

Name \_\_\_\_\_ KEY \_\_\_\_\_ Rec. Instr. \_\_\_\_\_

1. (4 pts) Mercury has a density of 13.6 g/mL. The pressure measured using a mercury barometer is 745.0 mm Hg. How high would a column of a new high tech oil (density 5.50 g/mL) be at this same pressure AND would this be a reasonably useful barometer? (**EXPLAIN!**). (1 in = 2.54 cm, 1 ft = 0.3048 m)

$$P = g \cdot d \cdot h \quad (\text{See homework problem 10.16 solutions, 10.14 in 10<sup>th</sup> ed.})$$

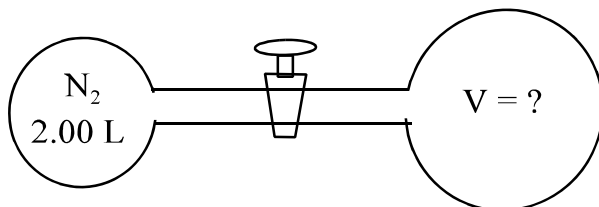
Since the P has to be the same no matter what liquid you have you get,

$$d_2 \cdot h_2 = d_1 \cdot h_1 \quad (P_2 = g \cdot d_2 \cdot h_2, P_1 = g \cdot d_1 \cdot h_1, P_2 = P_1)$$

$$\therefore h_2 = \left(\frac{d_1}{d_2}\right) h_1 = \left(\frac{13.6 \text{ g/mL}}{5.50 \text{ g/mL}}\right) * 745.0 \text{ mm} = 1842.1 \text{ mm oil} = 1.84 \text{ m (6.043 ft)}$$

So a barometer made using this oil would have to be just over 6 ft high to measure this pressure. In order to measure pressures we normally encounter, around 760.0 mm Hg, the barometer would have to be over 6.2 ft high. This would NOT be a very **practical** (useful) barometer. You need to use a liquid with a fairly large density to make a useful barometer or make a fancier barometer.

2. (5 pts) Two flasks are connected by a stopcock. Both flasks are held at the same temperature. The 2.00 L flask is filled with  $N_2$  at a pressure of 1456 mm Hg. The flask with an unknown volume,  $V$ , was evacuated (contains no gas). The stopcock is opened and the  $N_2$  fills both flasks. The resulting pressure after the  $N_2$  fills both flasks is 416 mm Hg? What is the volume,  $V$ , of the flask on the right (in liters, L)?



There's a flask with unknown volume,  $V$ , connected to the 2.0 L flask with  $N_2$  at a pressure of 1456 mm Hg. The stopcock is opened and the  $N_2$  expands to fill both flasks. The final pressure is 416 mm Hg. What is the volume of the flask on the right? Use Boyle's Law to calculate the TOTAL volume of both flasks and then the volume of the flask on the right.

P & V change at constant T - Use **Boyle's Law**

$$P_2 V_2 = P_1 V_1 \quad \text{or} \quad P_f V_f = P_i V_i$$

$$P_1 = 1456 \text{ mm Hg}$$

$$P_2 = 416 \text{ mm Hg}$$

$$V_1 = 2.00 \text{ L}$$

$$V_2 = ? \text{ L}$$

$$V_2 = \frac{P_1 V_1}{P_2} = \left( \frac{P_1}{P_2} \right) V_1 = \left( \frac{1456 \text{ mm Hg}}{416 \text{ mm Hg}} \right) 2.00 \text{ L} = 7.00 \text{ L}$$

Check: If P dec, V inc and it did. Hopefully this makes sense, the gas fills the whole thing.

Determine the volume of the container,

$$V_2 = V_1 + V \quad V = V_2 - V_1 = 7.00 - 2.00 = \mathbf{5.00 \text{ L}}$$

3. (5 pts) What **volume** will 1.60 g of O<sub>2</sub> occupy at STP? (atomic weights: O = 16.00)

There are several methods for solving this problem. In all of them you need to know what STP is.

**STP** => Standard Temp. & Pressure: T = 0°C (273.15K) & P = 1 atm

a) Method 1

To get the volume determine the moles of O<sub>2</sub> and then use IGL (PV=nRT) to get the volume.

$$? \text{ mol O}_2 = 1.60 \text{ g O}_2 \times \frac{1 \text{ mol O}_2}{32.00 \text{ g O}_2} = 0.0500 \text{ mol O}_2$$

$$\begin{aligned} V &= \frac{nRT}{P} = \frac{(0.0500 \text{ mol})(0.08206 \text{ L}\cdot\text{atm/mol}\cdot\text{K})(273.15 \text{ K})}{(1 \text{ atm})} \\ &= 1.12073 \text{ L O}_2 \\ &= 1.12 \text{ L O}_2 \end{aligned}$$

b) Method 2

$$\mathcal{M} = \left(-\frac{RT}{P}\right) D \quad \Rightarrow \quad D = \left(-\frac{P}{RT}\right) \mathcal{M} \quad (\text{in g/L})$$

$$D = \frac{(1 \text{ atm})(32.00 \text{ g/mol})}{(0.08206 \text{ L}\cdot\text{atm/mol}\cdot\text{K})(273.15 \text{ K})} = 1.4276 \text{ g/L}$$

$$V = \frac{m}{D} = \frac{1.60 \text{ g}}{1.4276 \text{ g/L}} = 1.12 \text{ L}$$

Using dimensional analysis:

$$? \text{ L} = 1.60 \text{ g} \times \frac{1 \text{ L}}{1.4276 \text{ g}} = 1.12 \text{ L}$$

c) Method 3 (only usable at STP)

**Molar Volume** at STP: V/n = 22.41 L/mol (1 mol gas = 22.41 L)

$$? \text{ L} = 0.0500 \text{ mol} \times \frac{22.41 \text{ L}}{1 \text{ mol}} = 1.12 \text{ L}$$

4. (5 pts) Consider a cylinder fitted with a movable piston that can expand against the atmosphere. The initial pressure, volume and absolute temperature inside the cylinder are  $P_i$ ,  $V_i$  and  $T_i$ . What is the new **temperature** of the system when the **pressure** is **tripled** and the **volume** is **decreased to one half** of the **original** volume?

Use **Combined Gas Law**:

$$\frac{P_f V_f}{T_f} = \frac{P_i V_i}{T_i}$$

$$P_f = 3P_i \qquad V_f = 1/2 V_i \quad (\text{Vol dec to } 1/2 \text{ its initial value})$$

$$T_f = \frac{P_f V_f}{P_i V_i} T_i = \left(\frac{P_f}{P_i}\right)\left(\frac{V_f}{V_i}\right) T_i$$

$$T_f = \left(\frac{3 P_i}{P_i}\right) \left(\frac{1/2 V_i}{V_i}\right) T_i = (3/2)T_i$$

5. (4 pts) Consider three one-liter flasks labeled A, B, and C filled with the gases NO, NO<sub>2</sub>, and N<sub>2</sub>O, respectively, each at STP. What can be said about the number of molecules of each gas? (atomic weights: N = 14.01, O = 16.00)

We can calculate the moles for each of the gases given using the P, V and T data given, (STP means 1 atm and 0 °C ( 273.15 K)) and a volume of 1 L:

$$n = \frac{PV}{RT}$$

However, you do NOT have to do this calculation. Since all have the same P, V and T they have the **same number of moles (same # of molecules)**.

6. (5 pts) A cylinder of containing  $H_2$  gas with a volume of 18.0 L and a pressure of 35.0 atm at a temperature of 23.0 °C is used to fill smaller cylinders with a volume of 2.00 L. How many smaller cylinders can be filled at a temperature of 25.0 °C to a volume of 2.00 L and a pressure of 745.0 torr (assuming all the gas can be transferred to the smaller cylinders).  
(1 atm = 760 mmHg = 760 torr = 101.325 kPa = 14.7 lb/in<sup>2</sup>)

Since P, V & T all change use the “Super” Combined Gas Law (with n, moles, constant):

$$\frac{P_2 V_2}{n_2 T_2} = \frac{P_1 V_1}{n_1 T_1} \quad \frac{P_2 V_2}{T_2} = \frac{P_1 V_1}{T_1}$$

$$P_1 = 35.0 \text{ atm} \quad V_1 = 18.00 \text{ L} \quad T_1 = 23^\circ\text{C} + 273.15 = 296.15 \text{ K}$$

$$P_2 = 745.0 \text{ torr} \times \frac{1 \text{ atm}}{760 \text{ torr}} = 0.98026 \text{ atm} \quad V_2 = ? \quad T_2 = 25^\circ\text{C} + 273.15 = 298.15 \text{ K}$$

$$V_2 = \frac{P_1 V_1 T_2}{P_2 T_1} = \left(\frac{P_1}{P_2}\right)\left(\frac{T_2}{T_1}\right)V_1 = \left(\frac{35.0 \text{ atm}}{0.98026 \text{ atm}}\right)\left(\frac{298.15 \text{ K}}{296.15 \text{ K}}\right) 18.00 \text{ L} = 647.92 \text{ L}$$

This is the total volume (647.92 L) that could be filled at a pressure of 745.0 torr.

$$\# \text{ cylinders} = 647.92 \text{ L} \times (1 \text{ cylinder}/2.00 \text{ L}) = 323.96 \text{ cylinders} = \mathbf{324 \text{ cylinders}} \quad (3 \text{ s.f.})$$

Could also determine the moles of gas present in the larger cylinder and how many moles could be held in each smaller cylinder and then divide the total you started with by the number of moles which could be put in a smaller cylinder to get the number of small cylinders needed.

7. (4 pts) Five identical 1.0-L flasks contain the following gases each at 0°C and 1 atm pressure. The densities (g/L) of the gases are listed below. Which gas has the **LARGEST** molar mass?

Gas 1	Gas 2	Gas 3	Gas 4	Gas 5
0.178	3.16	0.715	0.760	1.25

The **density** is **directly proportional** to the **molar mass** (molecular or atomic weight). Therefore, the gas with the largest density should have the largest molar mass (MW or AW) (since P, V & T same for all). The densities are listed below, as are the MW (which you didn't need to calculate).

$$\mathcal{M} = \left(\frac{RT}{P}\right) D \quad \Rightarrow \quad D = \left(\frac{P}{RT}\right) \mathcal{M} \quad (\text{in g/L})$$

0.178	<b>3.16</b>	0.715	0.760	1.25
3.99	<b>70.8</b>	16.0	17.0	28.0

8. (5 pts) The empirical formula of a volatile liquid is  $C_2H_4O$ . A 0.345-gram sample of its vapor occupied 85.0 mL at  $100.0^\circ\text{C}$  and 0.942 atm. What is the **molecular formula** for the compound? (Atomic weights: H = 1.008, C = 12.01, O = 16.00)

Determine molecular formula of a gas given the empirical formula,  $C_2H_4O$ , mass & P, V, T data

$$MF = (EF)_n \quad \& \quad MW = n * (EFW) \quad (\text{where } MW = \text{molecular wt and } EFW = \text{empirical formula wt})$$

$$n = \frac{MW}{EFW} \quad \& \quad \mathcal{M} = \frac{\text{mass}}{\text{moles}} \quad (\text{molar mass or molecular wt})$$

Have mass of 0.345 g, need moles. (Remember, molar mass = g/mol, same as MW.)

$$P = 0.942 \text{ atm}; \quad V = 85.0 \text{ mL} = 0.0850 \text{ L}; \quad T = 100^\circ\text{C} + 273.15 = 373.15 \text{ K}$$

$$n_{C_xH_yO_z} = \frac{PV}{RT} = \frac{(0.942 \text{ atm})(0.0850 \text{ L})}{(0.08206 \text{ L}\cdot\text{atm}/\text{mol}\cdot\text{K})(373.15 \text{ K})} = 2.6148 \times 10^{-3} \text{ mol}$$

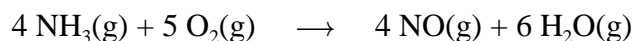
$$\mathcal{M} = \frac{0.345 \text{ g}}{2.6148 \times 10^{-3} \text{ mol}} = 131.93 \text{ g/mol or } 131.93 \text{ amu}$$

$$EFW_{C_2H_4O} = 44.05 \text{ amu}$$

$$n = \frac{131.93 \text{ amu}}{44.05 \text{ amu}} = 2.9951 = 3$$

$$MF = (C_2H_4O)_3 = C_6H_{12}O_3$$

9. (5 pts) What volume (L) of NO at 500°C and 0.5 atm will be produced in the following reaction if 10.0 L of oxygen reacts with excess NH<sub>3</sub> and the volume of NO is measured under the same conditions of temperature and pressure? (atomic weights: N = 14.01, H = 1.008, O = 16.00)



Can calculate the volume of desired from volume of given by using the volume ratio which is the same as the mole ratio from the balanced equation. You can see this from **Avogadro's Law**:

$$\frac{V_2}{n_2} = \frac{V_1}{n_1} \quad \text{or} \quad \frac{n_2}{n_1} = \frac{V_2}{V_1} \quad \text{vol ratio} = \text{mole ratio}$$

$$? \text{ L NO} = 10.0 \text{ L O}_2 \times \frac{4 \text{ L NO}}{5 \text{ L O}_2} = 8.00 \text{ L}$$

numbers in this ratio are  
coefficients in bal. eqn.

Could use the P, T, V data given to first calculate the moles of O<sub>2</sub> that reacts. Then do a mole-to-mole stoichiometry problem to determine the moles of NO produced from the moles of O<sub>2</sub>. Then you could use the moles of NO with the P and T data given to calculate the volume of NO. This is not complicated but certainly more complicated and much more work than above.