

LING4400: Study Guide 2

Practice 10.1: schematized function

Define a schematized **And** function for conjoining transitive verbs like *peel* and *eat* of type $\langle e, \langle e, t \rangle \rangle$.

$$\llbracket \text{And}_{\langle e, \langle e, t \rangle \rangle} \rrbracket^M = \llbracket \lambda_{f: \langle e, \langle e, t \rangle \rangle} \lambda_{g: \langle e, \langle e, t \rangle \rangle} \lambda_{x_2: e} \lambda_{x_1: e} f x_2 x_1 \vee g x_2 x_1 \rrbracket^M$$

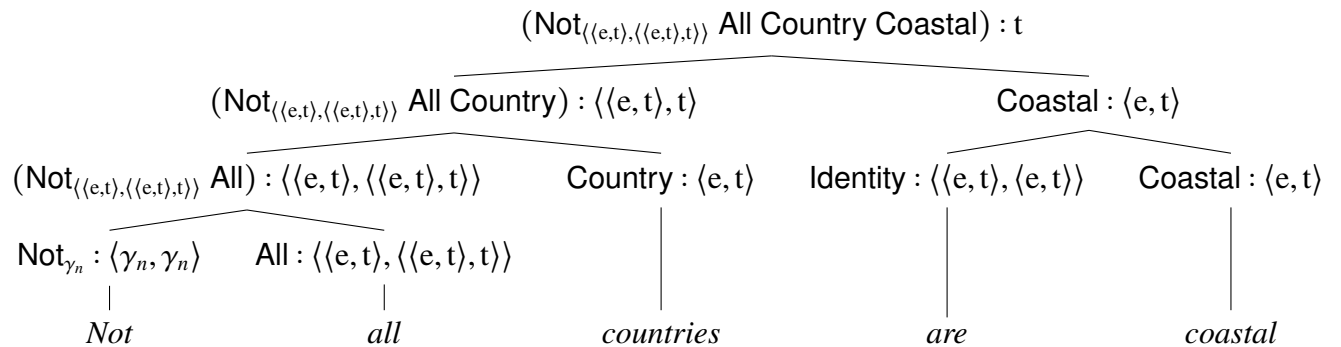
Practice 10.2: schematized function

Define a schematized **Not** _{γ_n} function that can combine with **All**.

$$\llbracket \text{Not}_{\langle e, t \rangle, \langle \langle e, t \rangle, t \rangle} \rrbracket^M = \llbracket \lambda_{f: \langle \langle e, t \rangle, \langle \langle e, t \rangle, t \rangle \rangle} \lambda_{x_2: \langle e, t \rangle} \lambda_{x_1: \langle e, t \rangle} \neg f x_2 x_1 \rrbracket^M$$

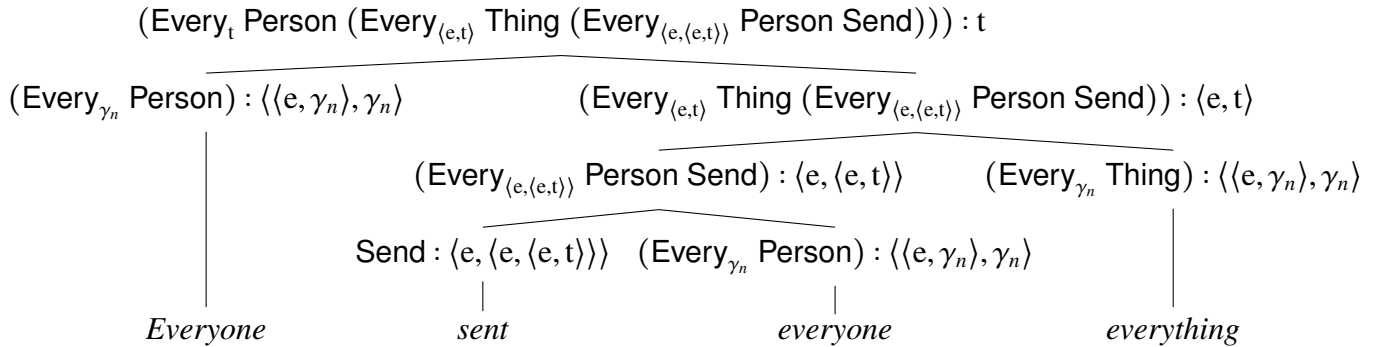
Practice 10.3: tree drawing

Draw a translation tree for *Not all countries are coastal*, using the above function.



Practice 10.4: tree drawing

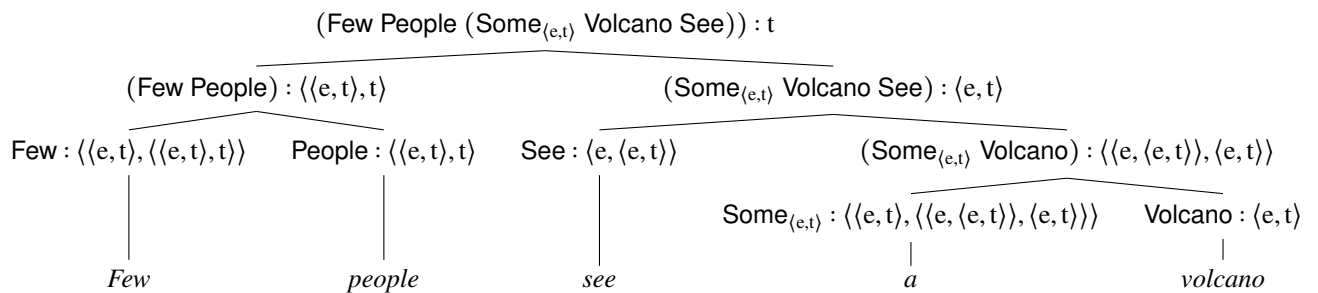
Draw a translation tree for *Everyone sent everyone everything*, using type $\langle e, \langle e, \langle e, t \rangle \rangle \rangle$ for *sent*.



Practice 10.5: translate English to logic

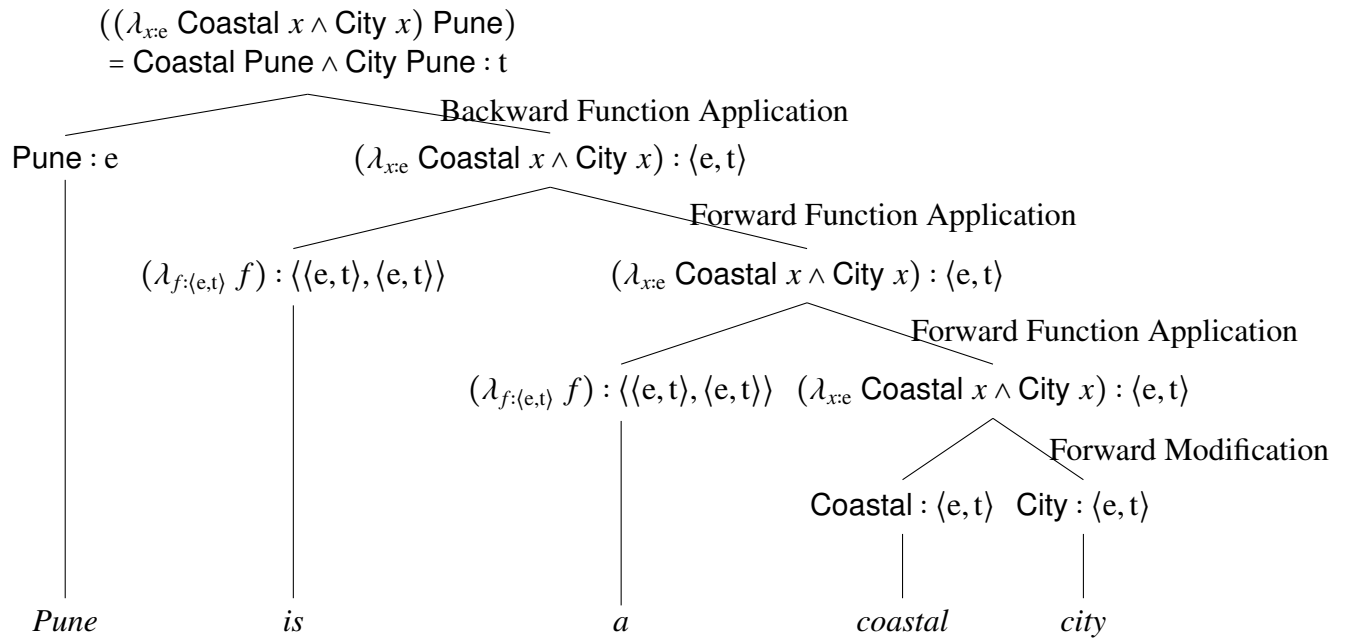
Translate the following into logic by drawing a tree with a logical expression at each branch:

Few people see a volcano.



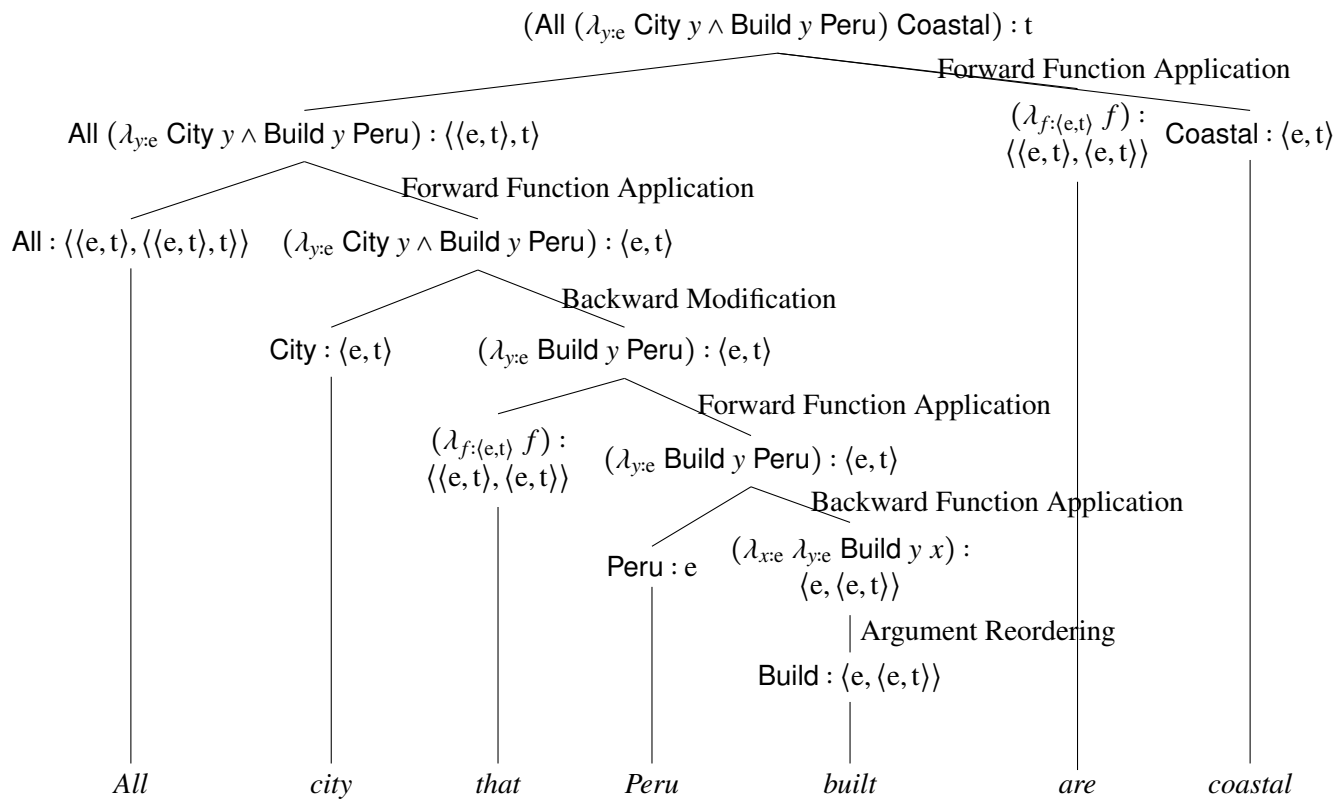
Practice 11.1: trees with rules

Label each branch in the translation tree for the sentence *Pune is a coastal city* with a rule name (forward function application, backward function application, forward modification, backward modification).



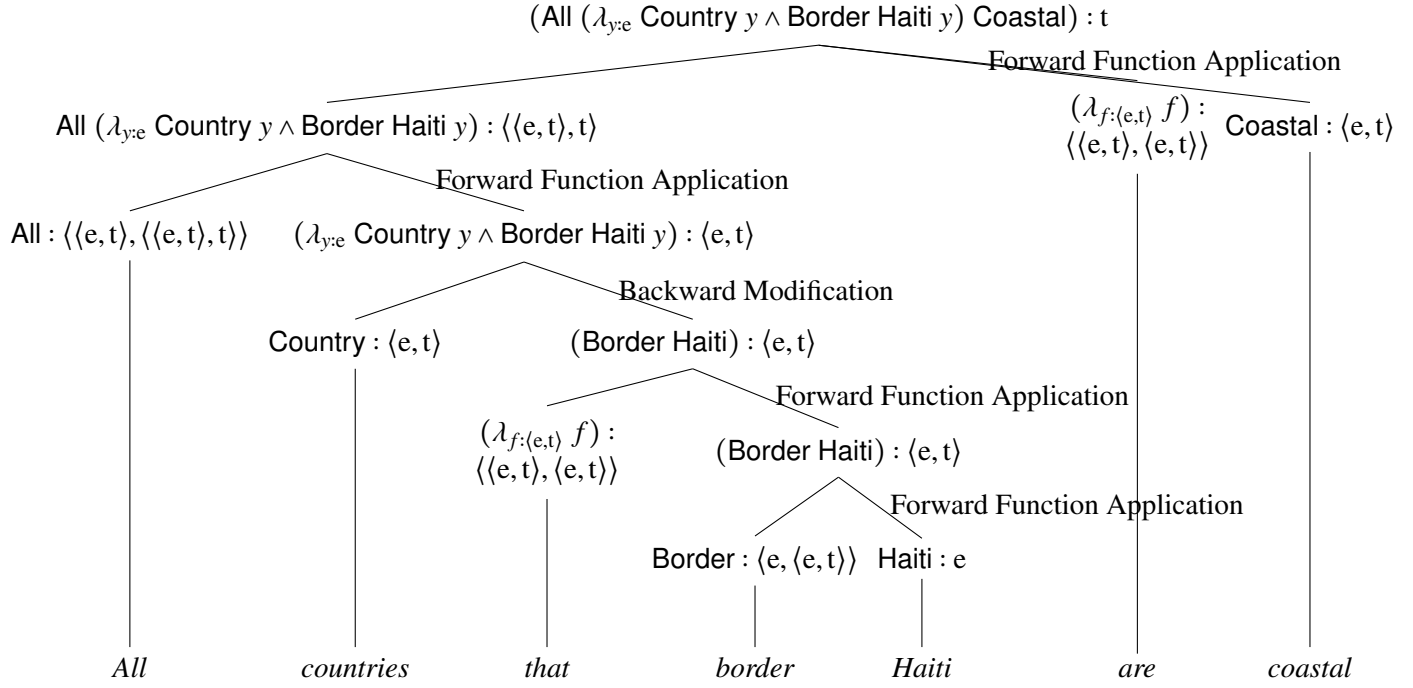
Practice 11.2: trees with rules

- (a) Draw a translation tree for the sentence *all cities that Peru built are coastal*.
- (b) Label each branch in this translation tree with a rule name (forward function application, backward function application, forward modification, backward modification, argument re-ordering).



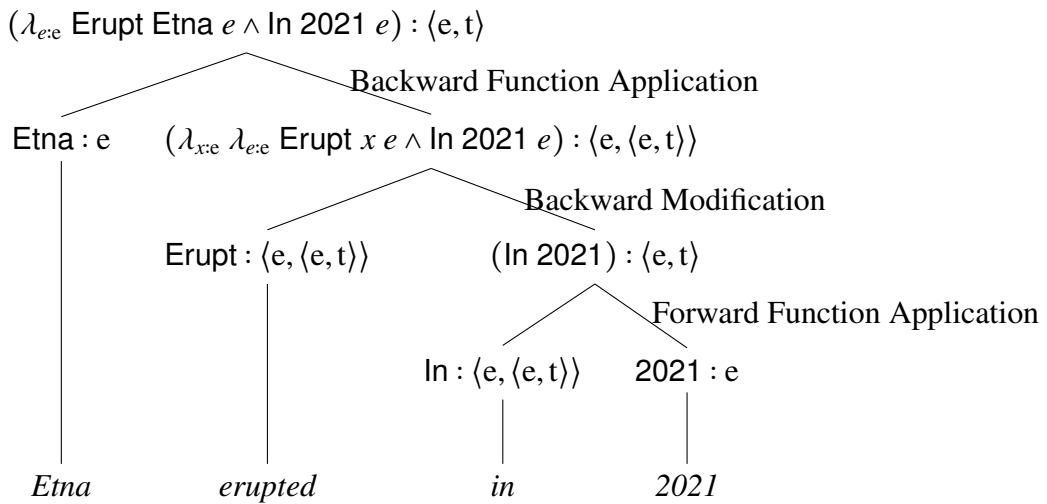
Practice 11.3: trees with rules

- (a) Not all relative clauses need argument re-ordering. Draw a translation tree for the sentence *all countries that border Haiti are coastal*.
- (b) Label each branch in this translation tree with a rule name (forward function application, backward function application, forward modification, backward modification, argument re-ordering).



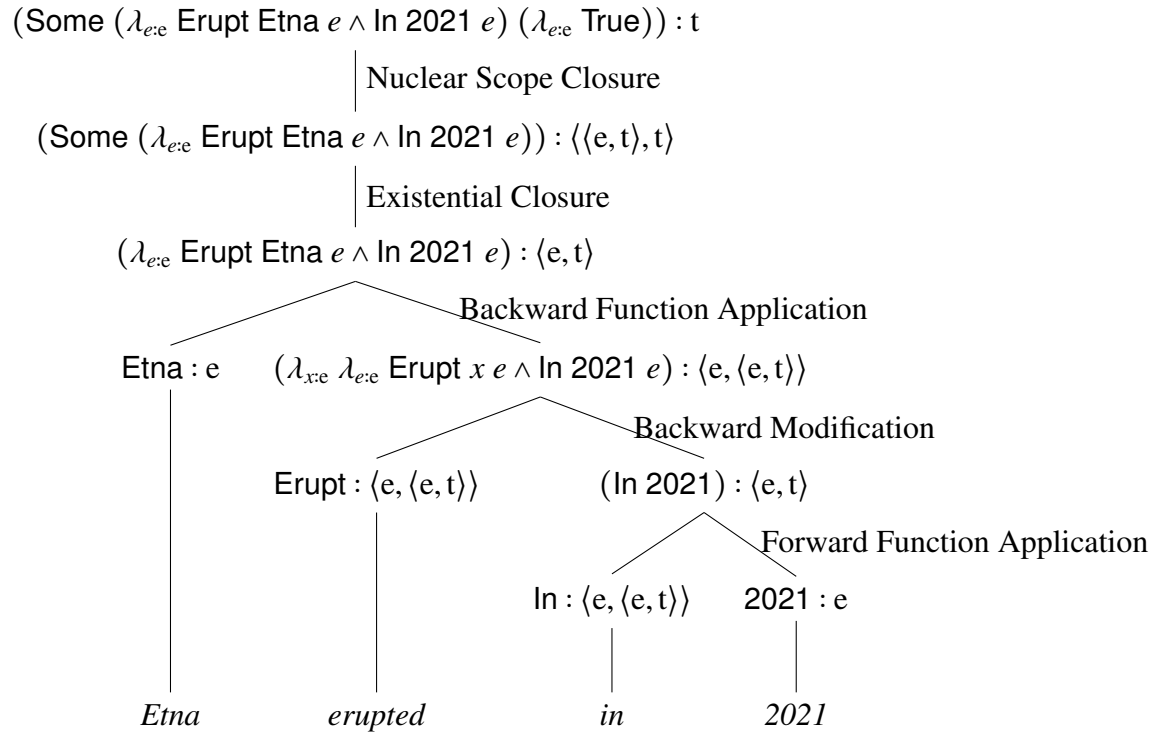
Practice 12.1: trees with rules

Label the initial tree for *Etna erupted in 2021* with rules.



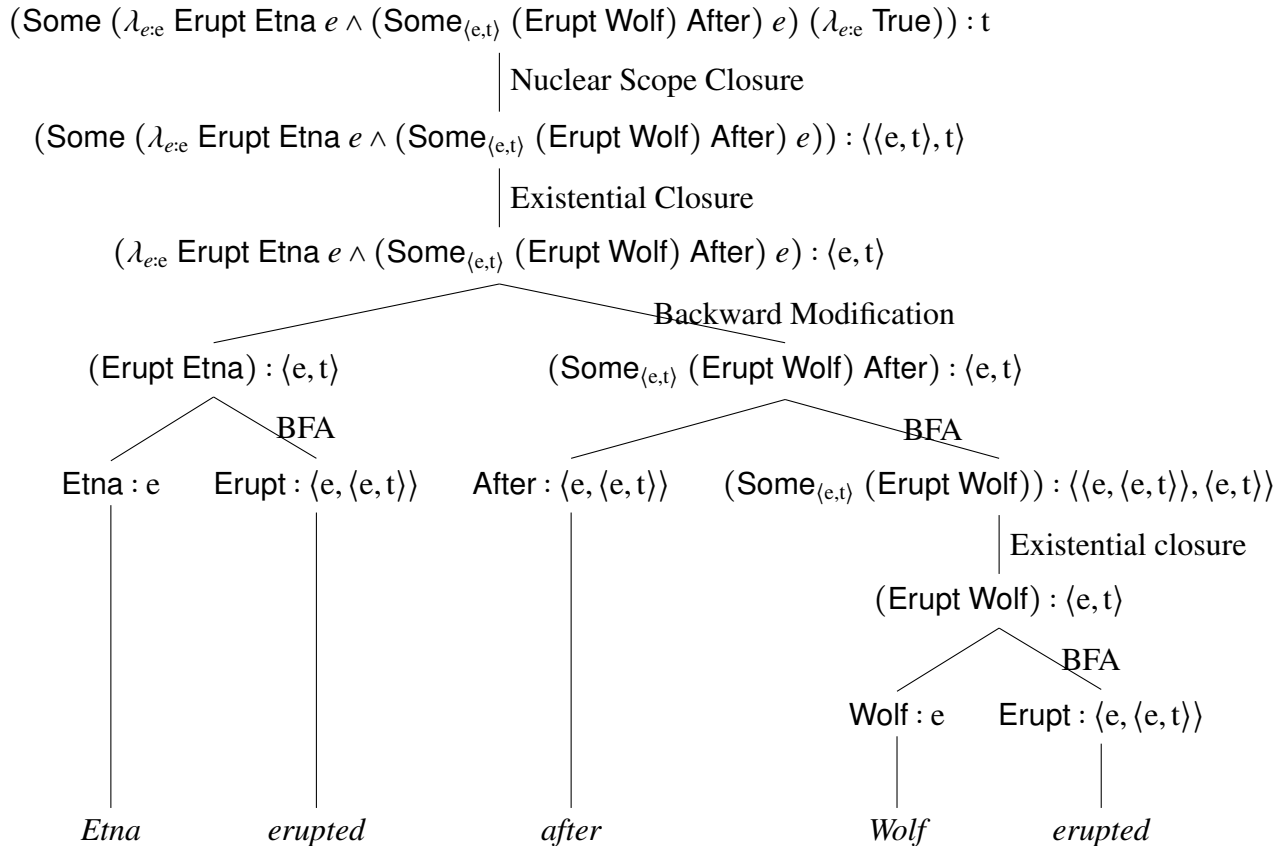
Practice 12.2: trees with rules

Label the complete tree for *Etna erupted in 2021* with rules.



Practice 12.3: trees with rules

Label the tree for *Etna erupted after Wolf erupted* with rules.



Practice 13.1:

Write **logical translations** that distinguish the following sentences:

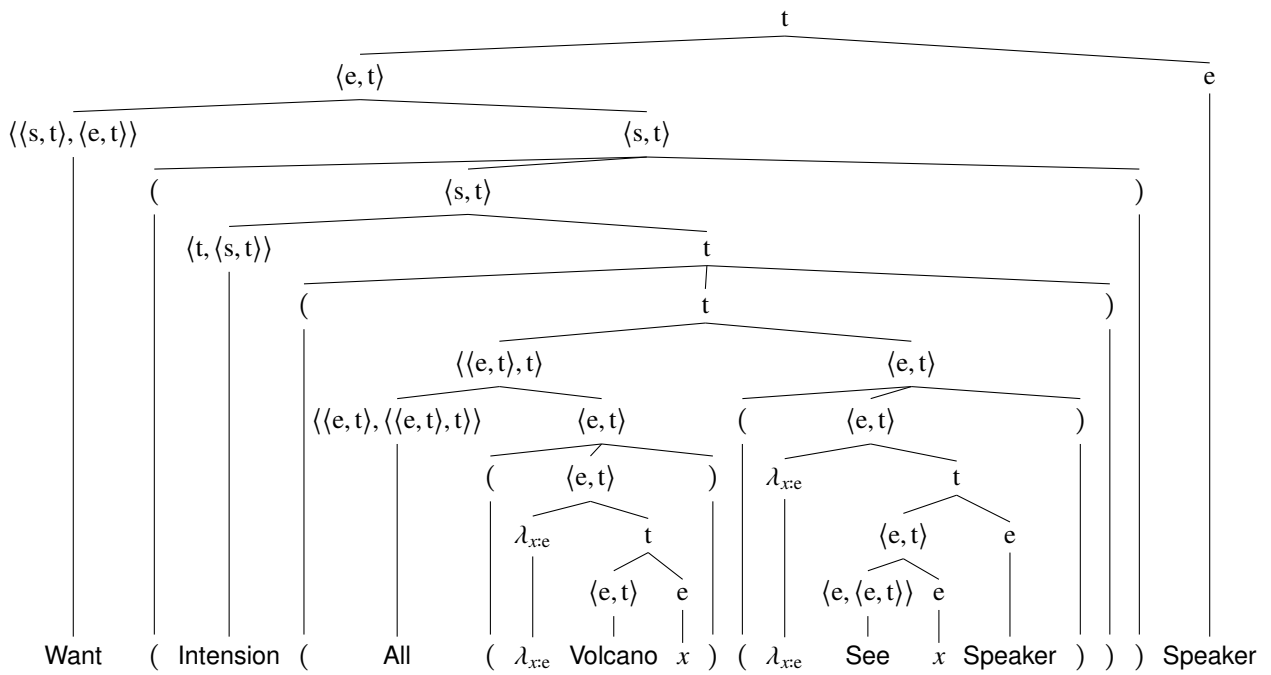
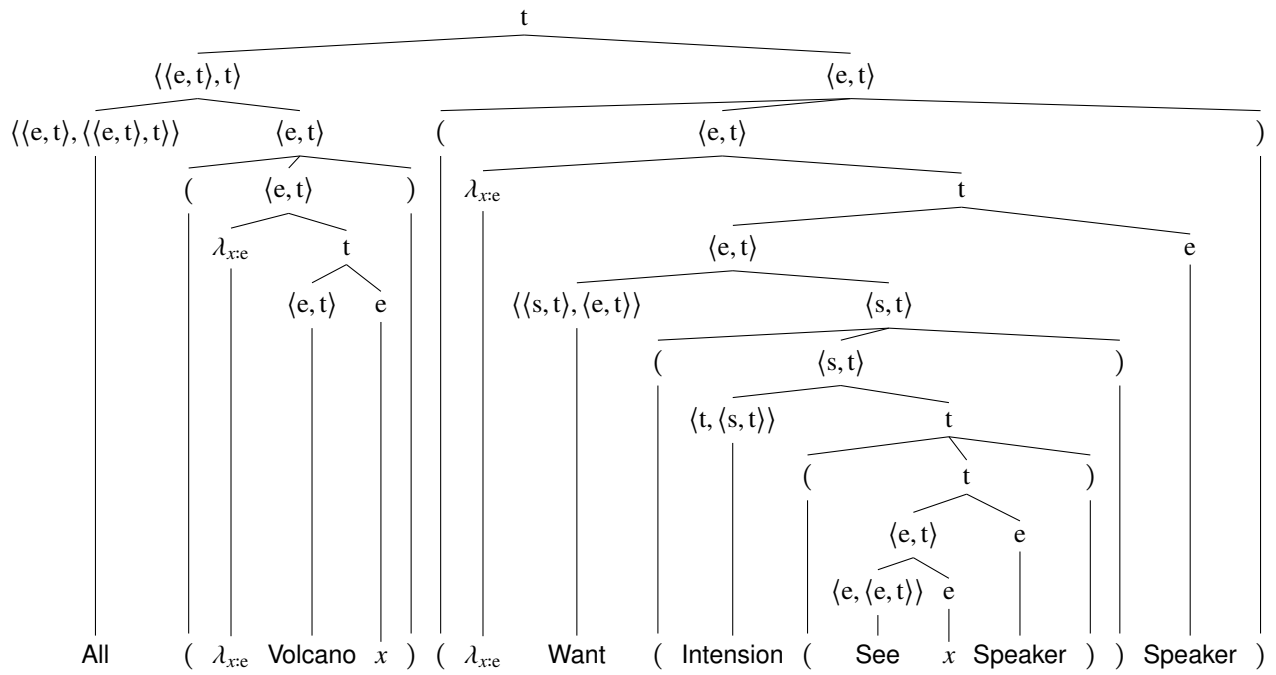
- 1. *France believes it's not true that Etna erupted twice.*
- 2. *It's not true that France believes Etna erupted twice.*

- 1. $\text{Some } (\text{Believe } (\text{Intension } (\text{Not } (\text{Two } (\text{Erupt Etna}) (\lambda_{e:e} \text{ True})))) \text{ France}) (\lambda_{e:e} \text{ True})$
- 2. $\text{Not } (\text{Some } (\text{Believe } (\text{Intension } (\text{Two } (\text{Erupt Etna}) (\lambda_{e:e} \text{ True})))) \text{ France}) (\lambda_{e:e} \text{ True})$

Practice 13.2:

Draw **derivation trees** (with just types at each branch) for the above expressions:

- 1. $\text{All } (\lambda_{x:e} \text{ Volcano } x) (\lambda_{x:e} \text{ Want } (\text{Intension } (\text{See } x \text{ Speaker}))) \text{ Speaker}$
- 2. $\text{Want } (\text{Intension } (\text{All } (\lambda_{x:e} \text{ Volcano } x) (\lambda_{x:e} \text{ See } x \text{ Speaker}))) \text{ Speaker}$



Practice 13.3:

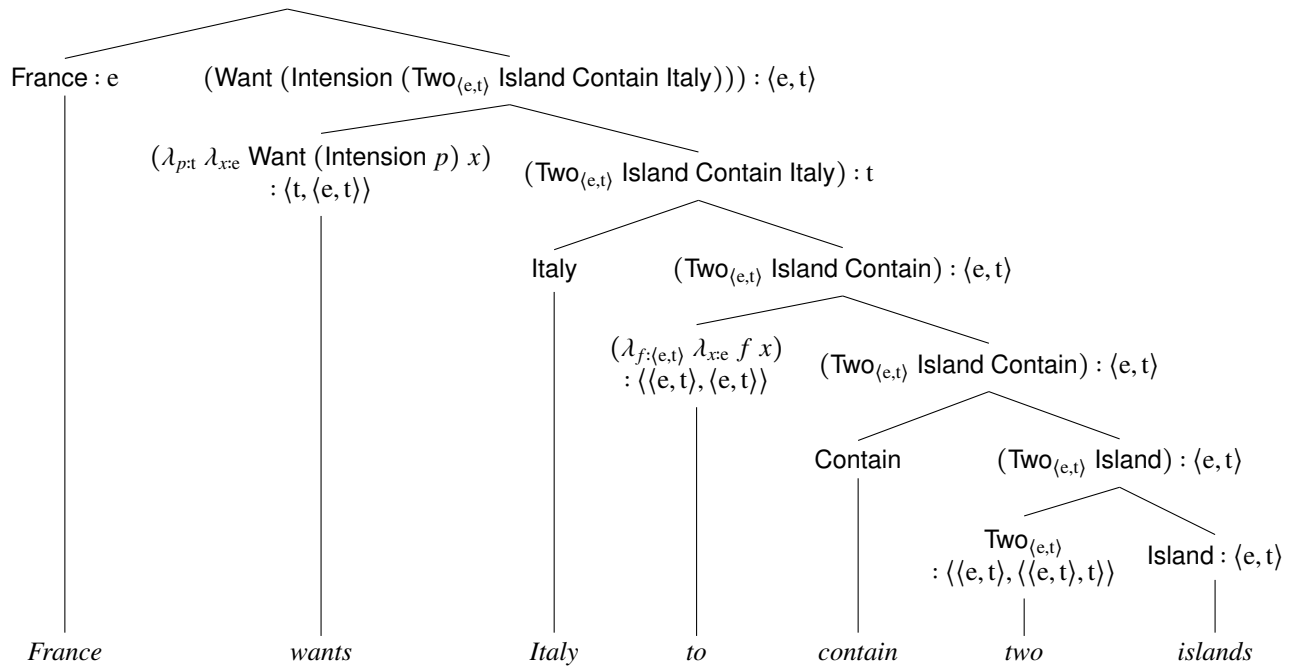
Write an **English translation** of the following logical form (with no eventualities) and draw a **derivation tree with a logical form at each branch** for your translation:

Want (Intension (Two_(e,t) Island Contain Italy)) France

You may assume the following expression for the word *want*:

$\lambda_{p:t} \lambda_{x:e} \text{Want (Intension } p) x$

(Want (Intension (Two_(e,t) Island Contain Italy)) France) : t



Practice 14.1:

Which of the following are valid entailments?

1. *Etna erupts and Wolf erupts*, so *Etna erupts*.
2. *Etna erupts or Wolf erupts*, so *Etna erupts*.
3. *If Etna erupts then Wolf erupts*, and *Etna erupts* so *Wolf erupts*.

1. Valid (because of conjunction elimination)
2. Not valid (disjunction may be satisfied by other disjunct)

3. Valid (because of modus ponens)

Practice 14.2:

Classify the following as right upward or right downward entailing or neither:

1. *at least seven*
2. *at most seven*
3. *exactly seven*
4. *most*

1. Right upward (if *at least seven volcanoes erupt now* then *at least seven volcanoes erupt*)
2. Right downward (if *at most seven volcanoes erupt* then *at most seven volcanoes erupt now*)
3. Neither (no test entailments hold)
4. Right upward (if *most volcanoes erupt now* then *most volcanoes erupt*)

Practice 14.3:

Classify the following as left upward or left downward entailing or neither:

1. *at least seven*
2. *at most seven*
3. *exactly seven*
4. *most*

1. Left upward (if *at least seven coastal volcanoes erupt* then *at least seven volcanoes erupt*)
2. Left downward (if *at most seven volcanoes erupt* then *at most seven coastal volcanoes erupt*)
3. Neither (no test entailments hold)
4. Neither (no test entailments hold)

Practice 14.4:

Which of the following are valid entailments?

1. *Two volcanoes erupted*, so *Two coastal volcanoes erupted*.
2. *Two coastal volcanoes erupted*, so *Two volcanoes erupted*.

1. Not valid (the volcanoes may be inland)

- Valid (*[at least] two* is left upward entailing)

Practice 14.5:

Do the following words behave like negative polarity markers?

- at all*
- usually*

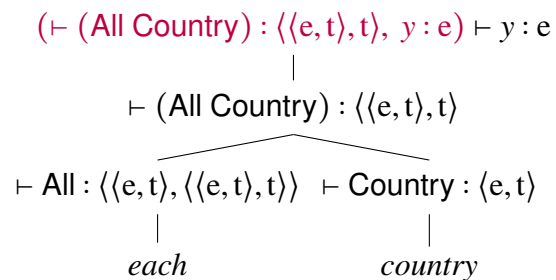
- Yes (*No volcanoes erupt at all* is more grammatical than *Some volcanoes erupt at all*)
- No (*No volcanoes erupt usually* is not more grammatical than *Some volcanoes erupt usually*)

Practice 15.1: trees with sequents

Draw a derivation tree with logical sequents at each branch for the phrase:

each country

in which *each country* undergoes storage.

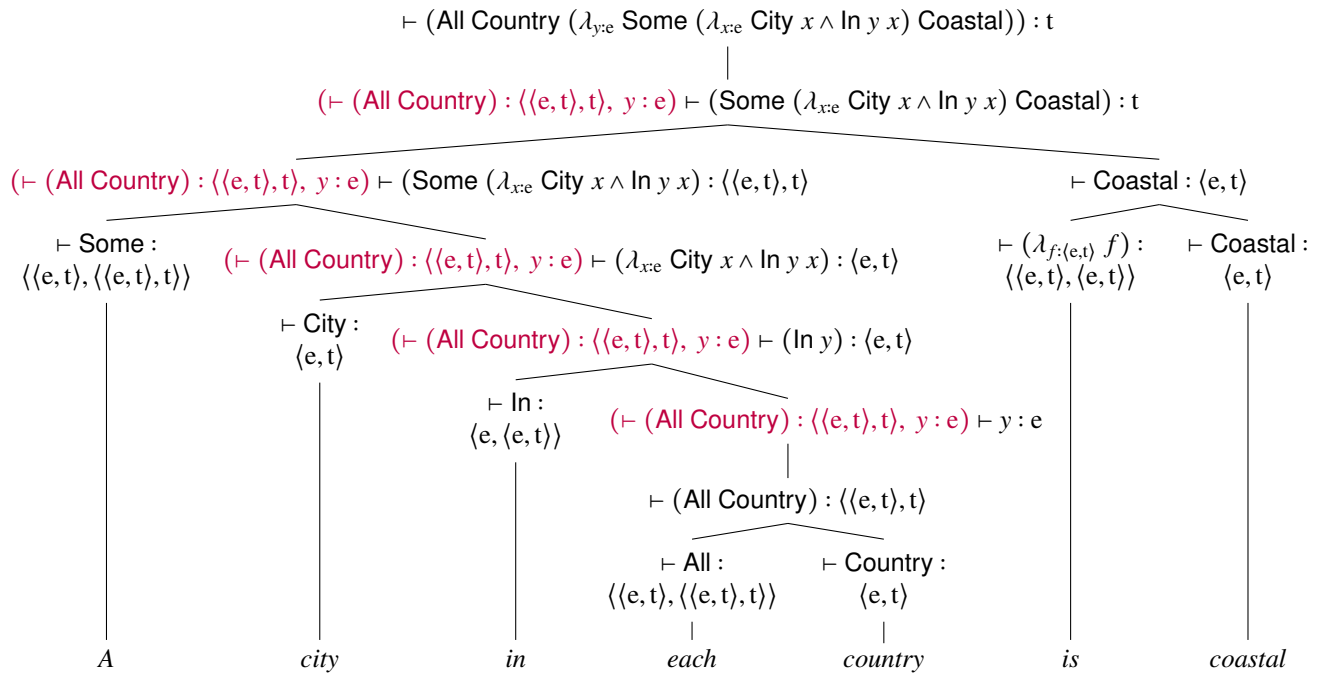


Practice 15.2: trees with sequents

Draw a derivation tree with logical sequents at each branch for the following sentence:

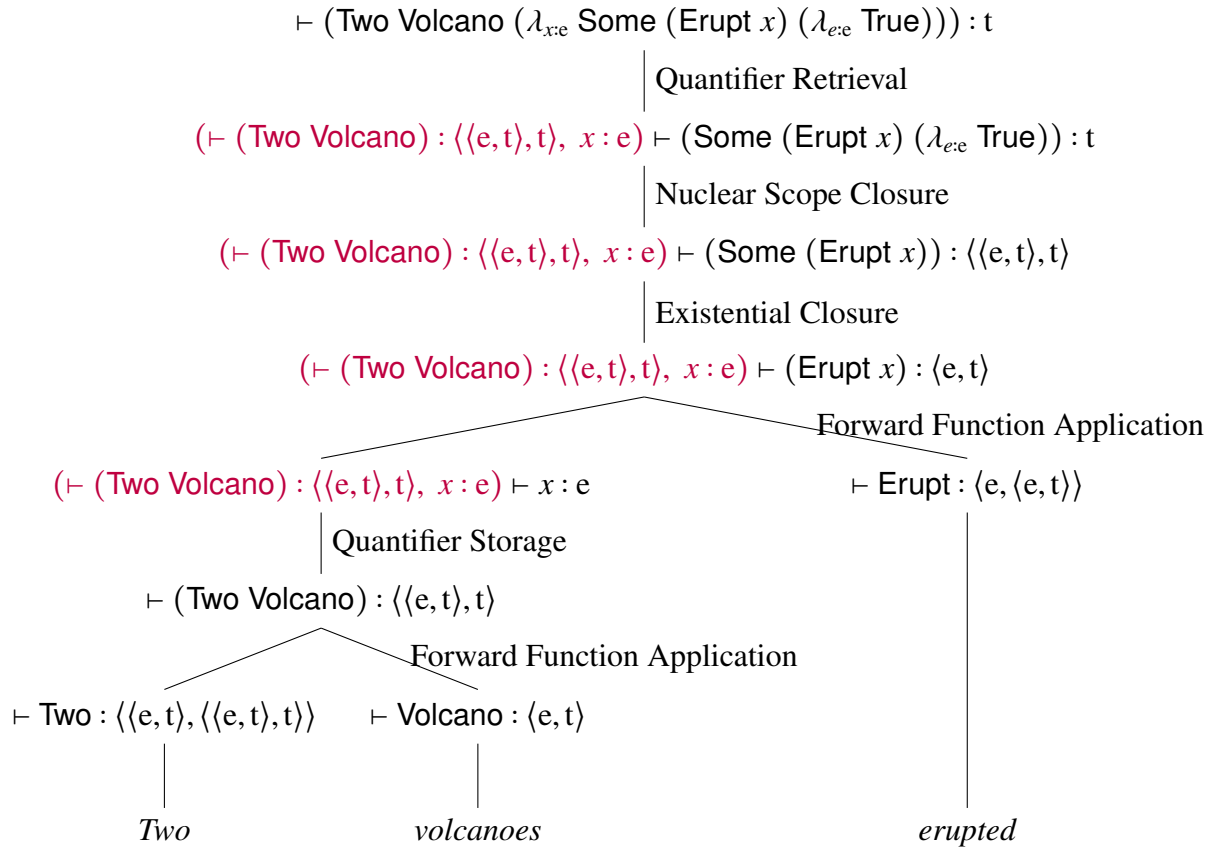
A city in each country is coastal.

in which *each country* is scoped **high**.



Practice 15.3: rule labeling

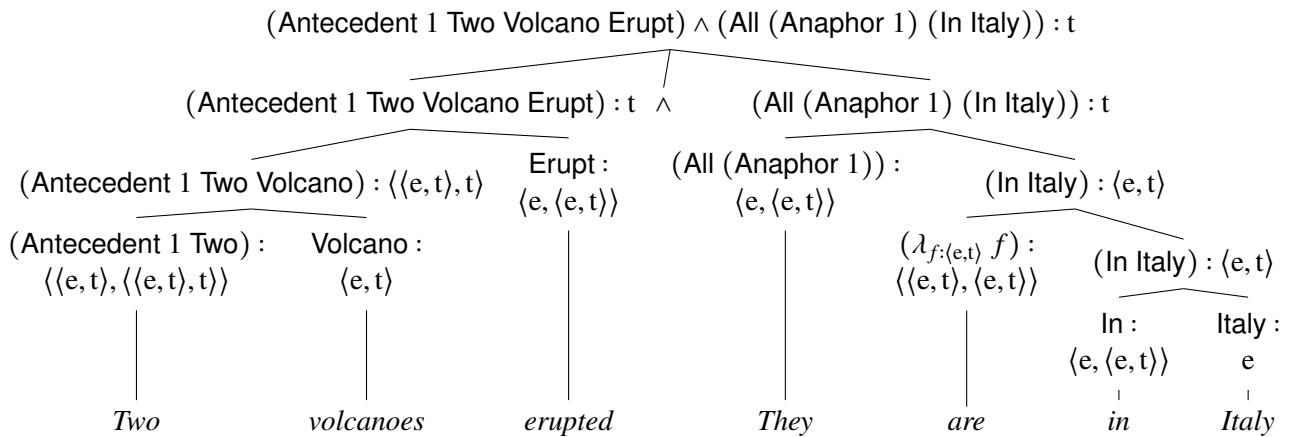
Label the **rules** in the above tree for *Two volcanoes erupted*.



Practice 16.1:

Translate the following sentences into **logic** using **Antecedent** and **Anaphor** functions:

Two volcanoes erupted. They are in Italy.



Practice 16.2:

Translate the following sentences into **logic** by **expanding Antecedent** and **Anaphor** functions:

Two volcanoes erupted. They are in Italy.

