikely.

BF	Belle	Babar	WA	SM	$C_7 = -C_7^{\text{SM}}$
$q^2 > (2m_\mu)^2$	4.11 ± 1.1	5.6 ± 2.0	4.5 ± 1.0	4.4 ± 0.7	8.8 ± 0.7
$1 < q^2 < 6 \text{ GeV}^2$	1.5 ± 0.6	1.8 ± 0.9	1.60 ± 0.5	1.57 ± 0.16	3.30 ± 0.25

Donut : 90% CL allowed region





Sample for $B \rightarrow K^* l l$ events 113 ± 13

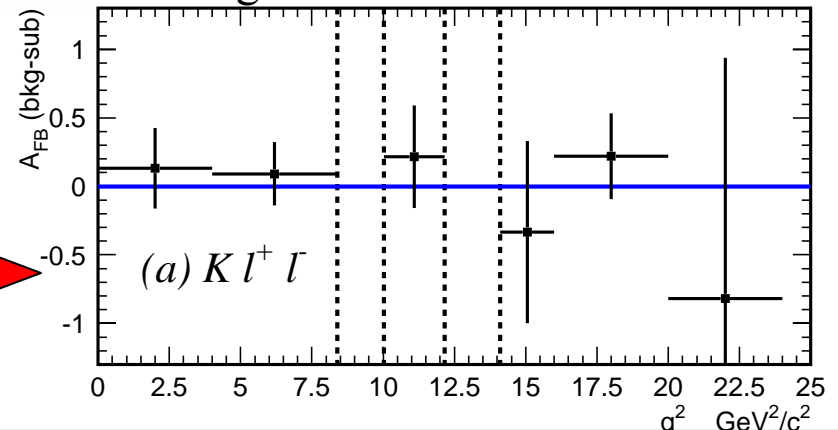
$B \rightarrow K l l$ control sample 96 ± 12

Consistent with flat



$$\begin{aligned}
 & P(q^2, \cos \theta; A_9/A_7, A_{10}/A_7) \\
 &= f_{\text{sig}} \epsilon_{\text{sig}}(q^2, \cos \theta) \frac{d^2 \Gamma}{dq^2 d \cos \theta}(q^2, \cos \theta) / N_{\text{sig}} \\
 &+ f_{\text{cfcl}} \epsilon_{\text{cfcl}}(q^2, \cos \theta) \frac{d^2 \Gamma}{dq^2 d \cos \theta}(q^2, \cos \theta) / N_{\text{cfcl}} \\
 &+ f_{\text{ifcl}} \epsilon_{\text{ifcl}}(q^2, \cos \theta) \frac{d^2 \Gamma}{dq^2 d \cos \theta}(q^2, -\cos \theta) / N_{\text{ifcl}} \\
 &+ f_{X_s, ll} \mathcal{P}_{X_s, ll}(q^2, \cos \theta) \\
 &+ f_{\text{dilep}} \left\{ (1 - f_{K^* l h}) \mathcal{P}_{\text{dilep}}(q^2, \cos \theta) \right. \\
 &\quad \left. + f_{K^* l h} \mathcal{P}_{K^* l h}(q^2, \cos \theta) \right\} \\
 &+ f_{K^* h h} \mathcal{P}_{K^* h h}(q^2, \cos \theta) + f_{\psi} \mathcal{P}_{\psi}(q^2, \cos \theta), \quad (
 \end{aligned}$$

Treat $q^2, \cos(\theta)$ dependence of bkg.



New Measurement of $A_{FB}(q^2)$ in K^*II

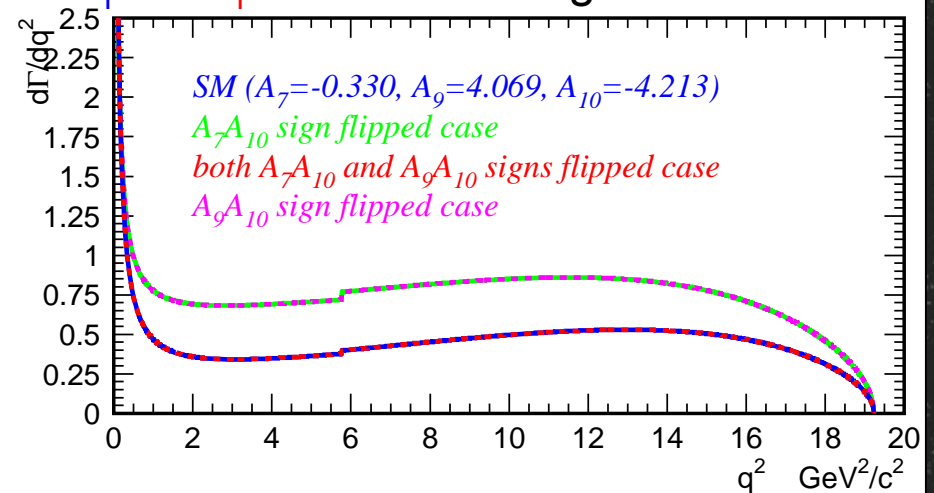
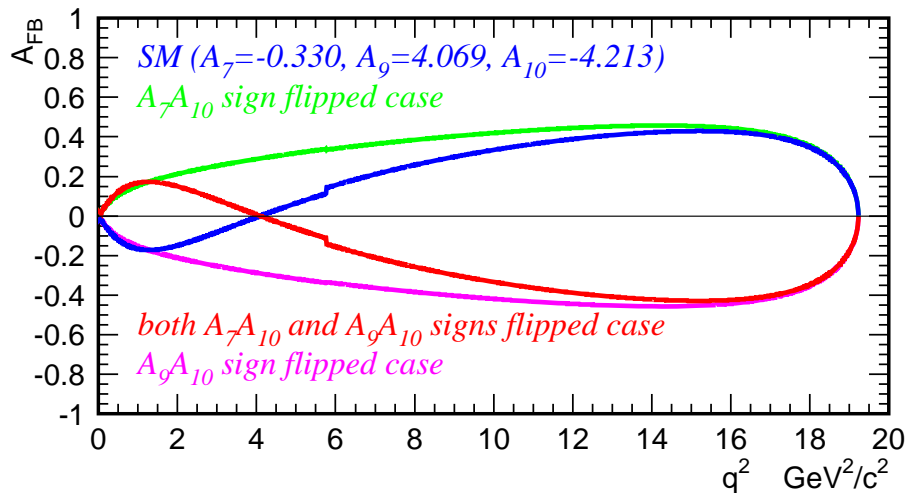


- Forward-backward asymmetry is induced by interference btw virtual photon and Z^0 contributions.
- Relative signs and magnitudes of C_7 to C_{10} and C_9 to C_{10} can be determined from $A_{FB}(B \rightarrow K^*II)$!!

$$A_{FB}(q^2) = \frac{\Gamma(q^2, \cos \theta_{Bl^-} > 0) - \Gamma(q^2, \cos \theta_{Bl^-} < 0)}{\Gamma(q^2, \cos \theta_{Bl^-} > 0) + \Gamma(q^2, \cos \theta_{Bl^-} < 0)}$$

$$\frac{d}{d\hat{s}}(\Gamma_F^{K^*} - \Gamma_B^{K^*}) = -\frac{G_F^2 \alpha^2 m_B^5}{28\pi^5} |V_{ts}^* V_{tb}|^2 \hat{s} \hat{u}(\hat{s})^2 \times \left[\text{Re}(C_9^{\text{eff}}) C_{10} V A_1 + \frac{\hat{m}_b}{\hat{s}} C_7^{\text{eff}} C_{10} (V T_2 (1 - \hat{m}_{K^*}) + A_1 T_1 (1 + \hat{m}_{K^*})) \right].$$

We do not use C_i but A_i which is leading coefficients.



Fit results for ratios of Wilson coefficients

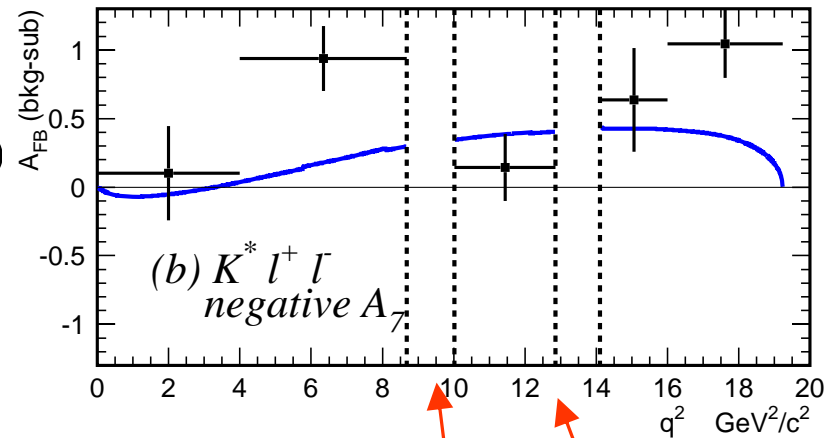


- Null test with K^+ll

$$A_{FB}^{\text{bkg-sub}}(B \rightarrow K^+ ll) = 0.09 \pm 0.14(\text{stat.})$$

- Projection to A_{FB}

$$A_{FB}^{\text{bkg-sub}}(B \rightarrow K^* ll) = 0.56 \pm 0.13(\text{stat.})$$



Best fit for negative A_7 (SM like)

$$A_9/A_7 = -15.3^{+3.4}_{-4.8} \pm 1.1,$$

$$A_{10}/A_7 = 10.3^{+5.2}_{-3.5} \pm 1.8,$$

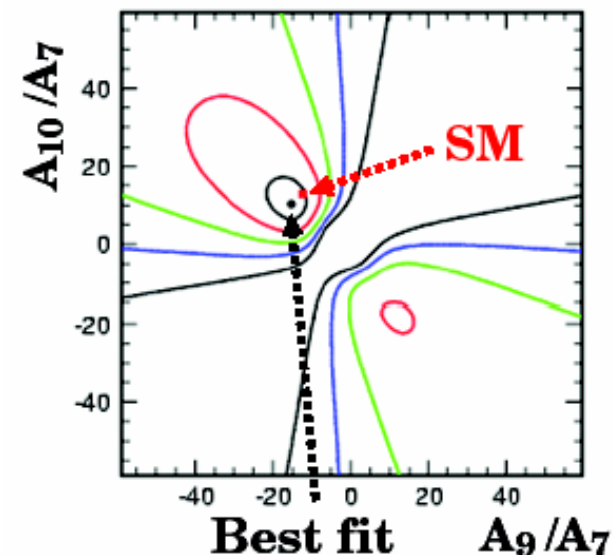
SM $A_9/A_7 = -12.3,$
 $A_{10}/A_7 = 12.8.$

Best fit for positive A_7 (non-SM like)

(This solution is also allowed)

$$A_9/A_7 = -16.3^{+3.7}_{-5.7} \pm 1.4,$$

$$A_{10}/A_7 = 11.1^{+6.0}_{-3.9} \pm 2.4,$$



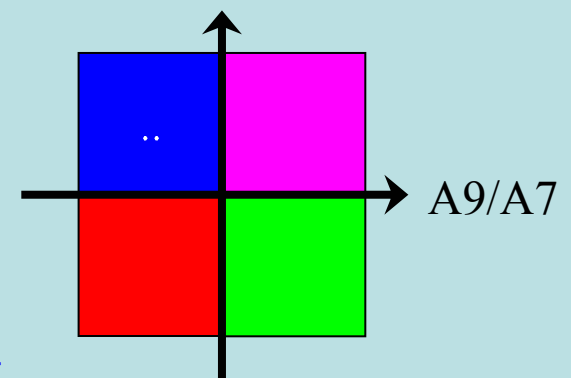
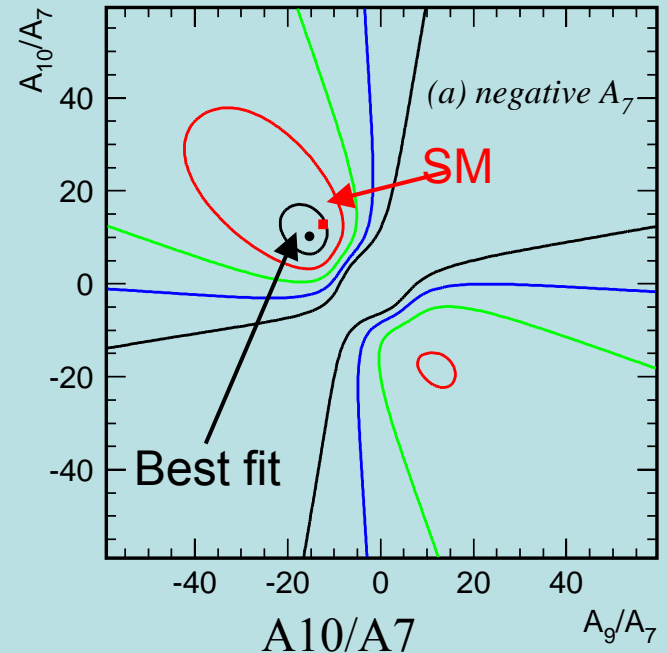
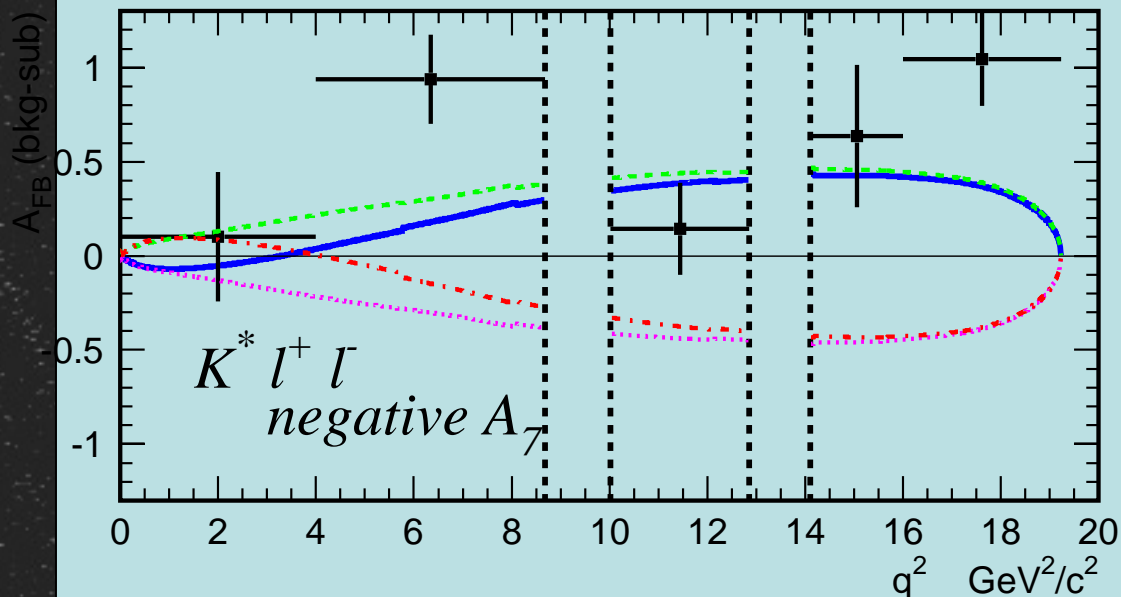
Confidence Level Contours

- For any allowed A_7 , we obtain 95% CL

$$-1401 < A_9 A_{10} / A_7^2 < -26.4.$$

$$\text{SM } A_9 A_{10} / A_7^2 = -157.$$

- Sign of $A_9 A_{10}$ is negative!!
- Sign of $A_9 A_{10}$ flipped case is excluded
 - The first and third quadrants
- Sign of $A_7 A_{10}$ is not determined yet.
 - The second and fourth quadrants



fit result

$A_7 A_{10}$ sign flipped (to SM)

Both $A_7 A_{10}$ and $A_9 A_{10}$ signs flipped

$A_9 A_{10}$ sign flipped

What is the ultimate possible UT precision?

- Theoretical limits (continuum methods)
- Many measurements will not be theory-limited for quite some time

Ligeti:

Measurement (in SM)	Theoretical limit	Present error
$B \rightarrow \psi K_S$ (β)	$\sim 0.2^\circ$	1.6°
$B \rightarrow \phi K_S, \eta^{(\prime)} K_S, \dots$ (β)	$\sim 2^\circ$	$\sim 10^\circ$
$B \rightarrow \pi\pi, \rho\rho, \rho\pi$ (α)	$\sim 1^\circ$	$\sim 15^\circ$
$B \rightarrow DK$ (γ)	$\ll 1^\circ$	$\sim 25^\circ$
$B_s \rightarrow \psi\phi$ (β_s)	$\sim 0.2^\circ$	—
$B_s \rightarrow D_s K$ ($\gamma - 2\beta_s$)	$\ll 1^\circ$	—
$ V_{cb} $	$\sim 1\%$	$\sim 3\%$
$ V_{ub} $	$\sim 5\%$	$\sim 15\%$
$B \rightarrow X\ell^+\ell^-$	$\sim 5\%$	$\sim 20\%$
$B \rightarrow K^{(*)}\nu\bar{\nu}$	$\sim 5\%$	—
$K^+ \rightarrow \pi^+\nu\bar{\nu}$	$\sim 5\%$	$\sim 70\%$
$K_L \rightarrow \pi^0\nu\bar{\nu}$	$< 1\%$	—