## LING4400: Lecture Notes 16 Anaphora

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### 16.1 Anaphora

Anaphora are words (e.g. pronouns like it and they) that re-use or inherit constraints.
The constraints they inherit are translated from an antecedent (e.g. a preceding noun phrase).
Some common anaphora (indexed $i$ and underlined), with antecedents (indexed but not underlined):

1. pronouns:
(1) Etna $a_{i}$ erupted. It $t_{i}$ is in Italy.
(2) $[\text { Two volcanoes }]_{i}$ erupted. They $y_{i}$ are in Italy.
(3) It is not true that $[\text { fewer than three volcanoes }]_{i}$ erupted. They $y_{i}$ are in Italy.
2. possessive pronouns:
(4) Italy $_{i}$ is in Europe. Itsi capital is Rome.
3. definite references:
(5) Italy contains $[\text { two volcanoes }]_{i}$. [The volcanoes $]_{i}$ erupted.
(6) Italy contains $[\text { two volcanoes }]_{i}$. [Italy's volcanoes $]_{i}$ erupted.
4. deictic pronouns:
(7) a. Italy contains $[\text { Two volcanoes }]_{i}$. [These volcanoes] $]_{i}$ erupted.
b. Italy contains $[\text { Two volcanoes }]_{i}$. [Those volcanoes $]_{i}$ erupted.
(8) a. Italy contains $[\text { Two volcanoes }]_{i}$. These ${ }_{i}$ erupted.
b. Italy contains $[\text { Two volcanoes }]_{i}$. Those $i_{i}$ erupted.

## 5. temporal anaphora:

(9) Etna erupted ${ }_{i}$. It was recent.
6. propositional anaphora:
(10) Etna erupted ${ }_{i}$. France wanted $i t_{i}$.

## 7. bridging anaphora:

(11) Etna $i_{i}$ erupted. The lava []$_{i}$ was hot.
(12) Etna $i_{i}$ erupted. Other volcanoes []$_{i}$ did not erupt.

### 16.2 Intra-sentential anaphora

How can we express anaphora in logic? Some anaphora can just re-use variables.
For example:
(13) a. Fiji contains several provinces and funds them.
b. (entailed by 13a:) Fiji funds the provinces it contains.
can be translated as:

$$
\llbracket\left(\text { Several }_{\langle e, t\rangle} \text { Province }\left(\text { And }_{\langle e,\langle e, t\rangle\rangle} \text { Contain Fund }\right)\right) \text { Fiji } \rrbracket^{M}
$$

or, equivalently, showing variables:

$$
\llbracket\left(\text { Several }_{\langle\mathrm{e}, \mathrm{t}\rangle} \text { Province }\left(\lambda_{y: \mathrm{e}} \lambda_{x: \mathrm{e}} \text { Contain } y x \wedge \text { Fund } y x\right)\right) \text { Fiji } \rrbracket^{M}
$$

But it can't be translated as:
(that would let the funded provinces be different than the contained ones).

### 16.3 Discourse anaphora [King, 2004]

When anaphora have antecedents in other sentences this shared-variable analysis doesn't work.
For example, we probably have an intuition that the following claims hold:
(14) a. Nine provinces are in Gabon. Exactly three of Gabon's provinces are coastal.
b. (entailed by14a:) Exactly three coastal provinces are in Gabon.
c. (not entailed by 14a:) Exactly three provinces are in Gabon. They are coastal.

Separate sentences don't seem able to reach in and constrain restrictors in preceding sentences.
This is the translated meaning of 14 b but not 14 :

$$
\text { Three }\left(\lambda_{x: \mathrm{e}} \text { Province } x \wedge \text { Coastal } x\right) \text { (In Gabon) }
$$

How to translate 14 k ? First, assume separate sentences are equivalent to conjoined sentences:
(15) a. Exactly three provinces are in Gabon. They are coastal.
b. (entailing/entailed by 15a:) Exactly three provinces are in Gabon and they are coastal.

Next we introduce new functions Antecedent and Anaphor to be expanded in interpretation.
They don't mean anything in ordinary sentence-level interpretation: $\llbracket$ Antecedent $i q \rrbracket^{M}=\llbracket q \rrbracket^{M}$, but they are expanded in a discourse-level interpretation function $\llbracket \varphi \rrbracket^{M}$ using access function $\llbracket \varphi \rrbracket^{8}$ :

$$
\llbracket \varphi \rrbracket^{\prime M}=\llbracket \llbracket \varphi \rrbracket^{g} \rrbracket^{M}
$$

where $g$ is an assignment - a function from antecedent indices $i$ to expressions $\varphi, \psi$, etc.
The access function substitutes anaphors with antecedents, converted by a closure function $\llbracket \varphi \rrbracket_{i}^{\mathrm{C}}$ :

$$
\begin{aligned}
& \llbracket \text { Anaphor } i \rrbracket^{g}=\lambda_{x_{i}: \mathrm{e}} \llbracket g i \rrbracket_{i}^{\mathrm{C}} \\
& \llbracket \ldots \wedge \varphi_{i} \wedge \ldots \wedge \psi \rrbracket^{g}=\llbracket \ldots \wedge \varphi_{i} \wedge \ldots \rrbracket^{g} \wedge \llbracket \psi \rrbracket \begin{array}{|c}
i: \varphi_{i} \\
\text { other } i^{\prime}: g i^{\prime}
\end{array} \\
& \text { (for ea. anaphor } i \text { in } \psi \mathrm{w} \text {. antecedent } i \text { in } \varphi_{i} \text { ) } \\
& \llbracket \pi\left(\lambda_{\chi: \alpha} \varphi\right)\left(\lambda_{\chi: \alpha} \psi\right) \rrbracket^{g}=\pi\left(\lambda_{\chi: \alpha} \llbracket \varphi \rrbracket^{g}\right)\left(\lambda_{\chi: \alpha} \llbracket \psi \rrbracket^{\text {other } i^{\prime}: g i^{\prime}} \text { ) (quant. } \pi \text {, antecedent } i \text { in } \varphi \text {, anaphor } i \text { in } \psi\right. \text { ) } \\
& \llbracket \pi\left(\lambda_{\chi: \alpha} \varphi\right)\left(\lambda_{\chi: \alpha} \psi\right) \rrbracket^{g}=\pi\left(\lambda_{\chi: \alpha} \llbracket \varphi \rrbracket \stackrel{\left.\begin{array}{c}
i \\
\text { other } i^{\prime}: g i^{\prime}
\end{array}\right)}{ }\right)\left(\lambda_{\chi: \alpha} \llbracket \psi \rrbracket^{g}\right) \quad \text { (quant. } \pi \text {, anaphor } i \text { in } \varphi \text {, antecedent } i \text { in } \psi \text { ) } \\
& \llbracket \varphi \psi \rrbracket^{g}=\llbracket \varphi \rrbracket^{g} \llbracket \psi \rrbracket^{g} \\
& \llbracket \lambda_{\chi: \alpha} \varphi \rrbracket^{g}=\lambda_{\chi: \alpha} \llbracket \varphi \rrbracket^{g} \\
& \llbracket \varphi \rrbracket^{g}=\varphi \\
& \text { (any other function application) } \\
& \text { (any abstraction) } \\
& \text { (if constant or variable) }
\end{aligned}
$$

(Some theories also posit constraints on this accessibility [Heim, 1982].)

The closure function replaces any quantifier outscoping the antecedent with an existential:

$$
\begin{array}{rrr}
\llbracket \text { Antecedent } i \pi \rho \sigma \rrbracket_{i}^{C} & =\left(\rho x_{i} \wedge \sigma x_{i}\right) & \text { (for quantifier } \pi \text {, restrictor } \rho \text {, nuclear scope } \sigma \text { ) } \\
\llbracket \pi \rho \sigma \rrbracket_{i}^{C} & =\left(\text { Some } \llbracket \rho \rrbracket_{i}^{\mathrm{C}} \sigma\right) & \text { (for quantifier } \pi, \text { if antecedent } i \text { in } \rho \text { ) } \\
\llbracket \pi \rho \sigma \rrbracket_{i}^{\mathrm{C}} & =\left(\text { Some } \rho \llbracket \sigma \rrbracket_{i}^{\mathrm{C}}\right) & \text { (for quantifier } \pi, \text { if antecedent } i \text { in } \sigma \text { ) } \\
\llbracket \varphi \psi \rrbracket_{i}^{\mathrm{C}} & =\llbracket \varphi \rrbracket_{i}^{\mathrm{C}} \psi & \text { (if antecedent } i \text { in } \varphi \text { ) } \\
\llbracket \varphi \psi \rrbracket_{i}^{\mathrm{C}} & =\varphi \llbracket \psi \rrbracket_{i}^{\mathrm{C}} & \text { (if antecedent } i \text { in } \psi \text { ) } \\
\llbracket \lambda_{\chi: \alpha} \varphi \rrbracket_{i}^{\mathrm{C}} & =\lambda_{\chi: \alpha} \llbracket \varphi \rrbracket_{i}^{\mathrm{C}} & \text { (any abstraction) }
\end{array}
$$

Here's an example of the whole process (I chose $i=1$ arbitrarily):
$\llbracket($ Antecedent 1 Three Province $($ In Gabon $)) \wedge($ All $($ Anaphor 1$)$ Coastal $) \rrbracket^{\mathrm{E}, M}$ $=\llbracket($ Three Province $($ In Gabon $)) \wedge\left(\right.$ All $\left(\lambda_{x_{1}: \mathrm{e}}\right.$ Province $x_{1} \wedge\left(\ln\right.$ Gabon $\left.\left.x_{1}\right)\right)$ Coastal $) \rrbracket^{M}$

Here's the derivation before expansion:


And here's the derivation after expansion:


This is for the sentences:
Gabon contains exactly three provinces. They are coastal.
Note this is different than:
Gabon contains exactly three coastal provinces.

Also note that they is translated as All (Anaphor 1).
This assumes the meaning is that all of the provinces are coastal.

But, it is possible the quantifier is weaker than that:
I hate mosquitoes. They carry malaria.
This doesn't mean all mosquitoes carry malaria, just more than you might think.
This is called a generic [Leslie, 2015]. It's a context-dependent quantifier.

## Practice 16.1:

Translate the following sentences into logic using Antecedent and Anaphor functions:

> Two volcanoes erupted. They are in Italy.

## Practice 16.2:

Translate the following sentences into logic by expanding Antecedent and Anaphor functions:
Two volcanoes erupted. They are in Italy.

### 16.4 More existential closure

You may have noticed quantifiers above the Antecedent are replaced with Some.
This is another form of existential closure for variables outside the antecedent.

For example, here is a derivation of a translation of: Two pools contain a geyser. They erupt.


The expansion requires existential closure of variable $y$ :


## 16.5 'Donkey' anaphora

A historically interesting case has anaphors and antecedents in different quantifier arguments.

Here is a derivation of a translation of Most who own a donkey feed it:

and here's the result of expanding these functions:


## References

[Heim, 1982] Heim, I. (1982). The semantics of definite and indefinite NPs. University of Massachusetts at Amherst dissertation.
[King, 2004] King, J. C. (2004). Context dependent quantifiers and donkey anaphora. Canadian Journal of Philosophy, 34(sup1), 97-127.
[Leslie, 2015] Leslie, S.-J. (2015). Generics oversimplified. Nous, 49(1), 28-54.

