Dr. Zellmer
Time: 7 PM Sun.
40 min

Chemistry 1250
Spring Semester 2022
Quiz XII

T, R
April 24, 2022

Name $\qquad$ Rec. TA/time $\qquad$

1. ( 3 pts) Given the following $\mathrm{K}_{\mathrm{a}}$ values, determine which species is the strongest base. Explain!

| $\mathrm{HSO}_{3}{ }^{-} 6.3 \times 10^{-8}$ | $\mathrm{HPO}_{4}^{2-} 4.8 \times 10^{-13}$ | $\mathrm{HCO}_{3}{ }^{-} 4.7 \times 10^{-11}$ |
| :--- | :--- | :--- | :--- |
| $\mathrm{HSO}_{3}{ }^{-} 6.3 \times 10^{-8}$ | $\mathrm{HPO}_{4}{ }^{2-} 4.8 \times 10^{-13}$ | $\mathrm{HCO}_{3}{ }^{-1} 4.7 \times 10^{-11}$ |

Remember:
Larger $\mathrm{K}_{\mathrm{a}}==>$ smaller $\mathrm{pK}_{\mathrm{a}}==>$ stronger acid $==>$ weaker conj. base
Larger $\mathrm{K}_{\mathrm{b}}==>$ smaller $\mathrm{pK}_{\mathrm{b}}==>$ stronger base $==>$ weaker conj. acid
For a conj. Acid-Base pair:

$$
\begin{array}{cc}
\mathrm{K}_{\mathrm{a}} \times \mathrm{K}_{\mathrm{b}}=\mathrm{K}_{\mathrm{w}} & \text { and } \quad \mathrm{pK}_{\mathrm{a}}+\mathrm{pK}_{\mathrm{b}}=\mathrm{pK}_{\mathrm{w}} \\
\mathrm{HSO}_{3}^{-} & \mathrm{SO}_{3}^{2-} \\
\mathrm{K}_{\mathrm{a}}=6.3 \times 10^{-8} & \mathrm{~K}_{\mathrm{b}}=1.6^{\times-} \times 10^{-7} \\
\mathrm{HPO}_{4}^{2-} & \mathrm{PO}_{4}^{3-} \\
\mathrm{K}_{\mathrm{a}}=4.8 \times 10^{-13} & \mathrm{~K}_{\mathrm{b}}=2.1^{2-} \times 10^{-2} \\
\mathrm{HCO}_{3}^{-} & \mathrm{CO}_{3}^{2-} \\
\mathrm{K}_{\mathrm{a}}=4.7 \times 10^{-11} & \mathrm{~K}_{\mathrm{b}}=2.1 \times 10^{-4}
\end{array}
$$

$$
\left.\mathrm{HSO}_{3}^{-} \text {strongest acid (largest } \mathrm{K}_{\mathrm{a}}\right)==>\text { weakest conj. base, } \mathrm{SO}_{3}{ }^{2-}\left(\text { smallest } \mathrm{K}_{\mathrm{b}}\right)
$$

$$
\mathrm{HPO}_{4}{ }^{2-} \text { weakest acid }\left(\text { smallest } \mathrm{K}_{\mathrm{a}}\right)==>\text { strongest conj. base, } \mathbf{P O}_{4}{ }^{3-}\left(\text { largest } \mathrm{K}_{\mathrm{b}}\right)
$$

2. (2 pts) Would you expect the following solutions to be acidic, neutral, or basic? Explain or show work!

In general: cations $=>$ acidic soln (except group $1 \mathrm{~A} \& 2 \mathrm{~A}\left\{\mathrm{Ca}^{2+}, \mathrm{Sr}^{2+}, \mathrm{Ba}^{2+}\right\}$ cations - give neutral)
anions $=>$ basic soln (except conj. bases of strong acids; $\mathrm{Cl}^{-}, \mathrm{Br}^{-}, \mathrm{I}^{-}, \mathrm{NO}_{3}^{-}, \mathrm{ClO}_{3}^{-}, \mathrm{ClO}_{4}^{-}$are neutral $\mathrm{HSO}_{4}{ }^{-}$is acidic)
Also, for most amphoteric anions (like $\mathrm{HCO}_{3}^{-}, \mathrm{HSO}_{3}^{-}, \mathrm{H}_{2} \mathrm{PO}_{4}^{-}$, etc.) you can't tell if it's basic or acidic w/o doing calculations)
a) $\mathrm{KBrO}_{4}---------->\mathrm{K}_{2}^{+}(\mathrm{Oq})+\mathrm{BrO}_{4}^{-}(\mathrm{aq})$ BASIC
$\mathrm{K}^{+}$: group 1A cation ("conj. acid" of a strong base, KOH , and does not act as an acid) - neutral $\mathrm{BrO}_{4}{ }^{-}$is conj. base of a weak acid, $\mathrm{HBrO}_{4}, \&$ acts as a weak base
$\mathrm{BrO}_{4}^{-}(\mathrm{aq})+\mathrm{H}_{2} \mathrm{O}(\ell) \rightleftarrows \mathrm{HBrO}_{4}(\mathrm{aq})+\mathrm{OH}^{-}(\mathrm{aq})$
b) $\mathrm{PbCl}_{2}--------->\mathrm{Pb}^{2+}(\mathrm{aq})+2 \mathrm{Cl}^{-}(\mathrm{aq})$

## ACIDIC

$\mathrm{Cl}^{-}$: conj. base of a strong acid, $\mathrm{HCl} \&$ does not act as a base - neutral
$\mathrm{Pb}^{2+}$ : metal cation - causes soln to be acidic
3. ( 8 pts ) What is the $\mathbf{p H}$ of a $0.30 \mathrm{M} \mathrm{NaCHO}_{2}$ solution at $25^{\circ} \mathrm{C} ?\left(\mathrm{HCHO}_{2}: \mathrm{K}_{\mathrm{a}}=1.8 \times 10^{-4}\right.$, at $\left.25^{\circ} \mathrm{C}\right)$ (Show the ICE table, state any assumptions made and check your percent error.) Explain or show work!

Hydrolysis problem (salt solution- ions reacting with $\mathrm{H}_{2} \mathrm{O}$ to make the soln acidic or basic)

## GENERALLY:

Cations - acidic (except group 1A \& 2A $\left\{\mathrm{Ca}^{2+}, \mathrm{Sr}^{2+}, \mathrm{Ba}^{2+}\right\}$ cations which are neutral)
Anions - basic (except conj. base of strong acids: $\mathrm{Cl}^{-}, \mathrm{Br}^{-}, \mathrm{I}^{-}, \mathrm{NO}_{3}^{-}, \mathrm{ClO}_{3}^{-}, \mathrm{ClO}_{4}^{-}$are neutral $\mathrm{HSO}_{4}{ }^{-}$is acidic)
$\mathrm{NaCHO}_{2}-\ldots \mathrm{Na}^{+}+\mathrm{CHO}_{2}^{-}$(this is the first step in a salt soln problem - what ions are present?)

$$
\text { Neutral Basic } \quad \text { Solution will be basic. }
$$

$\mathrm{CHO}_{2}{ }^{-}$is conj base of weak acid $\mathrm{HCHO}_{2}$ - base equil problem - Use ICE (equil.) table (in Molarity)

$$
\mathrm{CHO}_{2}^{-}+\mathrm{H}_{2} \mathrm{O} \rightleftarrows \mathrm{HCHO}_{2}+\mathrm{OH}^{-} \quad\left(\mathrm{Na}^{+} \text {is neutral so ignore it }\right)
$$

| initial | 0.30 | 0 | 0 |
| :---: | :---: | :---: | :---: |
| change | - x | + x | + x |
| equil | $0.30-\mathrm{x}$ | X | X |

Find the pH of the solution - need the $\mathrm{K}_{\mathrm{b}}$ for $\mathrm{CHO}_{2}{ }^{-}$
For a conj. acid base pair : $\mathrm{K}_{\mathrm{a}} \bullet \mathrm{K}_{\mathrm{b}}=\mathrm{K}_{\mathrm{w}}=1.0 \times 10^{-14} \quad \& \quad \mathrm{pK}_{\mathrm{a}}+\mathrm{pK}_{\mathrm{b}}=\mathrm{pK}_{\mathrm{w}}=14.00$
$\mathrm{K}_{\mathrm{b}}=\frac{\left[\mathrm{HCHO}_{2}\right]\left[\mathrm{OH}^{-}\right]}{\left[\mathrm{CHO}_{2}^{-}\right]}=\frac{\mathrm{x}^{2}}{0.30-\mathrm{x}}=\frac{\mathrm{K}_{\mathrm{w}}}{--\mathrm{K}_{\mathrm{a}}}=\frac{1.0 \times 10^{-14}}{1.8 \times 10^{-4}}=5.55 \times 10^{-11}$

Assume $0.30 \gg \mathrm{x}$, so $(0.30-\mathrm{x}) \approx 0.30$
$\frac{\mathrm{x}^{2}}{---30}=5 . \underline{5} 5 \times 10^{-11} ; \quad \mathrm{x}=\left[\mathrm{OH}^{-}\right]=4 . \underline{0} 82 \times 10^{-6}$
$\%$ error $=\frac{4.082 \times 10^{-6}}{0.30} \times---100 \%=0.0014 \%$ error (very good assumption that "x" was small)

$$
\begin{aligned}
& \mathrm{pOH}=-\log \left(4 . \underline{\mathbf{0}} 82 \times 10^{-6}\right)=5.3 \underline{9} \quad(2 \text { s.f. }) \\
& \mathbf{p H}=14.00-5.39=8.6 \underline{1} \text { ( } 2 \text { s.f.) } \\
& \text { or } \begin{aligned}
{\left[\mathrm{H}^{+}\right] } & =\frac{1.0 \times 10^{-14}}{4 .-------0^{-6}}=2.449 \times 10^{-9} \\
\mathrm{pH} & =-\log \left(2.449 \times 10^{-9}\right)=8.61
\end{aligned}
\end{aligned}
$$

Note: The number of sig. fig. in pH and pOH is to the right of the decimal point. While the 2.96 for pOH above appears to have " 3 " sig. fig. in reality it only has 2 , the digits to the right of the decimal. The " 2 " in the 2.96 comes from the power of 10 in the $\left[\mathrm{OH}^{-}\right]$.
4. (2 pts) Identify the Lewis acid and Lewis base in the following reactions. Explain!
a) $\mathrm{CN}^{-}(\mathrm{aq})+\mathrm{H}_{2} \mathrm{O}(\mathrm{l}) \longrightarrow \mathrm{HCN}(\mathrm{aq})+\mathrm{OH}^{-}(\mathrm{aq})$
LB LA LA LB

Lewis Acid : e pair acceptor (something that is electron deficient: $\mathrm{H}^{+}$is technically the Lewis Acid)
Lewis Base : $\mathrm{e}^{-}$pair donor (something with a lone-pair of electrons does not have to have a negative chg)

Bronsted-Lowry theory involves a proton transfer from an acid to a base. The $\mathrm{H}^{+}$literally is pulled off the acid by the base (the $\mathrm{H}^{+}$is transferred, actually moves, from the acid to the base).

In Lewis theory the e- pair does not actually move from one atom to another. Instead the LA combines with the LB and in so doing the LA is accepting a pair of $\mathrm{e}^{-}$from the LB (the LB is donating the $\mathrm{e}^{-}$pair) to form a new bond between the two. A good example is the reaction between $\mathrm{BF}_{3}$ with $\mathrm{NH}_{3}$. The $\mathrm{BF}_{3}$ molecule is overall e-deficient (even though there's electrons on the F atoms the B has only 6 e- around it making it and the molecule e-deficient). The $\mathrm{NH}_{3}$ has an e- pair on the N . Thus, the N atom in $\mathrm{NH}_{3}$ can donate the e-pair to the B in the $\mathrm{BF}_{3}$ to form a new bond and new molecule, $\mathrm{H}_{3} \mathrm{~N}-\mathrm{BF}_{3}$.

The $\mathrm{CN}^{-}$would also be considered a B-L base and the $\mathrm{H}_{2} \mathrm{O}$ would be a B-L acid. Remember, Arrhenius acids and bases are B-L acids and bases and B-L acids and bases are Lewis acids and bases. However, it doesn't necessarily go the other way.
b) $\underset{\mathrm{LA}}{\mathrm{SO}_{2}(\mathrm{~g})}+\underset{\mathrm{LB}}{\mathrm{H}_{2} \mathrm{O}(\mathrm{l})} \longrightarrow \quad \mathrm{H}_{2} \mathrm{SO}_{3}(\mathrm{aq})$

Lewis Acid : $\mathrm{e}^{-}$pair acceptor (something that is electron deficient: the S is "electron deficient" double bonded to the O atoms)

Lewis Base : $\mathrm{e}^{-}$pair donor (something with a lone-pair of electrons - like O atom)

5. (3 pts) Calculate the $\Delta \mathrm{S}(\mathrm{J} / \mathrm{mol} \cdot \mathrm{K})$ of fusion for a compound which melts at $-183.0^{\circ} \mathrm{C}$. The heat of fusion is $2.86 \mathrm{~kJ} / \mathrm{mole}$.

Given the $\Delta \mathrm{H}^{\circ}$ fus and the melting point determine $\Delta \mathrm{S}^{\circ}$ fus .

Fusion, melting, (phase change) is an equilibrium process

$$
\begin{aligned}
& \Delta \mathrm{G}^{\circ}=\Delta \mathrm{H}^{\circ}-\mathrm{T} \cdot \Delta \mathrm{~S}^{\circ}=0 \quad \text { (constant } \mathrm{T}, \text { standard state conditions) } \\
& \Delta \mathrm{S}^{\circ}=-\frac{\Delta \mathrm{H}^{\circ}}{\mathrm{T}}=--2.86 \mathrm{~kJ} / \mathrm{mol}-90.15 \mathrm{~K} \\
& \Delta \mathrm{~S}^{\circ}=0.031724 \mathrm{~kJ} / \mathrm{mol} \cdot \mathrm{~K} \\
& \Delta \mathrm{~S}^{\circ}=31.7 \mathrm{~J} / \mathrm{mol} \cdot \mathrm{~K}
\end{aligned}
$$

This applies to any phase change.

## NOTE:

The temp. in Celsius is given to the first decimal place so you should be adding 273.15 and NOT 273. Adding just 273 often won't make a difference but it can.
6. (4 pts) Predict the sign of $\Delta \mathrm{S}$ of the system or if it's approximately zero for the following reactions and explain your choices.
a) $\mathrm{CaCO}_{3}(\mathrm{~s})+2 \mathrm{HCl}(\mathrm{g}) \rightarrow \mathrm{CaCl}_{2}(\mathrm{~s})+\mathrm{CO}_{2}(\mathrm{~g})+\mathrm{H}_{2} \mathrm{O}(\ell)$
$\Delta \mathrm{S}<0(-)$ The number of moles of gas is decreasing. Generally speaking, when the number of moles of gas decreases in a reaction that leads to an decrease in entropy and $\Delta \mathrm{S}$ is negative. There's also a liquid being formed which is less ordered than a solid but since the liquid is $\mathrm{H}_{2} \mathrm{O}$ it is more ordered than most liquids due to hydrogen bonding. This makes $\Delta \mathrm{S}$ more negative than it would be if a different (less ordered) liquid formed.
$\Delta \mathrm{S}=-78.2 \mathrm{~J} / \mathrm{K}$ (calc. from $\mathrm{S}^{\circ}$ values)
b) $\mathrm{Al}_{2} \mathrm{O}_{3}(\mathrm{~s})+3 \mathrm{H}_{2}(\mathrm{~g}) \rightarrow 2 \mathrm{Al}(\mathrm{s})+3 \mathrm{H}_{2} \mathrm{O}(\mathrm{g})$
$\Delta \mathrm{S}>0(+) \quad$ The number of moles of gas is on each side is the same and there is solid on each side (doesn't matter that much that there are 2 moles of solid in the products compared to 1 mole in the reactants). In this case, I would expect someone to say the change in entropy is small and approx. zero. It would likely be a positive number (inc. in entropy) due to the fact the bent $\mathrm{H}_{2} \mathrm{O}$ molecule has many more rotational and vibrational degrees of freedom than the linear $\mathrm{H}_{2}$ and thus $\mathrm{H}_{2} \mathrm{O}$ many more microstates.
$\Delta \mathrm{S}=+178.8 \mathrm{~J} / \mathrm{K}$ (calc. from $\mathrm{S}^{\circ}$ values)

## The following generally cause an inc. in entropy:

Inc \# gas particles.
solid -> liquid -> gas (phase changes require energy when going to a more disordered state).
Forming a solution ( $\Delta \mathrm{S}_{\text {soln }}>0$ usually, mixing generally leads to more disorder, but not always.).
Inc. V (mainly for gases) - more room for the molecules to move around in, more positions for the gas molecules, more microstates.

Inc. Temp (molecular speeds are more spread out and molecules move around more randomly, more microstates.).

Molecules with more atoms generally have more disorder (greater number of vibrational degrees of freedom).

Inc. with inc. molar mass.
7. ( 5 pts$)$ Determine the entropy of reaction $\left(\Delta \mathrm{S}^{\circ}\right)$ (in $\left.\mathrm{J} / \mathrm{mol}-\mathrm{K}\right)$ for the following reaction at $25^{\circ} \mathrm{C}$.

$$
\begin{aligned}
& 2 \mathrm{CH}_{3} \mathrm{OH}(\ell)+3 \mathrm{O}_{2}(\mathrm{~g}) \rightarrow 2 \mathrm{CO}_{2}(\mathrm{~g})+4 \mathrm{H}_{2} \mathrm{O}(\ell) \\
& \begin{array}{lllll}
\mathrm{S}^{\circ}(\mathrm{J} / \mathrm{mol} \bullet \mathrm{~K}) & 126.8 & 205.0 & 213.6 & 69.91
\end{array} \\
& \Delta \mathbf{S}^{0}=\sum_{\text {products }} \mathbf{n} \mathbf{S}_{\text {products }}^{0}-\sum_{\text {reactants }} \mathbf{m} \mathbf{S}_{\text {reactants }}^{0} \\
& \Delta \mathrm{~S}^{\circ}=[(2 \mathrm{~mol})(213.6 \mathrm{~J} / \mathrm{mol} \cdot \mathrm{~K})+(4 \mathrm{~mol})(69.91 \mathrm{~J} / \mathrm{mol} \cdot \mathrm{~K})] \\
& {[(2 \mathrm{~mol})(126.8 \mathrm{~J} / \mathrm{mol} \cdot \mathrm{~K})+(3 \mathrm{~mol})(205.0 \mathrm{~J} / \mathrm{mol} \cdot \mathrm{~K})]} \\
& =[706 . \underline{8} 4 \mathrm{~J} / \mathrm{K}]-[868 . \underline{\mathbf{6}} \mathrm{J} / \mathrm{K}] \\
& =-161.8 \mathrm{~J} / \mathrm{K} \quad \text { (A fairly large neg } \Delta \mathrm{S}^{\circ} \text {, as you might expect; } 3 \mathrm{~mol} \text { gas }->2 \mathrm{~mol} \text { gas } \\
& \text { and } \mathrm{H}_{2} \mathrm{O} \text { is more ordered than } \mathrm{CH}_{3} \mathrm{OH} \text { since } \mathrm{H}_{2} \mathrm{O} \text { forms more } \mathrm{H} \text {-bonds } \\
& \text { per molecule and has fewer degrees of freedom.) }
\end{aligned}
$$

8. (3 pts) Write the reaction for the formation of $\mathrm{NH}_{4} \mathrm{NO}_{3}(\mathrm{~s})$ which corresponds to $\Delta \mathrm{H}_{\mathrm{f}}{ }^{\circ}$ and $\Delta \mathrm{G}_{\mathrm{f}}{ }^{\circ}$ and explain why you've written it the way you have.
$\Delta \mathrm{H}_{\mathrm{f}}{ }^{\circ}$ and $\Delta \mathrm{G}_{\mathrm{f}}{ }^{\circ}$ for a substance correspond to the formation of 1 mole of the substance from its elements in their standard states at a given temp. of interest.

$$
\mathrm{N}_{2}(\mathrm{~g})+2 \mathrm{H}_{2}(\mathrm{~g})+3 / 2 \mathrm{O}_{2}(\mathrm{~g}) \rightarrow \mathrm{NH}_{4} \mathrm{NO}_{3}(\mathrm{~s})
$$

Note: On the right there is only 1 mole of 1 substances. On the left there are only elements. For the elements in this reaction their standard states at $25^{\circ} \mathrm{C}$ are the gas state (i.e. they exist as gases at 1 atm and $25^{\circ} \mathrm{C}$ ). The temp of $25^{\circ} \mathrm{C}$ is not part of the standard state definition but is our reference temp.
9. (3 pts) Given $\Delta \mathrm{G}^{\circ}=-3217.4 \mathrm{~kJ} / \mathrm{mol}$ and the listed $\Delta \mathrm{G}^{\circ}{ }_{\mathrm{f}}$ values calculate $\Delta \mathrm{G}^{\circ}{ }_{\mathrm{f}}$ for $\mathrm{SO}_{2}(\mathrm{~g})$..

$$
\begin{aligned}
& 4 \mathrm{FeS}_{2}(\mathrm{~s})+11 \mathrm{O}_{2}(\mathrm{~g}) \longrightarrow 2 \mathrm{Fe}_{2} \mathrm{O}_{3}(\mathrm{~s})+8 \mathrm{SO}_{2}(\mathrm{~g}) \quad \Delta \mathrm{G}^{\circ}=-3217.4 \mathrm{~kJ} / \mathrm{mol} \\
& \Delta \mathrm{G}_{\mathrm{f}}{ }^{\circ}(\mathrm{kJ} / \text { mole }) \quad-166.7 \quad 0.0 \quad-740.9 \quad ? \\
& \Delta \mathrm{G}^{\mathrm{o}}=\sum_{\text {products }} \mathbf{n} G_{\mathrm{f}, \text { products }}^{\mathrm{o}}-\sum_{\text {reactants }} \mathbf{m} \mathrm{G}_{\mathrm{f}, \text { reactants }}^{\mathrm{o}} \\
& \Delta \mathrm{G}^{\circ}=\left[(2 \mathrm{~mol})\left(\Delta \mathrm{G}_{\mathrm{f}}{ }^{\circ}\left(\mathrm{Fe}_{2} \mathrm{O}_{3}(\mathrm{~s})\right)\right)+(8 \mathrm{~mol})\left(\Delta \mathrm{G}_{\mathrm{f}}{ }^{\circ}\left(\mathrm{SO}_{2}(\mathrm{~g})\right)\right)\right]- \\
& {\left[(4 \mathrm{~mol})\left(\Delta \mathrm{G}_{\mathrm{f}}{ }^{\circ}\left(\mathrm{FeS}_{2}(\mathrm{~s})\right)\right)-(11 \mathrm{~mol})\left(\Delta \mathrm{G}_{\mathrm{f}}{ }^{\circ}\left(\mathrm{O}_{2}(\mathrm{~g})\right)\right)\right]} \\
& \Delta \mathrm{G}^{\circ}=[(2 \mathrm{~mol})(-740.9 \mathrm{~kJ} / \mathrm{mol})+(8 \mathrm{~mol})(\mathrm{x})]- \\
& \text { [(4 mol) }(-166.7 \mathrm{~kJ} / \mathrm{mol})-(11 \mathrm{~mol})(0.0 \mathrm{~kJ} / \mathrm{mol})] \\
& -3217.4 \mathrm{~kJ}=[-1481.8 \mathrm{~kJ}+8 \mathrm{x}]-[-666.8 \mathrm{~kJ}] \\
& 8 \mathrm{x}=-2402.4 \mathrm{~kJ} \\
& \mathrm{x}=-300.3 \mathrm{~kJ} \\
& \Delta \mathrm{G}_{\mathrm{f}}{ }^{\circ}\left(\mathrm{SO}_{2}(\mathrm{~g})\right)=-300.3 \mathrm{~kJ}
\end{aligned}
$$

10. ( 5 pts ) For the following reaction $\Delta \mathrm{H}^{\circ}$ is $-150.5 \mathrm{~kJ} / \mathrm{mol}, \Delta \mathrm{S}^{\circ}$ is $-293.1 \mathrm{~J} / \mathrm{K} \cdot \mathrm{mol}$ at $25^{\circ} \mathrm{C}$. Assuming these don't change with temperature what is the value of $\Delta \mathrm{G}^{\circ}(\mathrm{kJ} / \mathrm{mol})$ at $141.0^{\circ} \mathrm{C}$ ?

$$
\mathrm{A}_{2}(\mathrm{~g})+2 \mathrm{~B}_{2}(\mathrm{~g}) \rightarrow 2 \mathrm{AB}_{2}(\mathrm{~g})
$$

Assume $\Delta \mathrm{H}^{\circ}$ and $\Delta \mathrm{S}^{\circ}$ are constant over this temperature range. They do change with temp. but the change is fairly small and much smaller than the variation of $\Delta \mathrm{G}^{\circ}$ with temp. The $\Delta \mathrm{G}^{\circ}$ given has no bearing on the problem.

$$
\begin{aligned}
\Delta \mathrm{G}^{\circ} & =\Delta \mathrm{H}^{\circ}-\mathrm{T} \cdot \Delta \mathrm{~S}^{\circ} \\
& =(-150.5 \mathrm{~kJ} / \mathrm{mol})-(414 . \underline{1} 5 \mathrm{~K}) \cdot(-0.2931 \mathrm{~kJ} / \mathrm{mol} \bullet \mathrm{~K}) \\
& =-29 . \underline{1} 12=-29.1 \mathrm{~kJ} / \mathrm{mol}
\end{aligned}
$$

11. ( 13 pts ) Given $\Delta \mathrm{H}^{\circ}=-71.75 \mathrm{~kJ}$ and $\Delta \mathrm{S}^{\circ}=-268.0 \mathrm{~J} / \mathrm{mol} \cdot \mathrm{K}$ for the following reaction at $25^{\circ} \mathrm{C}$,

$$
3 \mathrm{NO}_{2}(\mathrm{~g})+\mathrm{H}_{2} \mathrm{O}(\ell) \rightarrow 2 \mathrm{HNO}_{3}(\ell)+\mathrm{NO}(\mathrm{~g})
$$

a) ( 2 pts ) Calculate the $\Delta \mathrm{G}^{\circ}$ of the reaction at $25^{\circ} \mathrm{C}$. Is the reaction spontaneous or nonspontaneous at this temperature under standard state conditions? Show all work and explain.

$$
\begin{aligned}
\Delta \mathrm{G}^{\circ} & =\Delta \mathrm{H}^{\circ}-\mathrm{T} \Delta \mathrm{~S}^{\circ} \\
& =-71.75 \mathrm{~kJ}-(298.15 \mathrm{~K})(-0.2680 \mathrm{~kJ} / \mathrm{K})
\end{aligned}
$$

$$
=+8.15 \mathrm{~kJ} \quad \Delta \mathrm{G}^{\circ}>0 \quad \text { NONspontaneous under standard conditions }
$$ (nonspont. to products, but small so significant amounts of reactants and products at equil. )

$$
\Delta \mathrm{H}^{\circ}<0 \quad \text { and } \quad \Delta \mathrm{S}^{\circ}<0 \quad \text { so rxn is spont at "low" temp }
$$

(becomes more spont as temp dec and less spont as temp inc.)
b) ( 4 pts ) If the reaction is nonspontaneous, at what temperature would it be spontaneous. If the reaction is spontaneous, at what temperature would it be nonspontaneous. If the reaction will always be spontaneous at all temperatures or never be spontaneous at any temperature state that. Show ALL work \& explain!

Rxn. is NONspont. at $\mathrm{T}=25^{\circ} \mathrm{C}$. At what temp will it become spont., i.e. at what temp will $\Delta \mathrm{G}^{\circ}<0$

$$
\Delta \mathrm{H}^{\circ}<0 \quad \text { and } \quad \Delta \mathrm{S}^{\circ}<0 \quad \text { so rxn is spont at "low" temp }
$$

(becomes more spont as temp dec and less spont as temp inc.)

$$
\begin{aligned}
& \Delta \mathrm{G}^{\circ}=\Delta \mathrm{H}^{\circ}-\mathrm{T} \Delta \mathrm{~S}^{\circ}<0 \\
& \Delta \mathrm{H}^{\circ}<\mathrm{T} \Delta \mathrm{~S}^{\circ} \\
& -71.75 \mathrm{~kJ}<\mathrm{T}(-0.2680 \mathrm{~kJ} / \mathrm{K}) \\
& -71.75 \mathrm{~kJ} \quad--\mathrm{T} \quad(\text { Remember, when multiply or divide by a negative number an inequality } \\
& \begin{array}{c}
(-0.2680 \mathrm{~kJ} / \mathrm{K})
\end{array}
\end{aligned}
$$

$$
\mathrm{T}<267 . \underline{2} \mathrm{~K} \quad \mathrm{~T}<267.7^{\circ} \mathrm{C} \quad \text { (becomes spont. at temp below this) }
$$

(becomes more spont as temp dec)
***** cont. next page ${ }^{* * * * *}$
11. (Cont.)
c) ( 2 pts) What is the equilibrium constant at $25^{\circ} \mathrm{C}$ ? Show all work and explain.

$$
\begin{aligned}
& \Delta \mathrm{G}^{\circ}=-\mathrm{RT} \operatorname{lnK} \\
& \ln \mathrm{~K}=-\Delta \mathrm{G}^{\circ} / \mathrm{RT}=-\left(8.15 \times 10^{3} \mathrm{~J}\right) /\{(8.314 \mathrm{~J} / \mathrm{K})(298.15 \mathrm{~K})\}=-3.28 \underline{7} 85(3 \text { s.f.) } \\
& \mathrm{K}=\mathrm{e}^{-3.28785}=3.73 \times 10^{-2} \begin{array}{l}
\text { (fairly small but not extremely small - mostly reactants at } \\
\text { equilibrium, but not "only" reactants. This is more likely } \\
\text { appreciable amounts of reactants and products at equil.) }
\end{array}
\end{aligned}
$$

d) $(1 \mathrm{pt})$ This $\Delta \mathrm{G}^{\circ}$ and K corresponds to an equilibrium that is: (choose one from below \& explain)

1) closer to products
2) closer to reactants
3) midway between reactants and products (significant amounts of both at equilibrium)
$\Delta \mathrm{G}^{\circ}$ positive but small. Since $\mathrm{K}<1$ the reaction lies toward reactant. However, the $\Delta \mathrm{G}^{\circ}$ and K are small so there's significant amount of reactants and products at equil.)
e) ( 4 pts ) Is the reaction spontaneous or nonspontaneous at $25^{\circ} \mathrm{C}$ when the pressures of $\mathrm{NO}_{2}$ and NO are 2.50 atm and 0.50 atm , respectively? Show all work and explain.

$$
\begin{aligned}
& \Delta \mathrm{G}=\Delta \mathrm{G}^{\circ}+\mathrm{RT} \ln (\mathrm{Q}) \quad \mathrm{T} \text { in kelvin; } \mathrm{R} \text { converted to } \mathbf{k J} / \mathrm{K} \\
& \\
& \\
& \mathrm{Q}=-\frac{\mathrm{P}_{\mathrm{NO}}}{\left(\mathrm{P}_{\mathrm{NO} 2}\right)^{3}}=-\frac{0.50}{(2.50)^{3}}=0.032 \\
& \begin{aligned}
\Delta \mathrm{G} & =8.15 \mathrm{~kJ}+\left(8.314 \times 10^{-3} \mathrm{~kJ} / \mathrm{K}\right)(298.15 \mathrm{~K}) \ln (0.032) \\
& =8.15 \mathrm{~kJ}-8.532 \mathrm{~kJ} \\
& =-0.38 \mathrm{~kJ}
\end{aligned}
\end{aligned}
$$

$\Delta \mathrm{G}<0 \quad$ spontaneous under these pressure and temperature conditions

