

## THE ROTATIONAL SPECTRUM OF NITRIC ACID: THE FIRST FIVE VIBRATIONAL STATES

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**Abstract**—With the work reported here, we have completed a series of rotational analyses of the  $v_9$ ,  $v_7$ ,  $v_6$ , and  $v_8$  vibrational states of the important atmospheric species nitric acid. In this paper, we report the details of our work on the  $v_8$  vibrational state, which arise from the NO<sub>2</sub> out of plane vibration. For this state, over 210 transitions have been measured in the millimeter and submillimeter spectral region and analyzed with Watson's A reduced centrifugal distortion Hamiltonian. In the course of our work on the excited vibrational states, a number of additional lines of the ground state have been observed and a more complete analysis of the ground state is provided. Also included in this work is a comparison of all these spectra and an overview of the millimeter and submillimeter spectra associated with these states. Although at the high sensitivity available in laboratory experiments, many additional lines are observable, all arise from vibrational states whose populations are more than 100 times lower than the ground state. The most prominent of these are due to the states which give rise to the perturbed  $2v_9$  and  $v_5$  bands near 11  $\mu\text{m}$ . These results provide a significant data base for both atmospheric remote sensing experiments and spectral analyses of data in other spectral regions, especially the infrared (i.r.).

### INTRODUCTION

Nitric acid (HNO<sub>3</sub>) is both a common chemical species and an important minor constituent of the terrestrial atmosphere. As a result it has received considerable spectroscopic attention,<sup>1-18</sup> both in the microwave and i.r. spectral regions. As we have shown previously, with the spectral range available to our millimeter and submillimeter (mm/submm) techniques, it is possible to acquire enough data so that all unperturbed thermally populated rotational levels can be calculated with good accuracy from measurements of the pure rotational spectrum.

We have previously analyzed the rotational spectrum of its ground vibrational state,<sup>3,4,6</sup>  $v_9$  at 456  $\text{cm}^{-1}$ ,<sup>14</sup>  $v_7$  at 579  $\text{cm}^{-1}$ ,<sup>15</sup> and  $v_6$  at 647  $\text{cm}^{-1}$ .<sup>16</sup> In this paper we report the measurement and assignment of 215 transitions in the  $v_8$  excited vibrational state at 762  $\text{cm}^{-1}$ . Also reported in this paper are 193 newly measured lines, most of which are highly excited, of the ground vibrational state that were measured during the course of this work and an analysis of these data. Finally, we show a comparison among the spectral constants of these states and discuss the general nature of the spectra and their relation to atmospheric remote sensing experiments.

### EXPERIMENTAL STUDIES

The experimental techniques, which we have developed for high-resolution spectroscopy in the mm/submm, have been discussed in detail elsewhere.<sup>15,19-21</sup> In this work, we have used both a broad band mm/submm spectrometer based on YIG oscillator and TWT technology,<sup>15</sup> which was especially useful in the assignment of these spectra, as well as a klystron-driven system with a <sup>3</sup>He detector which was used for many of the higher frequency transitions.<sup>19-21</sup>

HNO<sub>3</sub> gas was obtained from a mixture of fuming nitric and sulfuric acids. The sulfuric acid, which has very low vapor pressure, was included in the mixture to bind water and thereby increase

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the purity of the  $\text{HNO}_3$  gas. The measurements were carried out in a variety of room-temperature cells, the length of which was typically 1m. Although  $\text{HNO}_3$  is a reactive gas, no extraordinary precautions were required. In a stainless steel and glass system, the sample was stable for long periods. In systems containing copper and brass, it was necessary to renew the sample periodically. Although a very wide range of states was observed, it is clear that the spectroscopy could be extended to much higher energy by the use of longer and/or heated cells.

## THEORY

We have used Watson's reduced centrifugal distortion Hamiltonian in its A form for all of our analyses of the vibrational states of nitric acid.<sup>22</sup> Through terms of the 8th order in the angular momentum, the Hamiltonian is

$$\mathcal{H} = \mathcal{H}_r + \mathcal{H}_d^{(4)} + \mathcal{H}_d^{(6)} + \mathcal{H}_d^{(8)}, \quad (1)$$

$$\mathcal{H}_r = 1/2 (B_y + B_z)P^2 + [B_x - 1/2(B_y + B_z)](P_z^2 - b_p P_{-}^2), \quad (2)$$

$$\mathcal{H}_d^{(4)} = -\Delta_J P^4 - \Delta_{JK} P^2 P_z^2 - \Delta_K P_z^4 - 2\delta_J P^2 P_{-}^2 - \delta_K (P_z^2 P_{-}^2 + P_{-}^2 P_z^2), \quad (3)$$

$$\begin{aligned} \mathcal{H}_d^{(6)} = & H_J P^6 + H_{JK} P^4 P_z^2 + H_{KJ} P^2 P_z^4 + H_K P_z^6 + 2h_J P^4 P_{-}^2 \\ & + h_{JK} P^2 (P_z^2 P_{-}^2 + P_{-}^2 P_z^2) + h_K (P_z^4 P_{-}^2 + P_{-}^2 P_z^4), \end{aligned} \quad (4)$$

Table 1. Assignments of observed transitions for  $v_8$  (MHz).

$J'K' - K' + J''K'' - K'' +$	Observation	Observed - Calculated	$J'K' - K' + J''K'' - K'' +$	Observation	Observed - Calculated
9 1 8 - 8 1 7	131352.490	0.008	17 5 12 - 16 5 11	281242.382	0.015
9 4 6 - 8 4 5	156271.044	0.001	17 6 11 - 16 6 10	293704.638	0.112
10 0 10 - 9 0 9	131430.908	-0.089	17 9 8 - 16 9 7	331502.247	0.072
10 1 9 - 9 1 8	143871.240	-0.093	17 10 8 - 16 10 7	331449.968	-0.152
10 2 8 - 9 2 7	156315.927	0.009	17 11 7 - 16 11 6	344197.593	0.159
11 2 9 - 10 2 8	168832.051	0.008	18 2 16 - 17 2 15	256440.270	-0.035
11 4 7 - 10 4 6	193767.578	-0.024	18 3 15 - 17 3 14	268872.314	0.096
11 5 7 - 10 5 6	193764.941	-0.053	18 3 16 - 17 3 15	256440.255	-0.050
12 0 12 - 11 0 11	156469.736	-0.044	18 4 14 - 17 4 13	281306.591	0.110
12 1 11 - 11 1 10	168908.302	0.000	18 5 13 - 17 5 12	293746.826	-0.006
12 2 10 - 11 2 9	181348.486	0.070	18 7 11 - 17 7 10	318676.966	-0.045
12 6 7 - 11 6 6	218773.640	0.065	18 9 9 - 17 9 8	343822.705	0.076
13 0 13 - 12 0 12	168988.574	-0.009	18 10 9 - 17 10 8	343816.210	0.180
13 2 11 - 12 2 10	193864.697	-0.020	18 17 1 - 17 16 2	459868.244	-0.034
13 4 9 - 12 4 8	218764.086	-0.069	18 17 2 - 17 16 1	459813.127	-0.009
13 5 8 - 12 5 7	231252.685	0.064	19 1 18 - 18 1 17	256523.095	-0.078
13 9 4 - 12 9 3	287812.150	0.160	19 2 17 - 18 2 16	268953.759	0.044
13 10 3 - 12 10 2	290177.462	-0.007	19 3 16 - 18 3 15	281383.837	-0.065
14 0 14 - 13 0 13	181506.884	-0.064	19 4 15 - 18 4 14	293815.576	-0.035
14 1 13 - 13 1 12	193943.701	-0.046	19 6 13 - 18 6 12	318697.568	-0.023
14 2 12 - 13 2 11	206380.850	0.092	19 10 9 - 18 10 8	368917.197	0.013
14 3 11 - 13 3 10	218820.996	-0.010	19 11 8 - 18 11 7	382005.469	0.017
14 4 10 - 13 4 9	231270.458	0.037	19 11 9 - 18 11 8	368900.579	0.002
14 6 8 - 13 6 7	256262.987	-0.135	19 12 8 - 18 12 7	381748.014	0.078
14 7 8 - 13 7 7	256260.155	-0.250	20 0 20 - 19 0 19	256606.005	-0.095
14 9 6 - 13 9 5	281411.519	0.008	20 1 19 - 19 1 18	269037.255	0.073
15 0 15 - 14 0 14	194024.853	0.011	20 1 20 - 19 1 19	256606.176	0.076
15 1 14 - 14 1 13	206460.742	-0.021	20 2 18 - 19 2 17	281466.357	-0.081
15 3 12 - 14 3 11	231334.243	0.033	20 5 15 - 19 5 14	318757.007	0.032
15 4 11 - 14 4 10	243778.564	-0.021	20 6 14 - 19 6 13	331196.837	-0.062
15 5 10 - 14 5 9	256238.085	-0.081	20 11 9 - 19 11 8	394060.819	-0.110
15 8 7 - 14 8 6	294119.995	0.089	21 1 20 - 20 1 19	281550.390	-0.094
15 10 6 - 14 10 5	306372.247	0.066	21 2 19 - 20 2 18	293978.368	-0.065
16 0 16 - 15 0 15	206542.216	-0.017	21 4 17 - 20 4 16	318832.433	0.004
16 1 15 - 15 1 14	218977.197	-0.054	21 5 16 - 20 5 15	331261.971	0.050
16 2 14 - 15 2 13	231411.620	0.017	21 8 13 - 20 8 12	368607.180	-0.097
16 4 12 - 15 4 11	256287.744	0.079	21 9 12 - 20 9 11	381105.625	0.085
16 5 11 - 15 5 10	268739.111	-0.007	21 14 7 - 20 14 6	450507.963	0.013
16 6 10 - 15 6 9	281213.808	0.018	21 15 7 - 20 15 6	443872.344	-0.028
16 8 8 - 15 8 7	306375.647	0.010	21 16 5 - 20 16 4	470529.270	0.071
16 14 2 - 15 12 3	447382.455	-0.087	21 16 6 - 20 16 5	450926.531	-0.005
17 0 17 - 16 0 16	219059.033	-0.053	21 17 4 - 20 17 3	457842.046	-0.055
17 1 16 - 16 1 15	231493.208	0.035	21 17 5 - 20 17 4	451191.356	-0.041
17 2 15 - 16 2 14	243926.308	0.057	21 18 3 - 20 18 2	448296.276	0.005
17 3 14 - 16 3 13	256359.912	-0.060	21 18 4 - 20 18 3	447387.561	0.006
17 4 13 - 16 4 12	268797.119	0.035	21 19 2 - 20 19 1	443214.733	0.028

Table 1—continued

$J'K^- K^+ J''K'' - K''^+$	Observation	Observed - Calculated	$J'K^- K^+ J''K'' - K''^+$	Observation	Observed - Calculated
22 0 22 - 21 0 21	281634.033	-0.130	29 3 27 - 29 1 28	341775.937	0.131
22 1 21 - 21 1 20	294062.988	-0.058	29 6 23 - 28 6 22	443685.863	0.004
22 4 18 - 21 4 17	331339.857	-0.033	29 7 22 - 28 7 21	456095.265	-0.016
22 5 17 - 21 5 16	343766.438	-0.032	29 8 21 - 28 8 20	468507.232	0.009
22 10 12 - 21 10 11	406092.441	0.053	29 11 18 - 28 11 17	505787.970	-0.052
22 13 9 - 21 13 8	444570.778	0.067	30 0 30 - 29 0 29	381714.568	0.028
22 14 8 - 21 14 7	459130.123	0.088	30 4 27 - 30 2 28	341645.801	-0.036
22 14 9 - 21 14 8	444385.264	-0.033	30 5 25 - 29 5 24	443774.777	0.003
22 15 7 - 21 15 6	477988.882	0.123	30 8 22 - 29 8 21	480994.901	0.035
22 15 8 - 21 15 7	457292.928	0.026	30 7 23 - 29 7 22	468586.829	-0.082
22 16 7 - 21 16 6	468253.552	0.036	30 9 21 - 29 9 20	493406.689	-0.017
22 17 6 - 21 17 5	473581.978	-0.032	31 1 30 - 30 1 29	406637.337	0.010
22 18 4 - 21 18 3	476895.452	0.004	31 4 27 - 30 4 26	443866.628	-0.013
22 18 5 - 21 18 4	472340.032	0.001	31 5 27 - 31 3 28	341507.832	0.022
22 20 2 - 21 20 1	463852.096	-0.027	31 5 26 - 30 5 25	456271.133	-0.092
22 20 3 - 21 20 2	463817.479	-0.035	31 6 25 - 30 6 24	468674.518	0.027
23 0 23 - 22 0 22	294147.021	-0.091	31 7 24 - 30 7 23	481077.522	0.012
23 2 21 - 22 2 20	319000.142	0.058	31 8 23 - 30 8 22	493481.618	-0.048
23 3 20 - 22 3 19	331423.541	-0.109	31 9 22 - 30 9 21	505888.767	-0.025
23 4 19 - 22 4 18	343846.711	0.107	32 0 32 - 31 0 31	406725.337	-0.031
23 6 17 - 22 6 16	368697.386	-0.046	32 3 29 - 31 3 28	443959.600	-0.020
23 9 14 - 22 9 13	406040.328	-0.003	32 4 28 - 31 4 27	456364.167	-0.091
23 13 10 - 22 13 9	456600.703	-0.085	32 5 27 - 31 5 26	468766.428	-0.054
23 14 9 - 22 14 8	469997.771	-0.028	32 6 26 - 31 6 25	481167.084	0.012
23 14 10 - 22 14 9	456571.990	-0.113	32 6 27 - 32 4 28	341361.184	-0.159
23 15 9 - 22 15 8	469623.976	0.023	33 2 31 - 32 2 30	444052.458	0.049
23 16 8 - 22 16 7	482371.676	0.126	33 3 30 - 32 3 29	456458.145	-0.012
23 19 5 - 22 19 4	493256.693	0.029	33 6 27 - 32 6 26	493658.453	0.030
23 20 3 - 22 20 2	488972.598	-0.009	33 7 27 - 33 5 28	341206.033	-0.003
23 20 4 - 22 20 3	488662.546	-0.055	34 1 33 - 33 1 32	444143.990	-0.019
23 21 2 - 22 21 1	484497.938	-0.045	34 2 32 - 33 2 31	456551.656	-0.047
23 21 3 - 22 21 2	484479.657	0.126	34 3 31 - 33 3 30	468955.428	-0.044
24 1 23 - 23 1 22	319085.800	-0.016	34 5 30 - 34 3 31	378715.161	-0.114
24 2 22 - 23 2 21	331509.618	-0.050	35 0 35 - 34 0 34	444233.557	-0.046
24 3 21 - 23 3 20	343931.578	0.002	35 1 34 - 34 1 33	456644.007	0.064
24 5 19 - 23 5 18	368773.876	0.099	35 2 33 - 34 2 32	469049.801	0.018
24 6 18 - 23 6 17	381197.301	0.025	35 4 31 - 34 4 30	493849.601	-0.052
24 11 13 - 23 11 12	443516.076	-0.008	35 6 30 - 35 4 31	378553.650	-0.019
24 14 11 - 23 14 10	468826.338	-0.050	35 9 27 - 35 7 28	340867.147	-0.088
25 0 25 - 24 0 24	319170.731	0.045	36 1 35 - 35 1 34	469142.689	0.014
25 1 24 - 24 1 23	331595.970	0.012	36 2 34 - 35 2 33	481546.584	-0.032
25 2 23 - 24 2 22	344018.400	0.024	36 3 33 - 35 3 32	493946.320	0.017
25 4 21 - 24 4 20	368857.505	-0.025	36 7 30 - 36 5 31	378383.668	-0.046
25 10 15 - 24 10 14	443459.055	0.025	36 10 27 - 36 8 28	340682.793	-0.069
25 12 13 - 24 12 12	468505.238	-0.041	37 0 37 - 36 0 36	469233.402	0.027
26 1 25 - 25 1 24	344105.191	-0.036	37 1 36 - 36 1 35	481640.115	-0.057
26 6 20 - 25 6 19	406195.161	-0.038	37 2 35 - 36 2 34	494042.107	-0.062
26 10 16 - 25 10 15	455928.005	0.067	37 11 27 - 37 9 28	340487.888	-0.005
26 11 15 - 25 11 14	468405.077	0.014	38 0 38 - 37 0 37	481731.519	0.071
27 0 27 - 26 0 26	344190.937	-0.005	38 1 37 - 37 1 36	494136.404	0.002
27 2 25 - 26 2 24	369033.100	0.073	38 9 30 - 38 7 31	378017.405	-0.010
27 8 19 - 26 8 18	443530.217	0.166	39 1 38 - 38 1 37	506631.408	0.077
27 10 17 - 26 10 16	468400.014	-0.003	39 10 30 - 39 8 31	377820.404	0.039
27 11 16 - 26 11 15	480861.882	0.068	40 0 40 - 39 0 39	506723.766	-0.039
28 1 27 - 27 1 26	369121.139	0.125	40 1 39 - 39 1 38	519125.009	0.082
28 2 26 - 27 2 25	381538.927	0.026	41 0 41 - 40 0 40	519217.987	-0.036
28 2 27 - 28 0 28	341898.064	-0.019	42 7 36 - 42 5 37	452665.134	0.111
28 4 24 - 27 4 23	406366.809	-0.052	44 8 37 - 44 6 38	464814.343	0.034
28 7 21 - 27 7 20	443602.718	0.003	44 9 36 - 44 7 37	452228.372	0.059
28 8 20 - 27 8 19	456018.958	0.069	45 10 36 - 45 8 37	451997.265	-0.018
28 10 18 - 27 10 17	480874.145	0.026	46 10 37 - 46 8 38	464347.390	-0.042
29 0 29 - 28 0 28	369207.693	0.071			

$$\begin{aligned} \mathcal{H}_d^{(8)} = & L_J P^8 + L_{JK} P^6 P_z^2 + L_{JK} P^4 P_z^4 + L_{KK} P^2 P_z^6 + L_K P_z^8 + 2l_J P^6 P_z^2 \\ & + l_{JK} P^4 (P_z^2 P_{-z}^2 + P_{-z}^2 P_z^2) + l_{KJ} P^2 (P_z^4 P_{-z}^2 P_z^4) + l_K (P_z^6 P_{-z}^2 + P_{-z}^2 P_z^6), \end{aligned} \quad (5)$$

where  $\Delta_j$  etc. are the quartic distortion coefficients;  $H_j$  etc. are the sextic distortion coefficients;  $L_j$  etc. are the 8th order distortion coefficients;  $b_p = (B_z - B_y)/(2B_x - B_y - B_z)$  is Wang's asymmetry parameter,  $P^2 = P_x^2 + P_y^2 + P_z^2$ . Here, we have used the definition

$$P_{-z}^2 = P_x^2 - P_y^2. \quad (6)$$

We have previously discussed our implementation of this theory.<sup>23-25</sup> All states have been analyzed using III<sup>1</sup> representation, which identifies the pseudo-oblate top c-axis with the z-axis.

Table 2. Results of analyses (MHz).

Constant	Ground State	$v_9$	$v_7$	$v_6$	$v_8$
$B_x$	13011.0363(9)	12998.9857(17)	13028.9751(20)	13006.2313(19)	12998.0750(40)
$B_y$	12099.8672(9)	12015.1109(14)	12098.5694(18)	12057.4635(14)	12005.4674(37)
$B_z$	6260.64550(83)	6255.24152(100)	6201.61605(110)	6282.34695(97)	6260.81793(62)
$\Delta_J$ ( $\times 10^1$ )	0.1411303(118)	0.1376247(173)	0.1455271(227)	0.1450237(233)	0.1398794(266)
$\Delta_{JK}$ ( $\times 10^1$ )	-0.2016851(263)	-0.1898288(582)	-0.2009457(858)	-0.2195221(621)	-0.1900644(1073)
$\Delta_K$ ( $\times 10^2$ )	0.7391763(1958)	0.657399(537)	0.604707(777)	0.969217(586)	0.636145(1014)
$\delta_J$ ( $\times 10^2$ )	0.118207(37)	0.12182(22)	0.12785(46)	0.14689(14)	0.12007(103)
$\delta_K$ ( $\times 10^1$ )	-0.205381(80)	-0.199121(282)	-0.27632(55)	-0.13082(35)	-0.17833(59)
$H_J$ ( $\times 10^7$ )	0.18871(681)	0.1895(193)	0.41398(3140)		0.51047(6505)
$H_{JK}$ ( $\times 10^7$ )	-0.941481(47120)	-2.1043(1288)	-5.32575(23190)	-1.3798(4194)	-2.6373(3024)
$H_{KJ}$ ( $\times 10^7$ )	0.989368(126900)	4.41454(2203)	11.3406(3971)	4.1976(12790)	4.14585(28780)
$H_K$ ( $\times 10^7$ )	-0.23920(8575)	-2.4851(1312)	-6.80644(19780)	-2.5066(8764)	-2.0240(533)
$h_J$ ( $\times 10^8$ )	-0.97610(2926)	-0.955(223)	-1.94(73)	-0.125(89)	-5.814(1537)
$h_K$ ( $\times 10^6$ )	-0.1102(97)	0.1224(491)	0.6103(1014)	-0.06546(3604)	0.194(120)
$h_K$ ( $\times 10^5$ )	0.11170(350)	0.00760(568)	-0.02870(990)		
$L_J$ ( $\times 10^{12}$ )	-0.1564(1404)			3.4299(22610)	
$L_{JK}$ ( $\times 10^{11}$ )	0.49019(9097)			-0.94605(68860)	
$L_{JK}$ ( $\times 10^{10}$ )	-0.367702(27670)			0.59592(46610)	
$L_{KK}$ ( $\times 10^{10}$ )	0.750362(37290)				
$L_K$ ( $\times 10^{10}$ )	-0.430728(17730)	-0.00368(232)			
$l_J$ ( $\times 10^{13}$ )	0.998(701)			-6.21(411)	
$l_{JK}$ ( $\times 10^{11}$ )	-0.500(268)			2.290(1975)	
$l_{KJ}$ ( $\times 10^{10}$ )	0.1337(731)				
$l_K$ ( $\times 10^{10}$ )	-0.2552(406)				
rms	0.109	0.124	0.068	0.086	0.066
lines	465	234	148	188	215

THE  $v_8$  STATE

The  $v_8$  vibrational state, which is derived from the  $\text{NO}_2$  out-of-plane vibration, lies  $762 \text{ cm}^{-1}$  above the ground state<sup>8</sup> and results in transition strengths that are reduced by a factor of about 50. Although the mm/submm spectrum of nitric acid is very crowded, our previous analyses of the lower-lying vibrational states allowed us to eliminate the large proportion of stronger lines that did not belong to  $v_8$  and greatly simplified the assignment. The rotational spectrum reported here was associated with the band identified in the i.r. as  $v_8$  on the basis of its intensity relative to the other vibrational states. Table 1 shows the 215 lines of this state that have been measured and assigned. These cover the range from  $J = 9$  to 46 and from  $K_p = 0$  to 21. The spectral constants that result from analysis of these data are shown in Table 2, along with the rms deviation of the fit, 0.066 MHz. Because of correlations among the constants, it is necessary to retain more digits in the spectral constants than indicated by the uncertainties, so that the spectrum can be accurately calculated from the constants.

## THE GROUND STATE

Although we have published extensive analyses of the ground state of nitric acid, in the course of this work our search for the substantially weaker lines of the excited vibrational states has led us to measure 194 additional lines of the ground-state spectrum. Many of these are at higher energy than those previously measured. This fact allows not only an improved calculation of the ground-state spectrum and its associated spectral constants, but the additional redundancy strengthens our test for misassigned lines and extends the frontier of assignment surely to substantially higher energy.

Table 3 lists the newly-measured transitions; the rest of the data set is not reproduced here but is taken from Refs. 1–6. These range to  $J = 70$  and to  $K_p = 51$ . The constants that result from this analysis are shown in Table 2, along with the deviation of the fit, 0.109 MHz. This deviation is somewhat larger than current measurement uncertainties, estimated to average 0.100 MHz, because of the large number of data sources that have been included in the analysis.

## OVERVIEW OF THE FIRST FIVE VIBRATIONAL STATES OF NITRIC ACID

The strongest features in the nitric acid spectrum are due to  $\Delta J = 1$  transitions that are quadruply degenerate. These transitions are of the form

$$J' - n(n, J' - 2n) \rightarrow J' - 1 - n(n, J' - 1 - 2n), \quad (7)$$

$$J' - n(n + 1, J' - 2n) \rightarrow J' - 1 - n(n + 1, J' - 1 - 2n), \quad (8)$$

$$J' - n(n, J' - 2n) \rightarrow J' - 1 - n(n + 1, J' - 1 - 2n), \quad (9)$$

$$J' - n(n + 1, J' - 2n) \rightarrow J' - 1 - n(n, J' - 1 - 2n), \quad (10)$$

where  $J'$  is the maximum  $J$  value for the branch and where  $n = 0, 1, 2, \dots$ . These values occur in bands of lines which, in the near oblate asymmetric-rotor limit, are separated by  $B_x + B_y - 4B_z$ .<sup>17</sup> For the vibrational states of nitric acid, this number is nearly zero and the bands are closely spaced. The spectra of the several states were assigned by using our broadband spectrometer to record the spectrum around the location of the band head. The different states then appeared as families of equally-spaced lines that were identifiable on the basis of their relative strengths. Identification of the observed spectra with the previously defined vibrational numbering scheme was done by an extensive intercomparison of the relative intensities. For lines of reasonable strength, the intensity ratios agreed with expectations to about 10%.

In addition to their utility in assigning the spectra, transitions of the type discussed have been used for the detection of the ground state of nitric acid in the atmosphere. The near degeneracy of many strong lines in each branch of the ground state provides easily identifiable spectroscopic features;<sup>6</sup> airborne observations of stratospheric emission spectra have detected these features.<sup>26,27</sup> Each excited vibrational state displays a similar near degeneracy of strong transitions, raising the possibility of assigning excited state transitions in atmospheric spectra.

In Table 2 we have collected together the spectral constants of the ground state and the first four vibrational states  $v_9$ ,<sup>14</sup>  $v_7$ ,<sup>15</sup>  $v_6$ ,<sup>16</sup> and  $v_8$  of nitric acid. At very high resolution, the torsional motion of the NO<sub>2</sub> group, which gives rise to the  $v_9$  vibrational state, produces a small splitting (about 2MHz) in the observed b-type rotational spectrum.<sup>14</sup> The constants shown in Table 2 for that state are from an analysis of 234 lines of the essentially unperturbed a-type spectrum; these results are representative of all the states that lie below 1200 cm<sup>-1</sup>. Although, for each of these states, a large amount of data was acquired (more than 1000 transitions were measured), the observed data represent only a small fraction of the observable transitions. It was the aim of this work to measure a sufficiently large number of lines in each vibrational state to be able to predict accurately all thermally populated energy levels. Since there is no step function in the thermal population, as a practical matter this work includes levels whose energy was below approx. 1200 cm<sup>-1</sup> (6 kT).

None of these states have shown any evidence of perturbation. In all cases, the theoretical fit to the experimental data has been as expected. In addition, the lower-order distortion constants are relatively constant among the vibrational states. This observation is unlike the well known cases for which there are interactions among different vibrational states; such interactions are often manifested in widely-varying distortion constants since these constants are correlated with the neglected interaction terms.

Because of the extremely crowded nature of this spectrum and the large number of states involved, we have made extensive use of the procedure in which observed lines are removed one at a time from the data set, the remaining lines were analyzed to predict the frequency of the removed line, and comparisons were then made between the predicted frequency, the calculated uncertainty in the predicted frequency, and the observed transition frequency. During the course of these checks, we have found three previously assigned ground-state lines, which are probably incorrectly assigned or blended with another absorption. These are listed in Table 4 and have been removed from the analysis. Although this procedure does not completely ensure against the inclusion of misassigned lines in the analyses of the several vibrational states, the procedure, combined with the substantial redundancy of the data sets, does ensure that any possible misassignments will have no significant effect on the results.

We have also recently reported a systematic study of pressure broadening of nitric acid by both O<sub>2</sub> and N<sub>2</sub>.<sup>18</sup> In that work, 16 transitions in the ground state that are representative of the strong transitions in the mm/submm spectrum of nitric acid were selected for study. Since little variation is expected among the pressure-broadening parameters of the vibrational states, these results should be applicable to all of the spectra reported here, as well as to the vibrational-rotational bands in the infrared. These results, which are significantly different from earlier theoretical predictions, in combination with the results in this paper, provide the parameters necessary to calculate the atmospheric spectral properties of nitric acid for most applications involving these vibrational states.

Table 3. Assignments of observed transitions for ground state (MHz).

J'K'- K+ J"K"- K"+	Observation	Observed - Calculated	J'K'- K+ J"K"- K"+	Observation	Observed - Calculated
9 2 7 - 8 0 8	319698.861	-0.065	32 26 7 - 31 26 6	697731.753	-0.027
9 9 0 - 8 7 1	262111.726	-0.062	33 9 25 - 33 7 26	319081.784	-0.045
9 9 1 - 8 8 0	231328.815	0.020	34 14 20 - 33 14 19	607041.079	-0.058
11 9 3 - 10 9 2	235167.573	-0.093	34 17 17 - 33 17 16	644820.104	-0.081
12 6 6 - 11 6 5	232178.597	-0.118	34 26 9 - 33 26 8	744035.380	0.155
13 3 10 - 12 1 11	457515.938	0.044	34 27 7 - 33 27 6	755750.279	-0.188
13 6 7 - 12 6 6	244528.077	-0.026	35 0 35 - 34 1 34	444283.608	-0.110
13 11 2 - 12 11 1	284871.069	-0.109	35 24 11 - 34 24 10	751809.933	0.013
14 4 10 - 13 4 9	231777.605	-0.143	35 25 11 - 34 25 10	749187.616	0.061
14 8 6 - 13 8 5	283003.024	-0.139	35 30 5 - 34 30 4	753963.992	0.165
15 4 11 - 14 4 10	244286.975	-0.161	36 0 36 - 35 0 35	456784.097	-0.102
15 10 6 - 14 7 7	454869.796	0.079	36 18 18 - 35 18 17	682227.925	0.060
15 10 6 - 14 8 7	454865.045	-0.011	36 24 13 - 35 24 12	747097.412	-0.103
16 8 8 - 15 6 9	506141.746	0.004	37 18 19 - 36 18 18	694608.396	0.004
16 9 8 - 15 7 9	506143.100	0.065	38 11 27 - 37 11 26	619342.933	0.085
16 11 6 - 15 9 7	479188.769	0.055	38 21 17 - 37 21 16	745021.509	-0.034
17 13 5 - 16 10 6	491280.049	0.048	39 1 38 - 38 1 37	506804.754	-0.156
18 0 18 - 17 0 17	231627.279	-0.114	39 7 32 - 38 7 31	581849.575	-0.034
18 11 7 - 17 11 6	371392.224	-0.038	39 9 30 - 38 9 29	606833.467	0.019
18 12 7 - 17 12 6	370541.181	-0.141	39 10 29 - 38 10 28	619322.672	-0.049
18 14 5 - 17 12 6	515772.928	-0.096	40 8 32 - 39 8 31	606821.346	0.001
18 16 2 - 17 15 3	456347.584	0.038	40 12 28 - 39 12 27	656764.256	0.006
18 16 3 - 17 15 2	454557.490	-0.049	41 5 36 - 40 6 35	581825.226	0.014
18 18 0 - 17 17 1	465630.266	-0.018	41 7 34 - 40 7 33	606811.282	-0.001
18 18 1 - 17 17 0	465628.278	0.002	41 11 30 - 40 11 29	656745.307	-0.050
19 3 16 - 18 3 15	281782.006	-0.106	42 6 36 - 41 6 35	606801.677	0.027
19 7 13 - 19 5 14	168985.797	-0.062	42 10 32 - 41 10 31	656733.531	0.054
19 7 13 - 18 7 12	319432.672	-0.016	42 14 28 - 41 14 27	706641.215	0.027
19 14 6 - 18 11 7	552005.830	0.151	42 18 24 - 41 18 23	7566621.405	0.053
19 14 6 - 18 12 7	551842.758	-0.012	43 5 38 - 42 5 37	606791.141	0.012
20 7 13 - 19 7 12	344496.104	-0.052	43 10 34 - 42 10 33	656725.943	0.031
20 15 5 - 19 13 6	546033.763	0.120	43 13 30 - 42 13 29	706616.667	0.070
20 15 5 - 19 15 4	453822.024	-0.164	43 16 27 - 42 16 26	744046.298	0.054
20 18 3 - 19 17 2	507143.929	0.047	43 20 23 - 42 20 22	794085.971	-0.144
21 16 6 - 20 14 7	600598.700	0.076	44 2 24 - 43 2 24	581774.235	0.044
21 17 4 - 20 16 5	536810.322	0.058	44 4 40 - 43 4 39	606778.578	-0.018
21 17 5 - 20 16 4	508458.978	-0.287	44 8 36 - 43 8 35	656720.743	0.095
21 19 2 - 20 17 3	606534.497	-0.042	44 12 32 - 43 12 31	706602.522	0.023
22 0 22 - 21 0 21	281685.373	-0.068	44 14 30 - 43 14 29	731536.408	-0.195
22 7 15 - 21 7 14	369487.272	-0.172	44 16 28 - 43 16 27	756479.879	0.074
22 17 6 - 21 14 7	626621.982	0.028	44 20 24 - 43 20 23	806471.651	0.076
23 16 7 - 22 17 6	491178.870	0.032	45 1 44 - 44 1 43	581749.428	0.064
23 18 5 - 22 18 4	517883.893	0.091	45 3 42 - 44 3 41	606762.991	-0.053
23 19 5 - 22 19 4	499212.170	0.020	46 3 43 - 45 3 42	619245.039	0.047
23 20 3 - 22 20 2	495303.929	0.110	46 6 40 - 45 6 39	656711.004	0.046
24 9 15 - 23 7 16	794479.102	-0.020	46 14 32 - 45 14 31	756427.074	0.139
24 15 9 - 23 15 8	496741.849	-0.008	46 16 30 - 45 16 29	781344.745	-0.004
24 22 3 - 23 22 2	511210.940	0.054	46 19 28 - 45 19 27	806279.639	0.017
25 15 10 - 24 16 9	508461.962	0.217	47 2 45 - 46 2 44	619225.822	-0.078
25 16 10 - 24 16 9	508471.401	-0.002	47 5 42 - 46 5 41	656703.976	-0.109
25 16 9 - 24 14 10	738366.836	0.111	47 6 41 - 46 6 40	669184.388	0.213
27 9 19 - 27 7 20	243964.774	0.011	47 8 40 - 47 8 41	506641.259	0.014
27 9 18 - 26 9 17	457042.054	-0.189	47 9 39 - 47 7 40	493923.543	0.108
27 16 11 - 26 16 10	545907.157	0.020	47 11 36 - 46 11 35	731510.657	-0.056
27 23 4 - 26 21 5	755465.728	0.101	47 15 32 - 46 15 31	781322.205	0.198
28 9 19 - 28 9 20	243809.970	-0.034	48 0 48 - 47 0 47	606689.260	0.022
28 20 8 - 27 20 7	622601.317	-0.072	48 4 44 - 47 4 43	656694.546	0.081
29 0 29 - 28 0 28	369257.890	-0.125	48 6 43 - 47 6 42	669178.253	0.057
29 25 4 - 28 25 3	624775.530	0.010	48 12 36 - 47 12 35	756415.986	-0.205
30 20 11 - 29 20 10	621886.823	-0.006	48 39 10 - 48 37 11	231235.699	0.030
30 21 9 - 29 21 8	656060.041	0.142	49 3 47 - 49 1 48	595347.120	-0.249
30 26 4 - 29 25 5	756713.391	-0.143	49 3 46 - 48 3 45	656681.163	0.006
31 10 22 - 31 8 23	281380.457	-0.058	49 5 45 - 48 5 44	669169.325	0.031
31 20 11 - 30 20 10	647591.809	0.040	49 11 39 - 49 9 40	493413.354	-0.001
32 10 22 - 31 10 21	531988.102	-0.025	50 2 48 - 49 2 47	656663.285	0.013
32 16 16 - 31 16 15	607388.926	-0.001	50 4 47 - 50 2 48	595068.762	-0.120

Table 3—continued

$J'K'$	$K'$	$J''K''$	$K''$	Observation	Observed - Calculated	$J'K'$	$K'$	$J''K''$	$K''$	Observation	Observed - Calculated
50	3 47	- 49	3 46	669156.576	0.033	57	10 48	- 57	8 49	605675.142	0.029
50	14 36	- 49	14 35	806188.657	-0.303	57	9 48	- 56	9 47	831130.632	-0.111
51	1 50	- 50	1 49	656640.006	0.054	57	15 43	- 57	13 44	541939.071	0.023
51	5 47	- 51	3 48	594783.135	-0.107	58	0 58	- 57	0 57	731440.736	0.194
51	3 49	- 50	3 48	669139.069	0.011	58	1 57	- 57	1 56	743934.850	0.064
51	9 42	- 50	9 41	756431.152	-0.118	58	3 56	- 58	1 57	707784.455	0.139
52	0 52	- 51	0 51	656610.428	0.072	58	4 54	- 57	4 53	781361.368	0.017
52	2 51	- 51	2 50	669115.955	-0.029	58	16 43	- 58	14 44	541604.648	0.010
52	4 48	- 51	4 47	706583.259	-0.066	58	22 37	- 58	20 38	465230.769	0.021
52	6 47	- 52	4 48	594490.337	-0.009	59	1 58	- 58	1 57	756398.030	-0.016
52	8 44	- 51	8 43	756437.867	-0.131	59	4 56	- 59	2 57	707409.179	0.174
52	10 42	- 51	10 41	781329.098	-0.022	59	4 56	- 58	4 55	781353.353	-0.180
53	1 53	- 52	1 52	669086.478	-0.004	59	12 48	- 59	10 49	604985.260	-0.057
53	3 50	- 52	3 49	706572.175	-0.056	59	33 26	- 59	32 27	323167.487	-0.035
54	0 54	- 53	0 53	681560.943	0.062	60	0 60	- 59	0 59	756369.150	0.004
54	2 52	- 53	2 51	706555.832	-0.105	60	5 56	- 60	3 57	707026.291	0.154
54	8 46	- 53	8 45	781348.653	-0.045	60	24 37	- 60	22 38	464504.224	-0.006
54	9 46	- 54	7 47	581122.605	-0.015	60	35 26	- 60	33 27	322575.366	0.019
54	12 42	- 53	12 41	831082.382	0.257	61	25 37	- 61	23 38	464123.828	-0.024
55	1 54	- 54	1 53	706533.566	-0.029	62	0 62	- 61	0 61	781289.975	0.066
55	3 52	- 54	3 51	731506.928	-0.042	62	15 48	- 62	13 49	603889.642	-0.107
55	7 48	- 54	7 47	781356.497	-0.155	62	26 37	- 62	24 38	463731.655	0.004
55	20 36	- 55	18 37	453513.656	0.060	63	16 48	- 63	14 49	603507.920	0.104
56	0 56	- 55	0 55	706504.437	0.072	63	27 37	- 63	25 38	463327.274	-0.032
56	2 54	- 55	2 53	731491.550	0.086	64	28 37	- 64	26 38	462910.543	0.055
56	9 48	- 56	7 49	606008.131	-0.069	65	29 37	- 65	27 38	462480.858	0.002
56	14 43	- 56	12 44	542264.840	-0.004	66	30 37	- 66	28 38	462038.013	-0.044
57	0 57	- 56	0 56	718973.467	0.083	67	31 37	- 67	29 38	461581.756	0.025
57	1 56	- 56	1 55	731469.683	0.081	68	32 37	- 68	30 38	461111.508	0.007
57	2 55	- 56	2 54	743956.380	-0.031	69	33 37	- 69	31 38	460626.956	-0.026
57	3 54	- 56	3 53	756433.958	-0.201	70	34 37	- 70	32 38	460127.787	0.014

Table 4. Transitions not included in the ground state fit.

$J' K'$	$K'$	$J'' K''$	$K''$	Observation	Reference
14	0	14	- 13	1 13	181560.28
58	45	13	- 58	45 14	30957.151
50	0	50	- 49	0 49	631654.53

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