

Relationships between electric force, field, potential energy and potential.

$$\vec{F} = q\vec{E} \quad U = qV \quad \Delta U = q\Delta V$$

$$\Delta V = -\int \vec{E} \cdot d\vec{s} \quad E_x = -\frac{\partial V}{\partial x}$$

Point charges.

$$F = k \frac{q_1 q_2}{r^2} \quad U = k \frac{q_1 q_2}{r} \quad E = k \frac{q}{r^2} \quad V = k \frac{q}{r}$$

Uniform electric fields.

$$\Delta V = -\vec{E} \cdot d\vec{s} \quad E_x = -\frac{\Delta V}{\Delta x}$$

Gauss's law and charge densities.

$$\Phi = \frac{1}{\epsilon_0} q_{enc} \quad q_{enc} = \rho V_{enc} \quad q_{enc} = \sigma A_{enc} \quad q_{enc} = \lambda L_{enc}$$

Electric field magnitudes for symmetric charge distributions.

$$(shell, inside) E = 0 \quad (ball, outside) E = k \frac{q}{r^2} \quad (line) E = \frac{\lambda}{2\pi\epsilon_0 r} \quad (sheet) E = \frac{\sigma}{2\epsilon_0} \quad (cond. surface) E = \frac{\sigma}{\epsilon_0}$$

Magnetic force and field, induction.

$$\vec{F} = q\vec{v} \times \vec{B} \quad \vec{F} = i\vec{L} \times \vec{B} \quad F = \frac{\mu_0 L i_1 i_2}{2\pi r}$$

$$r = \frac{mv_{\perp}}{qB} \quad f = \frac{qB}{2\pi m} \quad p = v_{\parallel} T$$

$$d\vec{B} = \frac{\mu_0 i}{4\pi} \frac{d\vec{s} \times \vec{r}}{r^3} \quad \oint \vec{B} \cdot d\vec{s} = \mu_0 i_{enc}$$

$$B_{wire} = \frac{\mu_0 i}{2\pi r} \quad B_{loop} = \frac{\mu_0 i}{2R} \quad B_{solenoid} = \mu_0 i n \quad B_{torroid} = \frac{\mu_0 i N}{2\pi} \frac{1}{r}$$

$$\mathcal{E} = -N \frac{d\Phi}{dt} \quad \Phi = \int \vec{B} \cdot d\vec{A} \quad \Phi = \vec{B} \cdot \vec{A} \quad \oint \vec{E} \cdot d\vec{s} = -N \frac{d\Phi}{dt}$$

Constants.

$$k = \frac{1}{4\pi\epsilon_0} = 8.99 \times 10^9 \frac{Nm^2}{C^2} \quad \epsilon_0 = 8.85 \times 10^{-12} \frac{C^2}{Nm^2} \quad \mu_0 = 4\pi \cdot 10^{-7} \frac{Tm}{A}$$

$$e = 1.60 \times 10^{-19} C \quad q_{electron} = -e \quad q_{proton} = e$$

Crossproduct

$$\vec{A} \times \vec{B} = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ A_x & A_y & A_z \\ B_x & B_y & B_z \end{vmatrix} = (A_y B_z - A_z B_y) \hat{i} - (A_x B_z - A_z B_x) \hat{j} + (A_x B_y - A_y B_x) \hat{k}$$

Capacitors

$$q = CV$$

$$C = \epsilon_0 \frac{A}{d} \quad \text{for a parallel plate capacitor}$$

$$U = \frac{1}{2} CV^2 = \frac{1}{2} \frac{q^2}{C}$$

$$u = \frac{1}{2} \epsilon_0 E^2$$

$$C_{\text{parallel}} = C_1 + C_2$$

$$q_{\text{parallel}} = q_1 + q_2$$

$$\frac{1}{C_{\text{series}}} = \frac{1}{C_1} + \frac{1}{C_2}$$

$$q_{\text{series}} = q_1 = q_2$$

Current, Resistivity, Power

$$i = \frac{dq}{dt}$$

$$i = \frac{\Delta q}{\Delta t} \quad \text{for a constant current}$$

$$\vec{J} = (ne) \vec{v}_d$$

$$J = \frac{i}{A} \quad \text{for a uniform current}$$

$$\vec{E} = \rho \vec{J}$$

$$P = iV$$

Resistors

$$V = iR$$

$$R = \rho \frac{L}{A} \quad \text{for a conductor of uniform cross-section}$$

$$\frac{1}{R_{\text{parallel}}} = \frac{1}{R_1} + \frac{1}{R_2}$$

$$i_{\text{parallel}} = i_1 + i_2$$

$$R_{\text{series}} = R_1 + R_2$$

$$i_{\text{series}} = i_1 = i_2$$

$$P_R = i^2 R = \frac{V^2}{R}$$

Circuits, RC circuits

$$i_{\text{in}} = i_{\text{out}} \quad \text{at a node or junction}$$

$$\sum \Delta V = 0 \quad \text{around a loop}$$

For a simple RC circuit (battery, resistor, capacitor in series):

$$\text{(charging)} \quad q(t) = C\mathcal{E} (1 - e^{-t/\tau}) \quad \text{(discharging)} \quad q(t) = C\mathcal{E} e^{-t/\tau}$$

$$\tau = RC$$

Constant Acceleration Kinematics.

$$v = v_0 + at \quad x = x_0 + v_0 t + \frac{1}{2} at^2 \quad v^2 = v_0^2 + 2a \Delta x$$