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The rotational spectra of the 6^1 , 7^1 , 8^1 , 9^1 and $5^1/9^2$ vibrational states of $H^{15}NO_3$

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ABSTRACT

The high-resolution rotational spectrum of $H^{15}NO_3$ has been recorded in the range between 74 and 850 GHz and used to complete an extensive analysis of the six vibrational states below 1000 cm^{-1} that include the isolated 8^1 and 9^1 states along with the weakly interacting 6^1 and 7^1 states and strongly interacting 5^1 and 9^2 dyad. The 6^1 and 7^1 states couple via a weak Coriolis interaction while the 5^1 and 9^1 states couple through strong Fermi and weaker Coriolis interactions. The Hamiltonian models account for the observed torsional splitting in the 9^1 and 9^2 states of 2.4 and 70 MHz, respectively, and the induced torsional splitting of 15 MHz in the 5^1 state due to the strong Fermi mixing with the 9^2 state. The transitions from each state are fit to within the experimental accuracy and the resulting spectroscopic constants agree well with the main isotopologue.

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1. Introduction

Spectroscopic characterization of nitric acid (HNO₃) continues to be a focus of laboratory studies since it is an important atmospheric trace gas and critical for understanding stratospheric ozone depletion chemistry [1]. Accurate HNO₃ concentration profiles retrieved via remote sensing, such as from NASA's MLS instruments on Aura and UARS or ESA's MIPAS instrument aboard ENVISAT, depend on the complete understanding of the spectroscopic details of HNO₃. As the sensitivity of the retrievals from these and future satellite instruments increases, the weaker spectra of transitions from vibrationally excited states and less abundant isotopologues of HNO₃ will interfere with the detection of the normal species and will need to be accurately modeled to remove systematic errors in the retrieved concentration profiles. Perrin et al. [2] recently reported the detection of H¹⁵NO₃ in the atmosphere (fractional abundance of 0.003663(4) [3]) by identifying the v_5 Q-branch near 871 cm⁻¹ in the residuals of the fitted MIPAS spectra and H¹⁵NO₃ spectral interference likely exists in other regions currently used to retrieve atmospheric nitric acid.

Several ground state rotational transitions of H¹⁵NO₃ were first measured by Millen and Morton [4] in the microwave region and

recently extended into the submillimeter wave region by Drouin et al. [5], providing a well determined set of ground state rotational and centrifugal distortional constants for H¹⁵NO₃. The low resolution infrared spectrum was measured by McGraw et al. [6] and used to determine the band origins of the fundamental vibrations. High resolution infrared studies include those for the v_2 band [7], the four lowest fundamental bands v_9 , v_7 , v_6 , and v_8 [8], and the strongly interacting v_5 and $2v_9$ bands [9]. In the latter study of the 5¹ and 9² states, Perrin et al. [9] observed an intensity ratio between the $2v_9$ and v_5 bands of $Int(2v_9)/Int(v_5) \sim 0.23$ that was satisfactory explained by the weaker $2v_9$ band borrowing intensity from the stronger v_5 band via a strong Fermi resonance. This result was based on the use of the previously determined F_0 Fermi parameter for the main isotopologue [10] and was not fit for in the H¹⁵NO₃ infrared analysis. The torsional splitting was not large enough to be resolved in the infrared spectrum for either state.

This paper reports an analysis of the H¹⁵NO₃ rotational spectrum recorded in the 74–850 GHz frequency range and includes all excited vibrational states with bands origins below 1000 cm⁻¹: $v_9 = 1$, $v_7 = 1$, $v_6 = 1$, $v_8 = 1$, $v_5 = 1$, and $v_9 = 2$. The fits include Coriolis coupling (v_6/v_7), Coriolis and Fermi Interactions ($v_5/$ $2v_9$) and torsional splitting (v_9 , v_5 , $2v_9$). The analysis method and Hamiltonians used in the present work follow closely those used for the analysis of the H¹⁴NO₃ parent isotopologue [10–13]. The most recent analyses of the ground and four lowest vibrational states of H¹⁴NO₃ were updated in Ref. [11]. Refs. [10,12] provide

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details of the Hamiltonian that describes the strong Fermi and Coriolis interactions between the 5^1 and 9^2 vibrational states as well as models for the torsional splitting. Ref. [13] provides details of the weak Coriolis interaction between the 6^1 and 7^1 vibrational state that was included to account for the systematic effect the interaction has on the quartic distortional constants. The $H^{15}NO_3$ data set and spectroscopic constants reported here are suitable for prediction of the observable millimeter and submillimeter wave spectrum as well as for simulating the infrared spectrum below 1000 cm⁻¹.

2. Experimental

The experimental data sets were collected from two different systems, the OSU FASSST and the JPL Frequency Multiplier Spectrometers. The OSU Fast Scan Submillimeter Spectroscopic Technique (FASSST) system is described in Refs. [14-16], and provided heated data over the frequency ranges from 118 to 186 GHz and 192 to 377 GHz using three different free-running, fast swept BWO tubes as sources and helium cooled hot-electron bolometers as detectors. The frequency was calibrated by use of separately recorded frequency markers from a cavity and SO₂ reference lines. An isotope enriched H¹⁵NO₃ sample was purchased from ISOTEC and filled a 6 m long, 15 cm diameter aluminum cell to a pressure of ~ 10 m Torr that was maintained in a slow flow and heated to \sim 170 °C to populate the higher lying vibrational states. A separate 60 cm cell in series with the sample cell was filled to $\sim 10 \text{ m}$ Torr with SO₂ that was used as a reference spectrum in order to calibrate the frequency. For most data sets, the normal species was only observed in small amounts (\sim 5% or less). however, for a few regions, the normal species was observed at concentrations of 50% that of the isotope concentration. In general, this did not pose any problems since the spectrum of the normal species is well characterized in Refs. [11–13] and did not significantly interfere due to the isotopic shift in frequencies, as shown in Fig. 1. The estimated accuracy of the measured transitions is 50–100 kHz.

The JPL Frequency Multiplier Submillimeter Spectrometer (FMSS) is described in Ref. [17] and provided spectra over the ranges of 74–109, 402–420, 639–656, and 800–850 GHz. Using an isotope enriched sample (98%), a gas pressure of ~10 m Torr was maintained in a slow flow in a room temperature 2 m long cell. The microwave synthesizer driving the multiplier chain was frequency modulated and the spectrum was recorded at the 2nd harmonic with a lock-in amplifier after being detected with either a room temperature diode detector near 100 GHz or a helium cooled hot-electron bolometer at the higher frequencies. Line positions were measured to 50–100 kHz precision. All of the data from both spectrometers were equally weighted in the analyses with a 100 kHz uncertainty.

3. Observed spectra and analyses

Nitric acid is a planar oblate asymmetric rotor ($\kappa = 0.729$) belonging to the C_s point group with dipole moments of $\mu_a = 1.986D$ and $\mu_b = 0.882D$ [18]. The spectrum of each vibrational state is characterized by strong R-type band heads spaced by approximately 12.5 GHz throughout the spectrum along with much more broadly spaced Q-branch transitions. Since the isotopic substitution of the nitrogen atom is close to the center of mass, the transitions in the symmetric-top limit are only slightly shifted from the normal species. The initial assignments for each vibrational state were made in order of ascending band origin energy by using the predicted spectrum of the normal species and identi-



Fig. 1. The $v_9 = 1$ R-branch band heads for the H¹⁵NO₃ and H¹⁴NO₃ isotopologues near 231 GHz. The characteristic triplet torsional splitting pattern consists of degenerate *a*-type transitions with weaker *b*-type satellites split by ~2 MHz. The *a*-type transitions are identified with the quantum numbers given for the H¹⁵NO₃ isotopologue, where $d = (J - K_a)$ and $(J - K_a + 1)$, and the *J* rotational quantum number is given in parenthesis for the H¹⁴NO₃ isotopologue transitions.

fying R-band heads that were slightly shifted in frequency and had the appropriate intensity, as shown in Fig. 1. The analysis for each corresponding vibrational state of the normal species served as the starting point for each analysis, with higher order distortional constants initially frozen until the data set was expanded. In the end, four separate analyses describe the rotational spectra of six vibrational states that all have band origins below 1000 cm⁻¹. Of these four analyses, the 8¹ and 9¹ states were fit as isolated states. Since the 6¹ and 7¹ states exhibit a weak Coriolis interaction at high *J* and K_{a} , an interaction term was included in a joint analysis of these states. The 9² and 5¹ states are coupled via strong Fermi and weaker Coriolis interactions. The Fermi interaction results in a mixing of the vibrational wavefunctions, consequently the 5^1 level also exhibits a torsional splitting in the spectra. Watson's effective A-reduced Hamiltonian in the I^r coordinate representation [19] was used in the analysis of the 8^1 , 6^1 and 7^1 states and was modified by using an internal axis system Hamiltonian with torsional parameters for the 9^1 , 5^1 and 9^2 states. All spectra were fit with

Table 1

\mathcal{O}	Sı	pectroscopic	constants	for	the	9 ¹ .	7 ¹ .	6 ¹ .	8 ¹ .	5^{1}	and s	9 ²	states	of	H^1	⁵ NO	a,
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the JPL SPFIT/SPCAT program suite [20,21]. Maximum values of the *J* and K_a quantum numbers for this isotope exceeds those for the normal species due to the recent improvements in the FASSST system that increased the sensitivity with the implementation of new signal averaging routines [15].

3.1. 8¹ state analysis

The 8¹ state is free from any significant perturbations and does not exhibit a resolvable torsional splitting; consequently it can be described with the simplest Hamiltonian and is therefore presented first. The v_8 vibrational mode corresponds to the NO₂ out of plane bend and is centered near 743.6 cm⁻¹, shifted up by less than 1 cm⁻¹ from the main isotopologue [8,22]. Table 1 summarizes the measurements that include 715 transitions that extend to maximum quantum numbers of J = 72 and $K_a = 47$. As discussed in Ref. [13], several of the quartic distortional constants for the vibrational states of nitric acid can vary

	$v_9 = 1$	$v_7 = 1$	$v_6 = 1$	$v_8 = 1$	$v_5 = 1$	$v_9 = 2$
v_o/cm^{-1}	458.29167 ^b	578.47191 ^b	646.96407 ^b	743.61660 ^b	875.0731(14)	889.4783(14)
ρ/unitless	1.468285 ^c	[0.0]	[0.0]	[0.0]	1.46810 ^c	1.46810 ^c
E _o /MHz	1.213(3)	[0.0]	[0.0]	[0.0]	[0.0]	-43.0437(115)
E _{al} /kHz	[0.0]	[0.0]	[0.0]	[0.0]	[0.0]	-1.6502(291)
$E_{\rho K}/kHz$	[0.0]	[0.0]	[0.0]	[0.0]	[0.0]	3.388(33)
E_{a^+}/kHz	0.0	[0.0]	0.0	[0.0]	0.0]	0.8180(74)
E_{aDab}/kHz	[0.0]	[0.0]	[0.0]	[0.0]	[0.0]	-0.2141(147)
E _{au} /Hz	10.01	10.01	10.01	0.01	0.01	-0.1378(126)
A/MHz	12964.232(113)	13028.00561(167)	13006.98612(163)	13000.93720(42)	12961.3070(264)	12966.5713(164)
B/MHz	12047.920(113)	12096.17370(164)	12054.47426(162)	12003.82226(39)	12137.5114(260)	11966.7862(165)
C/MHz	6254.721229(270)	6242.62085(33)	6240.211998(310)	6260.29604(42)	6233.9663(116)	6248.6970(115)
D _{ab} /MHz	-185.064(279)	[0 0]	[0.0]	[0.0]	-210220(50)	-171 419(49)
Dab/kHz	[0.0]	[0.0]	[0.0]	[0.0]	2 3790(262)	1 6896(245)
D ₋₁ w/kHz	-1.675(41)	[0.0]	[0.0]	[0.0]	-1.978(53)	-1522(88)
Λ_{l}/kHz	8 69687(80)	9 216139(229)	9 410316(201)	8 93445(43)	9 1296(56)	9 0399(43)
Δ _m /kHz	-37934(316)	-6.0589(134)	-4.4987(136)	-391647(69)	-5416(50)	-4.642(54)
Δ_{JK}/kHz	6 580(49)	8 8049(130)	6 6723(139)	6 48130(73)	6 989(91)	6 260(85)
δ./kHz	3 67298(40)	3 9/3867(103)	3 003078(118)	3 705301(117)	3 00064(281)	3.84203(215)
δ/kHz	7 1479(145)	8 0542(67)	7 6628(66)	6 888344(283)	8 2624(263)	7 2774(258)
Ф./Hz	-0.004270(38)	0.003226(39)	-0.011763(47)	0.000344(203) 0.014256(117)	[0.0]	-0.005834(174)
Ф _{//} /Нz	-0.02242(54)	-0.003220(33)	0.12392(213)	-0.06375(41)	0.01178(172)	0.00000000000000000000000000000000000
Φ _{JK} /H2	0.02242(54)	0.05250(267)	0.25286(243)	0.06007(63)	0.01023(233)	0.02037(203)
Φ _K //Hz	0.04686(149)	0.11445(113)	0.17321(53)	0.00337(03) 0.01264(71)	[0.0]	-0.0120(75)
Φ _K /Hz	0.0017775(182)	0.011443(113)	0.0054011(247)	0.01204(71)	0.000168(54)	0.0210(70)
φ ₁ /Hz	0.021/35(226)	0.0020144(210) 0.02820(114)	0.03643(120)	0.007430(33) 0.000337(181)	-0.000100(34) 0.03441(84)	0.002040(85)
φ _{JK} /Hz	-0.021433(220) 0.06032(46)	-0.02820(114) 0.05084(37)	0.00132(33)	0.02807(34)	0 15773(110)	-0.00200(30)
φ_{K}	[0.0]	3 809(134)	[0.0]	1 AQA(277)	[0.0]	[0.0]
	[0.0]	[0.0]	[0.0]	5 65(37)	[0.0]	[0.0]
L_{KKJ} $\mu \Pi Z$	[0.0]	2 576(208)	[0.0]	-0.00(07)	[0.0]	[0.0]
	[0.0]	-3.370(208)	0.412(60)	[0.0]	[0.0]	[0.0]
	[0.0]	-1.465(55)	0.413(60)	1 505(84)	[0.0]	[0.0]
	[0.0]	[0.0]	[0.0]	-1.505(64)	[0.0]	[0.0]
<i>ι_K</i> /μHZ	1.891(76)	[0.0]	[0.0]	1.990(146)	[0.0]	[0.0]
		v ₇ = ←	$\rightarrow v_6 = 1$		v ₅ = 1	$\leftrightarrow v_9 = 2$
C/MHz		[-9	030]		[(0.0]
C _{ab} /MHz		-41.94	41(181)		2.306	0(195)
C _{abJ} /kHz		0.764	2(272)			
C _{abK} /kHz					-0.10	042(43)
F _o /MHz					2563	14(35)
F _J /MHz					-7.423	36 (100)
F_K /MHz					6.487	1(174)
F _± /MHz					-3.27	43(45)
$F_{\pm K}/kHz$					0.234	96(111)
Number of transitions	1193	761	735	715	544 ^d	581 ^d
J _{max} , K _{a max} , K _{c max}	73, 59, 65	70, 50, 65	71, 50, 65	72, 47, 49	60, 41, 52	60, 40, 52
rms deviation/MHz	0.083	0.074	0.071	0.067	0.074	0.067

^a Numbers in parentheses are standard errors (1 σ), enough digits are supplied to reproduce the observed spectra.

^b The band origins are from Ref. [8].

^c Parameter cannot be fit with SPFIT and was adjusted empirically to minimize the rms deviation.

 d 79 of the transitions were between the υ_{5} = 1 and υ_{9} = 2 states.

by more than 10% when compared to the ground state constants due to correlations in the constants and the chosen reduction (A or S) and representation $(I^r, III^l, ...)$ of the Hamiltonian. For the analysis of the 8¹ state, Δ_{JK} , Δ_K and δ_K are shifted down by 17%, 14%, and 9%, respectively. However, when comparing the determinable combinations of coefficients (T_{aa} , T_{bb} , T_{cc} , T_1 and T_2 as given in Gordy and Cook [23]) the variation between the ground state and 8¹ quartic constants are all less than 6%. The T coefficients vary only slightly from the ground state and the *rms* deviation of the fitted lines is 67 kHz, which indicates that the 8¹ state does not have a significant perturbation over the set of measured transitions. These parameters are therefore a good diagnostic for determining the presence of interactions between the vibrational states of nitric acid.

3.2. 6^1 and 7^1 state analysis

The v_6 vibrational mode corresponds to the O–NO₂ stretch and is centered near 647 cm⁻¹, shifted up by less than 0.2 cm⁻¹ from the main isotopologue [8,24] and the v_7 vibrational mode corresponds to the O–NO₂ bend and is centered near 578.5 cm⁻¹, shifted down by less than 2 cm^{-1} from the main isotopic species [8,22]. Table 1 summarizes the measurements that include 761 transitions that extend to maximum quantum numbers of I = 70 and $K_a = 50$ for the 7¹ state and 735 transitions that extend to maximum quantum numbers of J = 71 and $K_a = 50$ for the 6¹ state. The difference in the band origins is 68.5 cm⁻¹, so these two states are not expected to have significant perturbations. However, several Q-branch transitions in the frequency range from 275 to 375 GHz displayed a systematic deviation for quantum numbers $J \ge 58$ (to 71) and $K_c \ge 23$ (to 31) for the 7¹ state and $K_c \ge 24$ (to 31) for 6¹ state with approximately 20 transitions with deviations between 0.5 and 1.0 MHz and six transitions with deviation between 1.0 and 10.0 MHz. These deviations have been attributed to the Coriolis interaction and the effected transitions could not be fit to experimental accuracy without the inclusion of Coriolis parameters in the Hamiltonian. Inclusion of higher order distortional terms (a complete set of octic terms) in separate analyses that did not include the Coriolis coupling could not absorb the effect of the interaction.

As discussed in Ref. [13], differences in the T_{cc} coefficients for the 6¹ and 7¹ states indicated the presence of a *C*-type Coriolis interaction for the main isotopologue. In this work, when each state was fit separately, the T_{cc} coefficients differed from the ground state by 61% for the 6¹ state and -54% for the 7¹ state. The shift of the T_{cc} distortional coefficients due to the first-order Coriolis interaction was derived by Tanaka and Morino [25] and is given by

$$\Delta T_{cc} = \pm \frac{\left(G_{67}^{c}\right)^{4}}{\left(\omega_{6} - \omega_{7}\right)^{3}},\tag{1}$$

where the coupling coefficient is given by

$$G_{67}^{c} = \zeta_{67}^{c} C_{e} \frac{\omega_{6} + \omega_{7}}{\sqrt{\omega_{6}\omega_{7}}} \sqrt{(\upsilon_{6} + 1)\upsilon_{7}}$$
(2)

and y = c in the I^r representation, ζ_{67}^c is the Coriolis coupling constant, C_e is the equilibrium rotational constant and ω_6 and ω_7 are the harmonic vibrational frequencies. Following the methodology in Ref. [13], the Coriolis coupling constant ζ_{67}^c was calculated using the difference in the T_{cc} coefficients (1.5369 kHz) from the separate, uncoupled 6¹ and 7¹ state analyses, the ground state rotational constant for C_e from Ref. [5] and the observed band origins for the ω_6 and ω_7 from Ref. [8]. Based on these parameters, the Coriolis coupling constant was calculated to be $\zeta_{67}^c = -0.720$, which allowed the coupling coefficient G_{67}^c to be calculated.

The off-diagonal vibrational Coriolis operators used in the Hamiltonian are given by

$$\langle v_{6}, v_{7} | \boldsymbol{H}_{vv'}^{c} | v_{6} + 1, v_{7} - 1 \rangle = \mathbf{i} G_{67}^{c} J_{c} + (C_{ab} + C_{ab} J^{2}) \{ J_{a}, J_{b} \} + \frac{C_{abK}}{2} \\ \times \{ J_{a}^{2}, \{ J_{a}, J_{b} \} \}.$$

$$(3)$$

The first-order Coriolis term was fixed at the value determined by the above method since it is highly correlated with rotational and distortional constants and causes the analysis to be unstable. Two higher order terms were free parameters in the analysis and were determined. With the inclusion of the Coriolis parameters in the coupled state analysis, the T_{cc} coefficients differed from the ground state by 6.6% for the 6¹ state and -0.6% for the 7¹ state and all the transitions were fit to within 300 kHz with the exception of one transition with a residual of 430 kHz. Table 2 illustrates the effects

Table 2

Rotational, centrifugal distortion constants and determinable combinations of coefficients^a for the 6¹ and 7¹ vibrational states from analyses with and without Coriolis interactions included

	Ground state ^b /MHz	Without Coriolis int	eraction	With Coriolis interaction			
		7 ¹	61	7 ¹	6 ¹		
		Change from GS/MH	łz	Percent change from GS			
A	13012.26285	16.10	-21.03	15.74	-21.02		
В	12096.924	-1.10	-41.70	-0.75	-41.70		
С	6260.137183	-57.23	77.01	-17.52	-2.41		
	Ground state ^b /kHz ^c	Percent change from	n GS	Percent change from GS			
Δ_I	8.901231	-0.5	9.8	3.5	5.7		
Δ_{IK}	-4.49804	-32.9	69.6	34.7	0.0		
Δ_K	7.33846	-16.4	28.8	20.0	-9.1		
δ_{I}	3.782612	9.0	0.9	4.3	5.6		
δ_K	7.49446	6.4	3.6	7.5	2.2		
T _{aa}	-11.74166	2.0	-1.2	1.9	-1.3		
T _{bb}	-16.46654^{d}	3.9	5.7	3.9	5.6		
T _{cc}	-1.336007	-54.3	60.5	-0.6	6.6		
T_1	-22.20565	6.1	-2.3	-2.8	6.9		
T ₂	-172.11832	3.8	-1.4	-5.1	7.9		

^a See Table 2 in Ref. [13] for relationships between the distortional constants and the determinable combinations of coefficients.

^b Ground state constants are from Ref. [5].

^c The units for T_2 are MHz².

^d In Ref. [13], -6.47697 should be -16.47697.

of the Coriolis interaction on the rotational and centrifugal distortional constants and the *T* coefficients. The value of the Coriolis coupling constant determined in this work ($\zeta_{67}^c = -0.720$) agrees well with that of the main isotopologue ($\zeta_{67}^c = -0.733$), which is expected since, in this case, the isotopic substitution should have a small effect.

3.3. 9^1 state analysis

The v_9 vibrational mode corresponds to the O–H torsion and is centered near 458 cm⁻¹, shifted up by less than 0.1 cm⁻¹ from the main isotopic species [8,26]. The 9¹ state is the lowest lying vibrational mode and the large amplitude torsional-like motion results in a torsional splitting that creates a characteristic triplet structure for transitions in the symmetric-top limit with weaker *b*-type satellites split by ~2 MHz from the degenerate *a*-type transitions, as shown in Fig. 1. Details of the torsional splitting models are presented in Refs. [10,12,27] with the analyses in this paper following those of Refs. [11–13] in the analysis of the 9¹, 5¹/9², 7¹9¹ and 6¹9¹ states of the main isotopologue of HNO₃. A Watson-like internal axis system (IAS) Hamiltonian (*A*-reduced in the I^r representation) was used to model the spectrum and is composed of rotational and torsional operators given in Eqs. (4)–(6). The IAS is rotated away from the principal axis system in the *ab* plane of the molecule, resulting in a $D_{ab}(J_aJ_b + J_bJ_a)$ contribution to the Hamiltonian with higher order distortional terms along with Fourier series expansions of individual elements of the Hamiltonian that model the torsional splittings of the energy levels. The IAS Hamiltonian is

$$H_{\nu\nu} = H^R_{\nu\nu} + H^{\rho}_{\nu\nu} \tag{4}$$

$$H^{R}_{vv} = E_{v} + A_{J}J^{2}_{a} + B_{J}J^{2}_{b} + C_{J}J^{2}_{c} + D^{v}_{ab}\{J_{a},J_{b}\} - \Delta^{v}_{J}J^{4} - \Delta^{v}_{JK}J^{2}J^{2}_{a} - \Delta^{v}_{K}J^{4}_{a} - 2\delta^{v}_{J}J^{2}J^{2}_{bc} - \delta^{v}_{K}\{J^{2}_{a},J^{2}_{bc}\} + D^{v}_{abJ}J^{2}\{J_{a},J_{b}\} + \cdots$$
(5)

Table 3 Interstate transitions between the 5^1 and 9^2 vibrational states of $\mathrm{H^{15}NO_3}$

J′	K'_a	K'_c	J″	K''_a	K_c''	v(MHz)	0 – C	J	K'_a	K'_c	J″	K''_a	K_c''	v(MHz)	0 – C
v ₅ = 1	← υ ₉ = 2							v ₉ = 2	$\leftarrow v_5 = 1$						
28	2	26	27	1	27	359811.213	0.011	24	9	15	24	13	12	141631.043	0.121
28	2	26	27	0	27	359880.197	0.041	24	10	15	24	13	12	141665.551	0.063
28	3	26	27	1	27	359827.839	-0.013	24	11	14	24	14	11	178175.186	0.005
28	3	26	27	0	27	359896.815	0.009	29	0	29	28	2	26	364112.451	0.028
31	6	25	31	4	28	333048.964	0.099	29	1	29	28	3	26	364165.205	0.082
31	6	25	31	3	28	333105.053	0.123	33	7	27	33	8	26	308339.575	-0.054
31	7	25	31	4	28	333074.973	0.032	33	7	27	33	7	26	308348.478	0.060
32	9	24	32	6	27	297198.257	-0.020	33	7	26	33	9	25	322191.547	0.002
32	9	24	32	5	27	297222.445	0.031	33	7	26	33	8	25	322207.187	0.030
33	9	24	33	6	27	312461.912	-0.016	33	8	26	33	9	25	322223.189	0.039
33	10	24	33	7	27	312442.955	0.008	33	8	26	33	8	25	322238.781	0.019
36	14	23	36	11	26	271883.440	-0.058	34	8	26	34	9	25	319766.511	0.032
36	30	6	36	23	13	141165.517	0.255	34	9	26	34	9	25	319790.865	0.030
37	14	23	37	12	26	299094.972	0.054	35	9	27	35	9	26	299009.500	0.058
37	14	23	37	11	26	299122.845	-0.002	37	11	26	37	12	25	285777.884	0.108
37	15	23	37	12	26	299114.421	0.006	37	12	26	37	13	25	285803.268	0.075
38	15	23	38	13	26	300411.110	0.034	41	17	24	41	19	23	294417.940	0.051
38	15	23	38	12	26	300439.195	-0.007	41	17	24	41	18	23	294429.703	-0.053
38	16	23	38	13	26	300432.057	-0.048	41	18	24	41	18	23	294445.087	-0.075
38	16	23	38	12	26	300460.177	-0.054	41	28	14	41	30	11	162936.594	0.124
39	16	23	39	14	26	301631.426	0.066	42	18	24	42	19	23	292933.085	-0.065
39	16	23	39	13	26	301658.938	0.032	42	19	24	42	20	23	292936.815	0.015
39	17	23	39	14	26	301653.566	0.053	43	19	24	43	21	23	291463.149	0.095
39	17	23	39	13	26	301681.031	-0.028	43	19	24	43	20	23	291477.290	-0.004
41	19	22	41	16	25	285616.193	-0.017	43	20	24	43	21	23	291481.151	-0.021
41	20	22	41	17	25	285612.554	-0.025	43	20	24	43	20	23	291495.358	-0.054
42	20	22	42	18	25	286420.663	-0.009	44	20	24	44	22	23	290079.821	0.007
42	20	22	42	17	25	286443.253	-0.119	44	20	24	44	21	23	290094.952	-0.051
42	21	22	42	18	25	286440.485	-0.072	52	31	21	52	32	20	249223.836	0.023
42	31	11	42	27	16	172912.936	-0.030	52	32	21	52	33	20	249225.761	0.031
43	21	22	43	19	25	287165.921	-0.035								
43	21	22	43	18	25	287188.259	-0.028								
43	22	22	43	19	25	287186.167	-0.065								
43	22	22	43	18	25	287208.542	-0.020								
44	22	22	44	20	25	287794.147	-0.005								
44	23	22	44	19	25	287836.684	0.034								
45	24	21	45	21	24	271440.169	0.062								
45	25	21	45	22	24	271438.567	0.012								
45	25	21	45	21	24	271459.349	0.059								
46	25	21	46	22	24	271861.238	0.092								
46	26	21	46	23	24	271859.882	0.029								
47	26	21	47	24	24	272178.271	0.005								
47	26	21	47	23	24	272199.858	0.132								
48	27	21	48	24	24	272439.552	0.238								
48	28	21	48	25	24	272438.179	-0.093								
52	33	19	52	31	22	239364.647	-0.050								
53	34	19	53	32	22	238957.774	0.050								
53	34	19	53	31	22	238983.223	-0.009								
53	35	19	53	32	22	238982.305	-0.099								

The ratio of the moment of inertia of the top to that of the frame, ρ , cannot be fit for in SPFIT and was empirically adjusted to minimize the *rms* deviation of the fit. We used the convention that the NO₂ group was the top and OH the frame that allowed for a more convenient labeling of the states in SPFIT. Table 1 summarizes the measurements that include 1193 transitions that extend to maximum quantum numbers of J = 73 and $K_a = 59$. The rms deviation of fit was 87 kHz and a comparison of the fitted constants with the other vibrational states was not attempted due to the use of the IAS Hamiltonian. When comparing the torsional parameters between the two isotopologues, the structural parameter ρ was unchanged and there was only a slight change in the torsional splitting parameter E_{ρ} which changed from 1.170(4) MHz for H¹⁴NO₃ to 1.213(3) MHz for H¹⁵NO₃. For the D¹⁴NO₃ isotope, the torsional splitting for the 9¹ state is not resolvable [28].

3.4. 5^1 and 9^2 state analysis

The v_5 vibrational mode corresponds to the NO₂ in plane bend and is centered near 871 cm⁻¹, shifted down by ~8 cm⁻¹ from the main isotopic species, while the $2v_9$ is associated with the O– H torsional mode and is centered near 893 cm⁻¹, shifted down by ~3 cm⁻¹ from the main isotopic species [9,10]. The difference in the band origins is ~22 cm⁻¹ (compared to ~17 cm⁻¹ for the normal species) and these two states are coupled via a strong Fermi resonance that must be fit for simultaneously since this strong resonance causes the 5¹ and 9² wavefunctions to be mixed. In the infrared, this mixing results in an intensity borrowing where the expected weak $2v_9$ overtone band and expected strong v_5 fundamental band have an unexpectedly large intensity ratio of $Int(2v_9)/Int(v_5) \sim 0.23$ [9]. For pure rotational transitions, the mixing results in an induced torsional splitting observed for the 5¹ levels that would normally be expected only for the 9^2 levels. The observed torsional splitting is ~70 MHz for the 9^2 state rotational transitions and ~15 MHz for the 5^1 state transitions. Assuming the splitting in the 5^1 transitions is due to the wavefunction mixing, then the percent mixing is ~82% to ~18%, which then predicts the intensity ratio of 0.214 for the infrared bands, which is in close agreement with the observed ratio.

Due to the torsional splitting, the IAS Hamiltonian was used to fit the $5^{1}/9^{2}$ states and follows the "induced splitting" model from Ref. [12] where the zero-order Fermi resonance term, F_{0} , was fit for and only the 9^{2} state was given a set of torsional parameters. The torsional splitting in the 5^{1} state is then completely accounted for through the mixing of the wavefunctions due to the Fermi resonance rather than fitting for a separate set of torsional parameters. The Fermi operators coupling the vibrational states are given by

$$H_{vv'}^{F} = F_{0} + F_{J}J^{2} + F_{K}J_{a}^{2} + 2F_{\pm}J_{bc}^{2} + 2F_{\pm K}\{J_{a}^{2}, J_{bc}^{2}\}$$
(7)

and the resulting mixing of the vibrational wavefunctions can be expressed as

$$a^{2} = \frac{1}{2} \left(1 + \sqrt{1 - \frac{4F_{o}^{2}}{\Delta E^{2}}} \right)$$
(8)

where the coefficient a^2 represents the fractional mixing and ΔE is the difference in the observed (perturbed) band origins. The Coriolis interaction operators are given by Eq. (3).

Table 1 summarizes the measurements that include 544 transitions that extend to maximum quantum numbers of J = 60 and $K_a = 41$ for the 5¹ state and 581 transitions that extend to maximum quantum numbers of J = 60 and $K_a = 40$ for the 9² state with transitions measured up to a maximum frequency of 655 GHz. Due to localized anharmonic $\Delta K_a = \pm 2$ resonances, 79 transitions were labeled as interstate rovibrational transitions and are listed in



Fig. 2. A contour plot of the vibrational wavefunction mixing coefficients as a function of quantum number for the $v_5 = 1$ state. Note the base mixing coefficient of ~82% due to the F_0 term coupling the states. The variation in the contours arise due to local resonances and the levels involved in the interstate rovibrational transitions are labeled with the "*" symbol.

Table 3. Fig. 2 provides a contour map of the wavefunction mixing for the 5^1 levels along with the 5^1 state energy levels involved in the interstate rovibrational transitions.

The observed torsional splitting in each state is directly related to the mixing and the rotational transitions allow both the zero-order Fermi term, F_o , and the difference in the band origins, ΔE , to be determined. However, since F_0 is highly correlated with the vibrational energies E_5 and E_{99} and pure rotational transitions do not depend directly on these energies, we included the band origins reported by Perrin and Mbiaké [9] in the analysis as 'measured rotationless transitions' with values of 871.0955(3) and 893.4518(3) cm⁻¹ for the v_5 and 2v₉ bands, respectively, where the uncertainly in parenthesis reflects the estimated systematic uncertainty. This allowed both band origins and the zero-order Fermi term to be fit for simultaneously. Excluding one of these bands centers from the analyses does not significantly change the fitted parameters since the rotational transitions provided sufficient information to determine both the F_{0} and $\Delta E = E_{99} - E_5$, even though these remain highly correlated (correlation coefficient of -0.999996). As demonstrated in Ref. [10] for H¹⁴NO₃, the statistical uncertainty in these correlated parameters can be reduced if all the measured infrared energy levels are included in the analysis. When comparing the F_0 parameter for $H^{15}NO_3$ to that determined for $H^{14}NO_3$ in Refs. [10,12], this parameter is only slightly higher (\sim 0.2%) and is not significantly different. If the band origins are fixed at the values reported in Ref. [9], the uncertainty in the F_o terms is reduced by a factor of 300 to a value of 255738.055(96) MHz without significant changes in the other constants or the analysis. However, this value is still highly dependent on the band origins.

The torsional splitting parameter, E_{ρ} , determined for the 9² states for each isotopologue are nearly identical with values of 43.04(1) MHz for H¹⁵NO₃ and 43.15(1) MHz for H¹⁴NO₃ reported in a similar analysis in Ref. [12]. While the infrared analysis for the 5¹/9² dyad of H¹⁵NO₃ in Ref. [9] did not require the non-orthorombic terms, such as $D_{ab}^{\nu} \{J_a, J_b\}$, they were required in this analysis to describe the interaction between the torsional sublevels (Wang submatrices, $E^{\pm} \leftrightarrow O^{\pm}$), which is significant when the torsional splitting is approximately equal to the asymmetry splitting.

4. Summary

The rotational spectrum of $H^{15}NO_3$ has been recorded in the range between 74 and 850 GHz. The spectrum of the six lowest lying vibrational states (9¹, 7¹, 6¹, 8¹, 5¹, and 9²) have been analyzed and fit to produce a set of spectroscopic parameters that accurately predict the thermally populated millimeter and submillimeter wave spectrum over this range of frequencies. Fermi and Coriolis interactions between various states have been accounted for as well as the torsional splitting of the 9¹, 9² and 5¹ states.

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Appendix A. Supplementary data

Supplementary data for this article are available on ScienceDirect (www.sciencedirect.com) and as part of the Ohio State University Molecular Spectroscopy Archives (http://library.osu.edu/sites/ msa/jmsa_hp.htm). Supplementary data associated with this article can be found, in the online version, at doi:10.1016/j.jms. 2008.03.025.

References

- M.L. Santee, W.G. Read, J.W. Waters, L. Froidevaux, G.L. Manney, D.A. Flower, R.F. Jarnot, R.S. Harwood, G.E. Peckham, Science 267 (1995) 849–852.
- [2] A. Perrin, J.-M. Flaud, R. Mbiake, G.G. Brizzi, M. Carlotti, M. Ridolfi, in: 61st International Symposium on Molecular Spectroscopy, Ohio State University, Columbus, OH, USA, 2006.
- [3] T.B. Coplen, J.K. Bohlke, P. De Bievre, T. Ding, N.E. Holden, J.A. Hopple, H.R. Krouse, A. Lamberty, H.S. Peiser, K. Revesz, S.E. Rieder, K.J.R. Rosman, E. Roth, P.D.P. Taylor, R.D. Vocke, Y.K. Xiao, Pure Appl. Chem. 74 (2002) 1987–2017.
- [4] D.J. Millen, J.R. Morton, J. Chem. Soc. (1960) 1523-1528.
- [5] B.J. Drouin, C.E. Miller, J.L. Fry, D.T. Petkie, P. Helminger, I.R. Medvedev, J. Mol. Spectrosc. 236 (2006) 29–34.
- [6] G.E. McGraw, D.L. Bernitt, I.C. Hisatsune, J. Chem. Phys. 42 (1965) 237-244.
- [7] W.F. Wang, P.P. Ong, H.F. Chen, H.H. Teo, J. Mol. Spectrosc. 185 (1997) 207– 208.
- [8] F. Keller, A. Perrin, J.-M. Flaud, J.W.C. Johns, Z. Lu, E.C. Looi, J. Mol. Spectrosc. 191 (1998) 306–310.
- [9] A. Perrin, R. Mbiake, J. Mol. Spectrosc. 237 (2006) 27-35.
- [10] A. Perrin, J. Orphal, J.-M. Flaud, S. Klee, G. Mellau, H. Mader, D. Walbrodt, M. Winnewisser, J. Mol. Spectrosc. 228 (2004) 375–391.
- [11] D.T. Petkie, P. Helminger, R.A.H. Butler, S. Albert, F.C. De Lucia, J. Mol. Spectrosc. 218 (2003) 127–130.
- [12] D.T. Petkie, T.M. Goyette, P. Helminger, H.M. Pickett, F.C. De Lucia, J. Mol. Spectrosc. 208 (2001) 121–135.
- [13] D.T. Petkie, P. Helminger, M. Behnke, I.R. Medvedev, F.C. De Lucia, J. Mol. Spectrosc. 233 (2005) 189–196.
- [14] S. Albert, D.T. Petkie, R.P.A. Bettens, S.P. Belov, F.C. De Lucia, Anal. Chem. 70 (1998) 719A-727A.
- [15] I. Medvedev, M. Winnewisser, F.C. De Lucia, E. Herbst, E. Białkowska-Jaworska, L. Pszczołkowski, Z. Kisiel, J. Mol. Spectrosc. 228 (2004) 314–328.
- [16] D.T. Petkie, T.M. Goyette, R.P.A. Bettens, S.P. Belov, S. Albert, P. Helminger, F.C. De Lucia, Rev. Sci. Instrum. 68 (1997) 1675–1683.
- [17] B.J. Drouin, F.W. Maiwald, J.C. Pearson, Rev. Sci. Instrum. 76 (2005). Art. No.093113.
- [18] A.P. Cox, J.M. Riveros, J. Chem. Phys. 42 (1965) 3106-3112.
- [19] J.K.G. Watson, in: J.R. Durig (Ed.), Vibrational Spectra and Structure, vol. 6, Elsevier, New York, 1977, pp. 1–89.
- [20] H.M. Pickett, J. Mol. Spectrosc. 148 (1991) 371-377.
- [21] H.M. Pickett, R.L. Poynter, E.A. Cohen, M.L. Delitsky, J.C. Pearson, H.S.P. Muller, J. Quant. Spectrosc. Rad. Transfer 60 (1998) 883-890.
- [22] E.C. Looi, T.L. Tan, W.F. Wang, P.P. Ong, J. Mol. Spectrosc. 176 (1996) 222-225.
- [23] W. Gordy, R.L. Cook, Microwave Molecular Spectra, third ed., John Wiley & Sons, New York, 1984.
- [24] T.L. Tan, W.F. Wang, E.C. Looi, P.P. Ong, Spectrochim. Acta 52A (1996) 1315– 1317.
- [25] T. Tanaka, Y. Morino, J. Mol. Spectrosc. 5 (1969) 436-448.
- [26] A. Goldman, J.B. Burkholder, C.J. Howard, R. Escribano, A.G. Maki, J. Mol. Spectrosc. 131 (1988) 195–200.
 - [27] L.H. Coudert, A. Perrin, J. Mol. Spectrosc. 172 (1995) 352-368.
 - [28] S.G. Chou, D.T. Petkie, R.A.H. Butler, C.E. Miller, J. Mol. Spectrosc. 211 (2002) 284-285.