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```
// file: ising_opt.cpp
//
// Program to explore aspects of Monte Carlo simulation with the
// Metropolis algorithm using the one- and two-dimensional Ising model.
//
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//
// Revision history:
// 29-Apr-2004 original version (mc2d.cpp, mc2d.cooling.cpp)
//              by S.Y. Park
// 08-May-2004 added seeded GSL random number generators
//              (see random_seed.cpp) and made compatible with
//              sampling_test.cpp
// 10-May-2004 revised version with optimizations
//              by S.Y. Park
// 20-Feb-2005 minor changes to comments
// 20-Feb-2007 added comments and J_ising
//
// Notes:
// * uses the GSL random number functions and random_seed() to seed them.
// * uses the GSL random number functions and random_seed(),
//   and both the gsl_rng.h and gsl_randist.h header files are needed.
//
//*****
// include files
#include <iostream>           // cout and cin
#include <iomanip>            // manipulators like setprecision
#include <fstream>           // file input and output
#include <cmath>
using namespace std;        // we need this when .h is omitted

#include <gsl/gsl_rng.h>      // GSL random number generators
#include <gsl/gsl_randist.h>  // GSL random distributions

// function prototypes
extern unsigned long int random_seed ();           // routine to generate a seed
double calculate_energy (int configuration[],int nearest[][4]);
// calculate the energy given
// a spin configuration

// global constants
const double J_ising = 1.; // The "J" in the Ising model (+1 or -1 ONLY)
const int linear_sites = 5; // number of lattice sites in one direction

// two-dimensional Ising model only
const int num_sites = linear_sites * linear_sites;
const int dimension = 2;
// number of different energies
const int num_energies = 2 * dimension * num_sites + 1;
const int num_mcs = 10000; // # of Monte Carlo steps (mcs)

//*****
int
main (void)
{
    double kT = 2.; // temperature (in energy units)
    cout << "What temperature? (kT) ";
    cin >> kT;

    double dist_metropolis[num_energies]; // energy distribution at kT from
// importance sampling (Metropolis)
// initialize energy distribution histogram to zero
for (int i = 0; i < num_energies; i++)
{
    dist_metropolis[i] = 0.;
}
}
```

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// Set up the GSL random number generators (rng's)
gsl_rng *rng_ptr = gsl_rng_alloc (gsl_rng_taus); // allocate an rng
gsl_rng_set (rng_ptr, random_seed()); // seed the rng

// Find the energy distribution from a Markov chain of configurations
double energy0;
int config_metropolis[num_sites]; // current configuration
int nearest_neighbor[num_sites][4]; // nearest_neighbor_site

// generate a random configuration to start and find its energy
for (int i = 0; i < linear_sites ; i++)
{
    for (int j = 0; j < linear_sites ; j++)
    {
        int id=i+j*linear_sites;
        nearest_neighbor[id][0]=(i-1+linear_sites)%linear_sites+j*linear_sites;
        nearest_neighbor[id][1]=(i+1)%linear_sites+j*linear_sites;
        nearest_neighbor[id][2]=i+(j-1+linear_sites)%linear_sites*linear_sites;
        nearest_neighbor[id][3]=i+(j+1)%linear_sites*linear_sites;
    }
}
for (int i = 0; i < num_sites; i++)
{
    double random = gsl_ran_flat (rng_ptr, 0., 1.);
    if (random > 0.5)
    {
        config_metropolis[i] = -1; // spin down
    }
    else
    {
        config_metropolis[i] = +1; // spin up
    }
    energy0 = calculate_energy ( config_metropolis,nearest_neighbor );
}
// Open up an output file
ofstream out;
out.open ("ising_opt.dat");
out << "# Ising model in " << dimension << " dimensions at kT= "
    << kT << endl;
out << "# time energy " << endl;

// Take num_mcs Monte Carlo steps (mcs)
for (int step = 0; step < num_mcs; step++)
{
    for (int i = 0; i < num_sites; i++) // Entire loop is only one mcs
    {
        double delta_energy = 2*config_metropolis[i]
*(config_metropolis[nearest_neighbor[i][0]]
+config_metropolis[nearest_neighbor[i][1]]
+config_metropolis[nearest_neighbor[i][2]]
+config_metropolis[nearest_neighbor[i][3]]);

// decide whether to accept or reject the new configuration
if (delta_energy < 0.)
{
    energy0 += delta_energy; // accept the new configuration
    config_metropolis[i] *= -1;
}
else
{
    double random = gsl_ran_flat (rng_ptr, 0., 1.);
    if (random < exp(-delta_energy/kT))
    {
        energy0 += delta_energy; // accept the new configuration
        config_metropolis[i] *= -1;
    }
}
}
}
```

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    }
    // add to distribution
    dist_metropolis[dimension * num_sites + (int)energy0] += 1.;

    // print out every once in a while the current energy
    if ( (step < 100) || (step % 10 == 0) )
    {
        out << fixed << " " << setw(5) << step << " "
            << fixed << setprecision(3)
            << setw(10) << energy0 << endl;
    }
}
out.close ();
cout << "Time evolution of energy output to ising_opt.dat" << endl;

// normalize the distribution
for (int i = 0; i < num_energies; i++)
{
    dist_metropolis[i] /= (double)num_mcs;
}

//*****
// output the distributions of energies P(E)
ofstream histogram;
histogram.open ("ising_opt_histogram.dat");
histogram << "# energy metropolis " << endl;
for (int i = 0; i < num_energies; i += 2)
{
    histogram << fixed << " " << setw(5) << i - dimension*num_sites << " "
        << fixed << setprecision(8)
        << setw(11) << dist_metropolis[i] << " "
        << endl;
}
histogram << endl;
histogram.close();
cout << "Energy distribution P(E) output to ising_opt_histogram.dat"
    << endl;

return (0);
}

//***** calculate_energy *****
//
// Given the array of integers configuration[0..num_sites-1], which
// specifies the spin at each lattice point, find the energy of that
// configuration [eq.(12.6) in Session 12 notes].
// Note that a free boundary condition is specified here.
//
//*****
double
calculate_energy (int configuration[],int nearest[][4])
{
    double energy = 0.;

    // go through the 2d lattice with periodic boundary conditions
    for (int i = 0; i < linear_sites ; i++)
    {
        for (int j = 0; j < linear_sites ; j++)
        {
            int id = i + j * linear_sites;

            // x direction
            energy += - J_ising * double(configuration[id]
                * configuration[nearest[id][1]]);

            // y direction;
            energy += - J_ising * double(configuration[id]
                * configuration[nearest[id][3]]);
        }
    }
}

```

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    }
}
return (energy);
}

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